

## Integers

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## Lesson Menu

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Main Ideas and Vocabulary
Example 1: Write Integers for Real-World Situations
Example 2: Compare Two Integers
Example 3: Real-World Example
Key Concept: Absolute Value
Example 4: Expressions with Absolute Value
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## Main Ideas

- Compare and order integers.
- Find the absolute value of an expression.


## New Vocabulary

- negative number
- integers
- coordinate
- inequality
- absolute value


## EXAMPLE Write Integers for Real-World Situations

(1) Write an integer for each situation.
A. 32 feet underground -32
B. 8 weeks after birth +8
C. a loss of 6 pounds -6

## CHECK Your Progress

(1) A. Write an integer for a loss of 12 yards.
A. 12
(B.) -12
C. both A and B
D. neither A nor B


## C) CHECK Your Progress

(1) B. Write an integer for 15 feet above sea level.
(A.) 15
B. -15
C. both A and B
D. neither A nor B


## CHECK Your Progress

(1) C. Write an integer for the temperature decreased by 4 degrees.
A. 4
(B.) -4
C. both A and B
D. neither A nor B

(8) Math Chapter

RESOURGES $\square \sqrt{ } \sqrt{ }$

## EXAMPLE Compare Two Integers

(2) A. Use the integers graphed on the number line below for each question. Write two inequalities involving 7 and -4 .


Answer: Since 7 is to the right of -4 , write $7>-4$. Since -4 is to the left of 7 , write $-4<7$.

## EXAMPLE Compare Two Integers

(2) B. Use the integers graphed on the number line below for each question. Replace the • with <, >, or = in -2 • 3 to make a true sentence.


Answer: -2 is less since it lies to the left of 3 . So write $-2<3$.

## CHECK Your Progress

(2) A. Use the integers graphed on the number line below for each question. Write two inequalities involving -4 and 1.

(A.) $-4<1,1\rangle-4$
B. $-4<1,1<-4$
C. $-4>1,1>-4$
D. $-4>1,1<-4$

## STCHECK Your Progress,

(2) B. Use the integers graphed on the number line below for each question. Replace the • with <, >, or = in 6•-7 to make a true sentence.

A. <
B. $>$
C. =
D. none of the above

## Real-World EXAMPLE

(3) WEATHER The high temperatures for the first seven days of January were $-8^{\circ}, 10^{\circ}, 2^{\circ},-3^{\circ},-11^{\circ}$, $0^{\circ}$, and $1^{\circ}$. Order the temperatures from least to greatest.
Graph each integer on a number line.


Write the numbers as they appear from left to right.
Answer: The temperatures $-11^{\circ},-8^{\circ},-3^{\circ}, 0^{\circ}, 1^{\circ}, 2^{\circ}$, $10^{\circ}$ are in order from least to greatest.

## ChIECK Your Progress:

(3) FOOTBALL The yards gained during the first six plays of the football game were $5,-3,12,-9,6$, and -1 . Order the yards from least to greatest.
A. $-1,-3,5,6,-9,12$
B. $12,6,5,-1,-3,-9$
C. $5,6,12,-9,-3,-1$

$$
\triangle \mathrm{A} \square \mathrm{~B} \square \mathrm{C} \square \mathrm{D}
$$

(D. $-9,-3,-1,5,6,12$

## Integers and Absolute Value

## KEY CONCEPT

## Abolute Value

Words
The absolute value of a number is the distance the number is from zero on the number line. The absolute value of a number is always greater than or equal to zero.
Examples $|5|=5 \quad|-5|=5$

## EXAMPLE Expressions with Absolute Value

(4) A. Evaluate $|5|$.

$|5|=5 \quad$ The graph of 5 is 5 units from 0.
Answer: 5

## EXAMPLE Expressions with Absolute Value

(4) B. Evaluate $|-8|+|-1|$.

$$
|-8|+|-1|=8+1
$$

The absolute value of -8 is 8 . The absolute value of -1 is 1 .

$$
=9 \quad \text { Simplify }
$$

## Answer: 9

## $\int$ ClECK Your Progress

(4) A. Evaluate $|-9|$.
A. -9
(B. 9
C. $-\frac{1}{9}$
D. $\frac{1}{9}$

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## shentec Your Progress:

(4) B. Evaluate $|-9|+|2|$.

$$
\text { A. } 7
$$

B. -7
(C.) 11
D. -11


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## EXAMPLE

Algebraic Expressions with Absolute Value
(5) ALGEBRA Evaluate $|x|-8$ if $x=-2$.

$$
\begin{aligned}
|x|-8 & =|-2|-8 \\
& =2-8 \\
& =-6
\end{aligned}
$$

Replace $x$ with -2.
The absolute value of -2 is 2 .
Simplify.

Answer: -6

## arenteck rour Progress

(5) ALGEBRA Evaluate $5-|x|$ if $x=9$.
A. 14
B. 4
C. -14
(D.) -4

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## Lesson Menu

Five-Minute Check (over Lesson 2-1)
Main Ideas and Vocabulary
Example 1: Add Integers on a Number Line
Key Concept: Adding Integers with the Same Sign
Example 2: Add Integers with the Same Sign
Example 3: Add Integers on a Number Line
Key Concept: Adding Integers with Different Signs
Example 4: Add Integers with Different Signs
Example 5: Real-World Example
Key Concept: Additive Inverse Property
Example 6: Add Three or More Integers

## Main Ideas

- Add two Integers.
- Add more than two integers.


## New Vocabulary

- opposites
- additive inverse


## EXAMPIE Add Integers on a Number Line

(1) Find $3+4$.


Start at zero.
Move three units to the right.
From there, move four more units to the right.
Answer: $3+4=7$

## dichteck rour Progeress

(1) Find $-2+-5$.
A. 7
(B. -7
C. 3
D. -3


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## Adding Integers

## KEY CONCEPT

## Adding Integers with the Same Sign

Words To add integers with the same sign, add their absolute values. The sum is:

- positive if both integers are positive.
- negative if both integers are negative.

$$
\text { Examples }-5+(-2)=-7 \quad 6+3=9
$$

## EXAMPLE Add Integers with the Same Sign

(2) Find $-5+(-4)$.

$$
\begin{array}{ll}
-5+(-4)=-9 & \text { Add }|-5| \text { and }|-4| . \text { Both numbers are } \\
& \text { negative, so the sum is negative. }
\end{array}
$$

Answer: -9

## CHECK Your Progress

(2) Find $-3+-8$.
A. 5
B. -5
C. 11
(D.) -11

## EXAMPLE Add Integers on a Number Line

(3) A. Find $7+(-11)$.


Start at zero.
Move 7 units to the right.
From there, move 11 units to the left.
Answer: $7+(-11)=-4$

## EXAMPLE Add Integers on a Number Line

(3) B. Find $-2+9$.


Start at zero.
Move 2 units to the left.
From there, move 9 units to the right.
Answer: $-2+9=7$

## CHECK Your Progress

(3) A. Find $-5+8$.
A. 13
B. -13

0\%
C. 3
D. -3

## S

(3) B. Find $3+(-6)$.
A. 3
(B.) -3
$0 \%$
C. 9
D. -9

## Adding Integers

## KEY CONCEPT

## Adding Integers with Different Signs

To add integers with different signs, subtract their absolute values. The sum is:

- positive if the positive integer's absolute value is greater.
- negative if the negative integer's absolute value is greater.


## EXAMPLE Add Integers with Different Signs

(4) A. Find $-9+10$.

$$
\begin{array}{ll}
-9+10=1 & \text { To find }-9+10, \text { subtract }|9| \text { from }|10| . \\
& \text { The sum is positive because }|10|>|9| .
\end{array}
$$

Answer: 1

## EXAMPLE Add Integers with Different Signs

(4) B. Find $8+(-15)$.

$$
\begin{array}{ll}
8+(-15)=-7 & \text { To find } 8+(-15) \text {, subtract }|8| \text { from }|-15| . \\
& \text { The sum is negative because }|-15|>|8| .
\end{array}
$$

Answer: -7

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(4) A. Find $-6+11$.
(A.) 5
B. -5
C. 17
D. -17

## /2대ECK Your Progress:

(4) B. Find $4+(-7)$.

## A. 11

B. -11
C. 3
(D.) -3


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## Real-World EXAMPLE

(5) WEATHER On February 1, the temperature at dawn was $-22^{\circ}$ F. By noon, it had risen 19 degrees. What was the temperature at noon?

Words The temperature at dawn was $-22^{\circ} \mathrm{F}$. It had risen 19 degrees by noon. What was the temperature at noon?
Variable Let $x=$ the temperature at noon.


Real-World EXAMPLE
(5) Solve the equation.
$-22+19=x \quad$ To find the sum, subtract |19| from |-22|.
$-3=x \quad$ The sum is negative because $|-22|>|19|$.

Answer: The temperature at noon was $-3^{\circ} \mathrm{F}$.
(5) HIKING Dave started his hike at 32 feet below sea level. During the hike he gained an altitude of 29 feet. At what altitude did Dave complete his hike?
A. 3 feet above sea level
B. 3 feet below sea level
C. 61 feet above sea level
D. 61 feet below sea level


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## Adding Integers

## KEY CONCEPT

## Additive Inverse Property

Words The sum of any number and its additive inverse is zero.
Symbols $\quad x+(-x)=0 \quad$ Example $6+(-6)=0$

## EXAMPLE Add Three or More Integers

(6) A. Find $-8+(-4)+8$.

$$
\begin{array}{rlrl}
-8+(-4)+8 & =-8+8+(-4) & & \text { Commutative Property } \\
& =0+(-4) & & \text { Additive Inverse Property } \\
& =-4 & & \text { Identity Property of } \\
& & \text { Addition }
\end{array}
$$

Answer: -4

## EXAMPLE Add Three or More Integers

(6) B. Find $6+(-3)+(-9)+2$.

$$
\begin{array}{rlrl}
6+(-3)+(-9)+2 & =6+2+(-3)+(-9) & \begin{array}{l}
\text { Commutative } \\
\text { Property }
\end{array} \\
& =[6+2]+[-3+(-9)] & \begin{array}{l}
\text { Associative } \\
\text { Property }
\end{array} \\
& =8+(-12) \text { or }-4 & & \text { Simplify. }
\end{array}
$$

Answer: -4

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(6) A. Find $3+(-9)+(-3)$.
(A.) -9
B. -3

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C. 3
D. 15

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(6) B. Find $-2+11+(-4)+5$.
A. -22
B. -8
C. 0


## Lesson Menu

Five-Minute Check (over Lesson 2-2)
Main Ideas
Key Concept: Subtracting Integers
Example 1: Subtract a Positive Integer
Example 2: Subtract a Negative Integer
Example 3: Real-World Example
Example 4: Evaluate Algebraic Expressions

## Main Ideas

- Subtract Integers.
- Evaluate expressions containing variables.


## KEY CONCEPT

## Subtracting Integers

Words To subtract an integer, add its additive inverse.
Symbols $\quad a-b=a+(-b)$

# COncepts in MQtion 

BrainPOP:
Adding and Subtracting Integers

## EXAMPIE Subtract a Positive Integer

(1) A. Find 9-14.

$$
\begin{aligned}
9-14 & =9+(-14) & & \text { To subtract } 14, \text { add }-14 . \\
& =-5 & & \text { Simplify. }
\end{aligned}
$$

Answer: -5

## EXAMPIE Subtract a Positive Integer

(1) B. Find $-10-8$.

$$
\begin{aligned}
-10-8 & =-10+(-8) \\
& =-18
\end{aligned}
$$

To subtract 8, add -8 .
Simplify.

Answer: -18

## STCHECK Your Progress,

(1) A. Find 6-8.
A. 2
(B.) $\mathbf{- 2}$
C. -3
D. 14


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(1) B. Find -9-13.

$$
\text { (A.) }-22
$$

B. -4
C. 4
D. 22

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## EXAMPIE Subtract a Negative Integer

(2) A. Find 15 - (-4).

$$
\begin{aligned}
15-(-4) & =15+4 & & \text { To subtract }-4, \text { add } 4 . \\
& =19 & & \text { Simplify. }
\end{aligned}
$$

Answer: 19

## EXAMPLE Subtract a Negative Integer

(2) B. Find $-11-(-7)$.
$-11-(-7)=-11+7 \quad$ To subtract -7 , add 7.

$$
=-4 \quad \text { Simplify }
$$

Answer: -4

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(2) A. Find $8-(-2)$.
A. 6
(B.) 10
C. -6
D. 16

## 

(2) B. Find -12 - (-5).
A. 17
B. 7
C. -17
D. -7

## Real-World EXAMPLE

(3) WEATHER The table shows the record high and low temperatures recorded in selected states. What is the range of temperatures for West Virginia?

| State | Lowest <br> Temperature ( ${ }^{\circ}$ F) | Highest <br> Temperature ( ${ }^{( } \mathbf{F}$ ) |
| :--- | :---: | :---: |
| Utah | -69 | 117 |
| Vermont | -50 | 105 |
| Virginia | -30 | 110 |
| Washington | -48 | 118 |
| West Virginia | -37 | 112 |

Source: The World Almanac

## Real-World EXAMPLE

(3) Explore

You know the highest and lowest temperatures. You need to find the range for West Virginia's temperatures.
Plan
To find the range, or difference, subtract the lowest temperature from the highest temperature.
Solve

$$
\begin{aligned}
112-(-37) & =112+37 & & \begin{array}{l}
\text { To subtract }-37, \\
\text { add } 37 .
\end{array} \\
& =149 & & \text { Add } 112 \text { and } 37 .
\end{aligned}
$$

Answer: The range for West Virginia is $149^{\circ} \mathrm{F}$.
(3) Examine

Think of a thermometer. The difference between $112^{\circ}$ above zero and $37^{\circ}$ below zero must be $112^{\circ}+37^{\circ}$ or $149^{\circ}$. The answer appears to be reasonable.

## C）ClRCK Your Progress

（3）WEATHER The table shows the record high and low temperatures recorded in selected states．What is the range for Washington？

| State | Lowest <br> Temperature（ $\left.{ }^{\circ} \mathrm{F}\right)$ | Highest <br> Temperature（ ${ }^{\circ} \mathrm{F}$ ） |
| :--- | :---: | :---: |
| Utah | -69 | 117 |
| Vermont | -50 | 105 |
| Virginia | -30 | 110 |
| Washington | -48 | 118 |
| West Virginia | -37 | 112 |

Source：The World Almanac

A． $75 \%$
B． $70^{\circ} \mathrm{F}$
C． $\mathbf{1 6 6}^{\circ} \mathrm{F}$
D． $149^{\circ} \mathrm{F}$

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## EXAMPLE Evaluate Algebraic Expressions

(4) A. Evaluate $m-(-2)$ if $m=4$.

$$
\begin{array}{rlrl}
m-(-2) & =4-(-2) & & \text { Write the expression. } \\
& =4+2 & & \text { Replace } m \text { with } 4 . \\
& =6 & & \text { To subtract }-2, \text { add } 2 . \\
& & \text { Add } 4 \text { and } 2 .
\end{array}
$$

Answer: 6

## EXAMPIE Evaluate Algebraic Expressions

(4) B. Evaluate $x-y$ if $x=-14$ and $y=-2$.

$$
\begin{aligned}
x-y & =-14-(-2) & & \begin{array}{l}
\text { Write the expression. Replace } \\
\\
\end{array} \\
& =-14+2 & & \text { with }-14 \text { and } y \text { with }-2 . \\
& =-12 & & \text { To subtract }-2, \text { add } 2 .
\end{aligned}
$$

Answer: -12

## ChECK Your Progress:

(4) A. Evaluate $p-(-6)$ if $p=-4$.
A. 10
B. $\mathbf{- 2}$
(C. 2
D. -10

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## CHECK Your Progress:

(4) B. Evaluate $m-n$ if $m=-9$ and $n=-3$.

$$
\text { A. }-12
$$

(B.) -6
C. 6
D. -27

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## Lesson Menu

Five-Minute Check (over Lesson 2-3)
Main Ideas
Key Concept: Multiplying Integers with Different Signs
Example 1: Multiply Integers with Different Signs
Key Concept: Multiplying Integers with the Same Sign
Example 2: Multiply Integers with the Same Sign
Example 3: Standardized Test Example
Example 4: Simplify and Evaluate Algebraic Expressions

## Main Ideas

- Multiply integers.
- Simplify algebraic expressions.


## KEY CONCEPT

## Multiplying Integers with Different Signs

Words The product of two integers with different signs is negative.
Examples $4(-3)=-12 \quad-3(4)=-12$

## EXAMPI: Multiply Integers with Different Signs

(1) A. Find 8(-9).

$$
\begin{array}{ll}
8(-9)=-72 & \begin{array}{l}
\text { The factors have different signs. The } \\
\text { product is negative. }
\end{array}
\end{array}
$$

Answer: -72

## EXAMPI: Multiply Integers with Different Signs

(1) B. Find -9(11).

$$
-9(11)=-99
$$

The factors have different signs. The product is negative.

Answer: -99

## C) CriECK Your Progress

(1) A. Find-4(12).
A. -3
B. -46
C. 48

$$
\text { (D.) }-48
$$



## shlyeck Your Progress,

(1) B. Find 6(-2).
A. 12
(B.) -12
C. -3
D. -8

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## KEY CONCEPT

## Multiplying Integers with the Same Sign

Words The product of two integers with the same sign is positive.

$$
\text { Examples } 4(3)=12 \quad-4(-3)=12
$$

## EXAMPI: Multiply Integers with the Same Sign

(2) A. Find -4(-16).

$$
\begin{array}{ll}
-4(-16)=64 & \begin{array}{l}
\text { The factors have the same sign. The } \\
\text { product is positive. }
\end{array}
\end{array}
$$

Answer: 64

## EXAMPLE Multiply Integers with the Same Sign

(2) B. Find -9(-3)(-2).

$$
\begin{aligned}
-9(-3)(-2) & =[(-9)(-3)](-2) & & \text { Associative Property } \\
& =(27)(-2) & & (-9)(-3)=27 \\
& =-54 & & (27)(-2)=-54
\end{aligned}
$$

Answer: -54

## SHAECK Your Progress:

(2) A. Find -3(-8).
(A. 24
B. $\mathbf{- 2 4}$
C. -11
D. 23

## 0\%



## S C.WECK Your Progress,

(2) B. Find $-7(11)(-4)$.
A. 0
B. -81

0\%
C. 308
D. -308

## Standardized Test EXAMPLE

(3) A student missed only 4 problems on a test, each worth 20 points. What integer represents the total number of points earned for those questions?

A - 5
B -20
C 24
D -80
Read the Test Item
The word missed means losing points, so the loss per problem is -20 . Multiply 4 times -20 to find the total number of points lost.

Standardized Test EXAMPLE
(3) Solve the Test Item
$4(-20)=-80 \quad$ The product is negative.

Answer: The answer is D.

## ChIECK Your Progress

(3) FOOTBALL A football team loses 3 yards on each of 3 consecutive plays. Find the total yards lost.
A. -3
B. 6

0\%
C. -9
(D. 9

## EXAMPLE

## Simplify and Evaluate Algebraic Expressions

(4) A. Simplify $8 a(-5 b)$.

$$
\begin{array}{rlrl}
8 a(-5 b) & =(8)(a)(-5)(b) & & \\
& =(8 \bullet-5)(a \bullet b) & & \text { Commutative Property of } \\
& =-40 a b & & \text { Multiplication } \\
& & (8 \bullet-5)=-40, a \bullet b=a b
\end{array}
$$

Answer: -40ab

## EXAMPLE

## Simplify and Evaluate Algebraic Expressions

(4) B. Evaluate $-3 x y$ if $x=-4$ and $y=9$.

$$
\begin{aligned}
-3 x y & =-3(-4)(9) \\
& =[-3(-4)](9) \\
& =12(9) \\
& =108
\end{aligned}
$$

Replace $x$ with -4 and $y$ with 9.

Associative Property of Multiplication
The product of -3 and -4 is positive.
The product of 12 and 9 is positive.

Answer: 108

## C) CriECK Your Progress

(4) A. Simplify $-6(2 c)$.
A. $12 c$
(B.) $-12 c$
C. $8 c$
D. $-8 c$

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## STCHECK Your Progress,

(4) B. Simplify $5 m(-7 n)$.
A. $-2 m n$
B. $-12 m n$
C. $35 m n$
(D.) $-35 m n$


## STCHECK Your Progress,

(4) $C$. Evaluate $-9 a b$ if $a=-3$ and $b=-6$.

$$
\text { A. } 81
$$

B. 162
(C.) -162
D. -81


## Lesson Menu

Five-Minute Check (over Lesson 2-4)
Main Ideas and Vocabulary
Key Concept: Dividing Integers with the Same Sign

## Example 1: Divide Integers with the Same Sign

Key Concept: Dividing Integers with Different Signs
Example 2: Divide Integers with Different Signs
Example 3: Evaluate Algebraic Expressions
Example 4: Real-World Example
Concept Summary: Operations with Integers

## Main Ideas

- Divide Integers.
- Find the average of a set of data.

New Vocabulary

- mean


## KEY CONCEPT

## Dividing Integers with the Same Sign

Words The quotient of two integers with the same sign is positive.
Examples $-12 \div(-3)=4$
$12 \div 3=4$

## EXAMPLE Divide Integers with the Same Sign

(1) A. Find $-28 \div(-4)$.
$-28 \div(-4)=7 \quad$ The quotient is positive.

Answer: 7

## EXAMPIE Divide Integers with the Same Sign

(1) B. Find $\frac{96}{8}$.

$$
\begin{aligned}
\frac{96}{8} & =96 \div 8 \quad \text { The quotient is positive. } \\
& =12
\end{aligned}
$$

Answer: 12

## CHECK Your Progress:

(1) A. Find $35 \div 7$.
(A.) 5
B. 6
C. 28
D. 42


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(1) B. Find $\frac{-36}{-4}$.
(A. 9
B. -8
C. -32
D. -9

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## Dividing Integers

## KEY CONCEPT

## Dividing Integers with Different Signs

Words The quotient of two integers with different signs is negative.
Examples $-12 \div 4=-3 \quad 12 \div(-4)=-3$

## EXAMPLE Divide Integers with Different Signs

(2) A. Find $54 \div(-3)$.
$54 \div(-3)=-18 \quad$ The quotient is negative.

Answer: -18

## EXAMPLE Divide Integers with Different Signs

(2) B. Find $\frac{-42}{6}$.

$$
\begin{aligned}
\frac{-42}{6} & =-42 \div 6 & & \text { The quot } \\
& =-7 & & \text { Simplify. }
\end{aligned}
$$

Answer: -7
(2) A. Find $72 \div(-8)$.
A. 9
(B.) -9
C. -8
D. 7

## STHECK Your Progress,

(2) B. Find $\frac{-36}{4}$.
(A.) -9
B. 9
C. -32
D. -7

## $0 \%$


$\square \mathrm{A} \square \mathrm{B} \square \mathrm{C} \square \mathrm{D}$
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## EXAMPLE Evaluate Algebraic Expressions

(3) Evaluate $6 x \div y$, if $x=-4$ and $y=-8$.

$$
\begin{aligned}
6 x \div y & =6(-4) \div(-8) & & \text { Replace } x \text { with }-4 \text { and } y \text { with }-8 . \\
& =-24 \div(-8) & & \text { Simplify. } \\
& =3 & &
\end{aligned}
$$

Answer: 3
(3) Evaluate $-4 m \div n$ if $m=-9$ and $n=-3$.

$$
\text { (A.) }-12
$$

B. -16
C. 12
D. 33

## Real-World EXAMPLE

(4) EXAM SCORE Ian had exam scores of $89,98,96,97$, and 95 . Find the mean (average) of his exam scores.
$\frac{89+98+96+97+95}{5}=\frac{475}{5}$
Find the sum of the quiz scores. Divide by the number in the set.
$=95$ Simplify.

Answer: The average of lan's exam scores is 95 .

## CHECK Your Progress

(4) Kyle had test scores of $89,82,85,93$, and 96 . Find the mean (average) of his test scores.
A. 85
B. 89
C. 93
D. 96


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## 2:5 Dividing Integers

## CONCEPT SUMMARY

## Operations with Integers

## Adding Two Integers

To add integers with the same sign, add their absolute values. Give the result the same sign as the integers.
To add integers with different signs, subtract their absolute values. Give the result the same sign as the integer with the greater absolute value.

## Subtracting Two Integers

To subtract an integer, add its additive inverse.

## Examples

$$
\begin{array}{ll}
-5+(-4)=-9 & 5+4=9 \\
-5+4=-1 & 5+(-4)=1
\end{array}
$$

$$
5-9=5+(-9) \text { or }-4
$$

$$
5-(-9)=5+9 \text { or } 14
$$

## Multiplying Two Integers

The product of two integers with the same sign is positive.
The product of two integers with different signs is negative.

## Dividing Two Integers

The quotient of two integers with the same sign is positive.
The quotient of two integers with different signs is negative.

| $5 \cdot 4=20$ | $-5 \cdot(-4)=20$ |
| :--- | :--- |
| $-5 \cdot 4=-20$ | $5 \cdot(-4)=-20$ |
| $20 \div 5=4$ | $-20 \div(-5)=4$ |
| $-20 \div 5=-4$ | $20 \div(-5)=-4$ |

negative.


## Lesson Menu

Five-Minute Check (over Lesson 2-5)
Main Ideas and Vocabulary
Example 1: Write Ordered Pairs
Example 2: Graph Points and Name the Quadrant
Example 3: Graph an Algebraic Relationship

## Main Ideas

- Graph points on a coordinate plane.
- Graph algebraic relationships.


## New Vocabulary

- quadrants


## EXAMPLE Write Ordered Pairs

(1) A. Write the ordered pair that names the point $P$.

The $x$-coordinate is 4 .
The $y$-coordinate is -2 .


Answer: The ordered pair is $(4,-2)$.

## EXAMPLE Write Ordered Pairs

(1) B. Write the ordered pair that names the point Q.

The $x$-coordinate is -3 .
The $y$-coordinate is -1 .


Answer: The ordered pair is $(-3,-1)$.

## CHECK Your Progress

(1) A. Write the ordered pair that names the point $M$.
A. $(2,3)$
B. $(-3,-2)$
C. $(-2,-3)$
D. $(-3,2)$


## shly

(1) B. Write the ordered pair that names the point $N$.
(A. $(4,-1)$
B. $(4,1)$
C. $(1,-4)$
D. $(-1,4)$



## EXAMPL: Graph Points and Name the Quadrant

(2) A. Graph and label $S(-1,-5)$ on a coordinate plane. Name the quadrant in which the point lies.

Start at the origin.
Move 1 unit left.
Then move 5 units down and draw a dot.

Answer: Point $S$ is in
Quadrant III.
COncepts in MQtion


Interactive Lab:
The Coordinate System
Click here to view!

## EXAMPLE Graph Points and Name the Quadrant

(2) B. Graph and label $U(-2,3)$ on a coordinate plane. Name the quadrant in which the point lies.

Start at the origin.
Move 2 units left.
Then move 3 units up and draw a dot.

Answer: Point $U$ is in Quadrant II.


## EXAMPLE Graph Points and Name the Quadrant

(2) C. Graph and label $T(0,-3)$ on a coordinate plane. Name the quadrant in which the point lies.

Start at the origin.
Since the $x$-coordinate is 0 , the point lies on the $y$-axis.
Move 3 units down and draw a dot.

Answer: Point $T$ is not in any quadrant.


## CHECK Your Progress:

(2) A. Graph and label $A(3,-4)$ on a coordinate plane. Name the quadrant in which the point lies.
A. Quadrant I
B. Quadrant II
C. Quadrant III

D. Quadrant IV

## CHECK Your Progress

(2) B. Graph and label $B(-2,1)$ on a coordinate plane. Name the quadrant in which the point lies.
A. Quadrant I
B. Quadrant II
C. Quadrant III

D. Quadrant IV

## CHECK Your Progress

(2) C. Graph and label $C(-4,0)$ on a coordinate plane. Name the quadrant in which the point lies.
A. Quadrant I
B. Quadrant II
C. Quadrant III


(D.) not in any quadrant

## EXAMPLE Graph an Algebraic Relationship

(3) The difference between two integers is 4. If $x$ represents the first integer and $y$ represents the second integer, make a table of possible values for $x$ and $y$. Then graph the ordered pairs and describe the graph.

First, make a table. Choose values for $x$ and $y$ that have a difference of 4 .

| $x-y=4$ |  |  |
| :---: | :---: | :---: |
| $x$ | $y$ | $(x, y)$ |
| 2 | -2 | $(2,-2)$ |
| 1 | -3 | $(1,-3)$ |
| 0 | -4 | $(0,-4)$ |
| -1 | -5 | $(-1,-5)$ |
| -2 | -6 | $(-2,-6)$ |

## EXAMPIE Graph an Algebraic Relationship

(3) Then graph the ordered pairs on a coordinate plane.


| $x-y=4$ |  |  |
| :---: | :---: | :---: |
| $x$ | $y$ | $(x, y)$ |
| 2 | -2 | $(2,-2)$ |
| 1 | -3 | $(1,-3)$ |
| 0 | -4 | $(0,-4)$ |
| -1 | -5 | $(-1,-5)$ |
| -2 | -6 | $(-2,-6)$ |

## EXAMPIE Graph an Algebraic Relationship

(3) Answer: The points in the graph are on a line that slants upward to the right. The line crosses the $y$-axis at $y=-4$.

|  |  |  | ${ }^{4}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| -4-3-2-1 |  |  | 012 |  |  | 3 | $4 x$ |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  | -3 | - |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  | - 5 |  |  |  |  |  |
|  |  | - - 6 |  |  |  |  |  |


| $x-y=4$ |  |  |
| :---: | :---: | :---: |
| $x$ | $y$ | $(x, y)$ |
| 2 | -2 | $(2,-2)$ |
| 1 | -3 | $(1,-3)$ |
| 0 | -4 | $(0,-4)$ |
| -1 | -5 | $(-1,-5)$ |
| -2 | -6 | $(-2,-6)$ |

## 2-6 The Coordinate System

## CHECK Your Progress

(3) A. The sum of two integers is 3 . If $x$ represents the first integer and $y$ represents the second integer, make a table of possible values for $x$ and $y$.

A. | $x$ | $y$ |
| ---: | ---: |
| -3 | 3 |
| 0 | 3 |
| 2 | 3 |
| 3 | 3 |

(B.)

| $x$ | $y$ |
| ---: | ---: |
| -3 | 6 |
| 0 | 3 |
| 2 | 1 |
| 3 | 0 |

C. | $x$ | $y$ |
| ---: | ---: |
| -3 | 0 |
| 0 | -3 |
| 2 | -5 |
| 3 | -6 |

D.

| $x$ | $y$ |
| ---: | ---: |
| -3 | 0 |
| 0 | 3 |
| 2 | 5 |
| 3 | 6 |

## STCHECK Your Progress,

(3) B. The sum of two integers is 3 . If $x$ represents the first integer and $y$ represents the second integer, graph possible ordered pairs.
A.

B.


D.

$\square \mathrm{A} \square \mathrm{B} \square \mathrm{C} \square \mathrm{D}$

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## Chapter Resources Menu

## $8 /$ checkPoint Five-Minute Checks

Math Tools

## COncepts <br> in MQtion

$\mathrm{An}_{\mathrm{I}_{\mathrm{m}} \mathrm{mation}}$ Multiplying Integers Interactive $+\frac{+}{x} \div$ The Coordinate System
$\stackrel{\text { Brain }}{\text { POP }}$ Adding and Subtracting Integers

Lesson 2-1 (over Chapter 1)
Lesson 2-2 (over Lesson 2-1)
Lesson 2-3 (over Lesson 2-2)
Lesson 2-4 (over Lesson 2-3)
Lesson 2-5 (over Lesson 2-4)
Lesson 2-6 (over Lesson 2-5)

## Integers

## Image Bank

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2. Open a chapter presentation using a full installation of Microsoft ${ }^{\circledR}$ PowerPoint ${ }^{\circledR}$ in editing mode and scroll to the Image Bank slides.
3. Select an image, copy it, and paste it into your presentation.

Integers

## Image Bank



Integers

## Image Bank



$\mid \leftarrow \leftarrow \Rightarrow$
(1) Find the value of the expression $\frac{48}{4}-2 \cdot 3$.
A. 30
B. 24
C. 8
(D. 6

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に $\Leftarrow \rightarrow$
(2) Find the value of the expression $3(1+5)-4 \bullet 2$.
A. 5
B. 10

C. 25
D. 28
(3) Evaluate $5 b+2 c-1$ for $b=3$ and $c=5$.
(A.) 24
B. 39
C. 100
D. 124
(4) Evaluate $a(c-b)$ for $a=6, b=3$ and $c=5$.
A. 4
B. 8
C. 12
D. 27

$\stackrel{\mathrm{F}}{\mathrm{H}} \mathrm{H}$
(5) Find the next term in the list. 112, 99, 86, $73,60, \ldots$

## A. 40

B. 47

C. 50
D. 57

## Standardized Test Practice

(6) Which sentence does the equation $n-5=10$ represent?
A. A number is the difference between 10 and 5.
B. Five more than a number is 10 .
C. Five less than a number is 10 .
D. A number less than 5 is 10 .

## 0 Fivo-Minute CHECK (over Lesson 2-1)

(1) Which option shows an integer to represent \$8 withdrawn from a bank account, and its graph on a number line?
A. 8


C. -8

D. 8

(2) Use $<,>$, or $=$ in $-9 \ldots-8$ to make the sentence true.
(A.) $<$
B. >

0\%
C. =

(3) Order the integers $\{-2,4,-1,2,-8\}$ from least to greatest.
A. $\{4,2,-8,-2,-1\}$

0\%
B. $\{-1,-2,2,4,-8\}$
C. $\{4,2,-1,-2,-8\}$
D. $\{-8,-2,-1,2,4\}$
$\square \mathrm{A} \mathrm{\square B} \mathrm{\square C} \mathrm{\square D}$
$88 /$ CheckPoint
$1 \leftarrow \leftarrow \rightarrow$
(4) Evaluate -| 17 |.
A. 17
B. 0
C. -1
(D.) -17

$88 /$ CheckPoint
$\stackrel{\vdash}{ }$
(5) Evaluate $|-8|+|b|+a$ if $a=0$ and $b=12$.
(A. 20
B. 12

C. -4
D. -20

Five-Minute CHECK (over Lesson 2-1)

## Standardized Test Practice

(6) The low temperatures for five days in February are shown in the table. What is the order of these temperatures from greatest to least?
A. $0^{\circ},-\mathbf{2}^{\circ},-3^{\circ},-4^{\circ}, 5^{\circ}$
B. $5^{\circ}, \mathbf{0}^{\circ},-\mathbf{4}^{\circ},-\mathbf{3}^{\circ}, \mathbf{2}^{\circ}$
C. $-4^{\circ},-3^{\circ},-\mathbf{2}^{\circ}, 0^{\circ}, 5^{\circ}$
$\square \mathrm{A} \square \mathrm{B} \square \mathrm{C} \square \mathrm{D}$
(D.) $5^{\circ}, 0^{\circ},-2^{\circ},-3^{\circ},-4^{\circ}$
(1) Find the sum $-4+(-3)$.
A. 7
B. 1
C. -1
D. -7


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に $\Leftarrow$
(2) Find the sum $2+(-6)$.
A. -8
B. -4

C. 4
D. 8
(3) Find the sum $-14+20$.

$$
\text { A. }-34
$$

B. -6
(C.) 6
D. 34
(4) Find the sum $-1+4+(-12)$.
A. 17
B. 15
(C. -9
D. -17

$\stackrel{\vdash}{ } \leftarrow \rightarrow$
(5) Find the sum $10+8+(-8)$.
A. 26
(B.) 10

C. -10
D. -26
F) Fivo-Minute CHECK (over Lesson 2-2)

## Standardized Test Practice

(6) Holly recorded the difference between morning and evening temperatures each day last week in the table shown. Which day had the greatest change in temperature?
(A.) Sun.

| Day | Sun. | Mon. | Tues. | Wed. | Thurs. | Fri. | Sat. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Change | -6 | +5 | -4 | +3 | -4 | -1 | +4 |

B. Mon.
C. Fri.
D. Sat.
(1) Find the difference $9-(-1)$.
A. -10
B. -8
C. 8
D. 10


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に $\Leftarrow \rightarrow$
(2) Find the difference - $3-(-21)$.

$$
\text { A. } 63
$$

B. 24

0\%

C. 18
D. 7
(3) Find the difference -8-3.
(A.) -11
B. -5

0\%
C. 5
D. 11
(4) Find the difference 12-21.
A. -33
(B.) -9
C. 9
D. 33

$\stackrel{\mid}{ } \mathrm{F} \rightarrow$
(5) Evaluate $a-b$ if $a=-7$ and $b=9$.
(A.) -16
B. -2

0\%

C. 2
D. 16

Standardized Test Practice
(6) When a number is subtracted from 17 the result is 20. What is the number?
A. 3

0\%
B. 37
C. -3
$\square \mathrm{A} \square \mathrm{B} \square \mathrm{C} \square \mathrm{D}$
D. -37
(1) Find the product $-9 \bullet 8$.
(A.) -72
B. -63
C. -17
D. -1


トた
(2) Find the product $-3(-13)$.

$$
\text { A. }-39
$$

B. -16
C. 10
(D. 39
(3) Find the product $-5(-3)(4)$.

$$
\text { A. }-70
$$

B. -60
C. 60
D. 70
(4) Simplify $-2 \cdot(-3 y)$.

$$
\text { A. }-6 y
$$

(B.) $6 y$
C. $-5 y$
D. $y$

$\stackrel{\mid}{\mathrm{H}} \mathrm{H}$
(5) Evaluate $-7 a b$ for $a=-1$ and $b=4$.
A. -28
B. -11

C. 11
(D.) 28

Standardized Test Practice
(6) What is the next number is the pattern $-3,6,-12$, 24, ...?
A. 48
$0 \%$
(B.) -48
C. 36
D. -36
$\square \mathrm{A} \square \mathrm{B} \square \mathrm{C} \square \mathrm{D}$
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FHF

# QuAPTES Integers <br> F) Fivo-Minute CHECK (over Lesson 2-5) 

(1) Find the quotient $\frac{-45}{-5}$.
A. 40
(B. 9
C. -9
D. -50


トヶ
(2) Find the quotient $\frac{72}{-12}$.
A. 60
B. 6

0\%

(C. - -6
D. -84
(3) Find the quotient $\frac{-90}{6}$.
(A.) -15
B. -12

0\%
C. 12
D. 15
(4) Evaluate $\frac{a}{-8}$ if $a=-96$.
A. -88
B. -12
C. 12
D. 88

$\stackrel{\leftarrow}{\leftarrow}$

# Integers <br> Fenvo-Minute CHECK (over Lesson 2-5) 

(5) Evaluate $\frac{x}{y}$ if $x=-65$ and $y=-5$.
A. -13
B. -11

0\%

C. 11
D. 13

Standardized Test Practice
(6) What is the average (mean) of $-7,6,-11,9$, and -2 ?
(A.) $\mathbf{- 1}$
$0 \%$
B. 1
C. -5
D. 7

