Interactive Classroom



Chapter 3 Equations

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Equations

Chapter Menu

Lesson 3-1 The Distributive Property

- **Lesson 3-2** Simplifying Algebraic Expressions
- Lesson 3-3 Solving Equations by Adding or Subtracting
- Lesson 3-4 Solving Equations by Multiplying or Dividing
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- **Lesson 3-6** Writing Two-Step Equations
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Lesson Menu

Five-Minute Check (over Chapter 2)

Main Ideas and Vocabulary

Key Concept: Distributive Property

Example 1: Use the Distributive Property

Example 2: Real-World Example

Example 3: Simplify Algebraic Expressions

Example 4: Simplify Expressions with Subtraction

Main Ideas

- Use the Distributive Property to write equivalent numerical expressions.
- Use the Distributive Property to write equivalent algebraic expressions.

Chapter RESOURCES

New Vocabulary

equivalent expressions

KEY CONCEPT

Distributive Property

To multiply a number by a sum, multiply each number inside the Words parentheses by the number outside the parentheses.

5-

Symbols a(b+c) = ab + ac

(b+c)a = ba + ca

Examples $3(4+2) = 3 \cdot 4 + 3 \cdot 2$

$$(5+3)2 = 5 \cdot 2 + 3 \cdot$$

COncepts in MOtion

2

BrainPOP: Distributive Property

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EXAMPLE Use the Distributive Property

A. Use the Distributive Property to write 4(5 + 8) as an equivalent expression. Then evaluate the expression.

Chapter RESOURCES

$$4(5+8) = 4 \cdot 5 + 4 \cdot 8$$

= 20 + 32 Multiply.
= 52 Add.

Answer: 52



EXAMPLE Use the Distributive Property

B. Use the Distributive Property to write (6 + 9)2 as an equivalent expression. Then evaluate the expression.

> Chapter RESOURCES

$$(6 + 9)2 = 6 \cdot 2 + 9 \cdot 2$$

= 12 + 18 Multiply.
= 30 Add.

Answer: 30



- A. Use the Distributive Property to write 3(9 + 2) as an equivalent expression. Then evaluate the expression.
- 0% A. 3 9 + 3 2; 30
- 0% **B.** 3 9 + 3 2; 33
- 0% C. (3 + 9)(3 + 2); 60
- 0% D. (3 + 9)(3 + 2); 72





- B. Use the Distributive Property to write (7 + 3)5 as an equivalent expression. Then evaluate the expression.
- 0% A. (7 + 5)(3 + 5); 96
- **0% B.** (7 + 5)(3 + 5); 86
- 0% **C.** 7 5 + 3 5; 50
- 0% D. $7 \bullet 5 + 3 \bullet 5; 45$





The Distributive Property

Real-World EXAMPLE

RECREATION A canoe camping class costs \$80 per person, including the cost for canoe rental. The cost for food is an additional \$39 per person.

A. Write two equivalent expressions to find the total cost of one class for a family of four.

Method 1 Find the cost for 1 person, then multiply by 4.

4(\$80 + \$39) 4 times the cost for 1 person





Method 2 Find the cost of 4 classes and food for 4. Then add.

cost of four classes + cost of food for 4





Real-World EXAMPLE

B. Evaluate either expression to find the total cost.

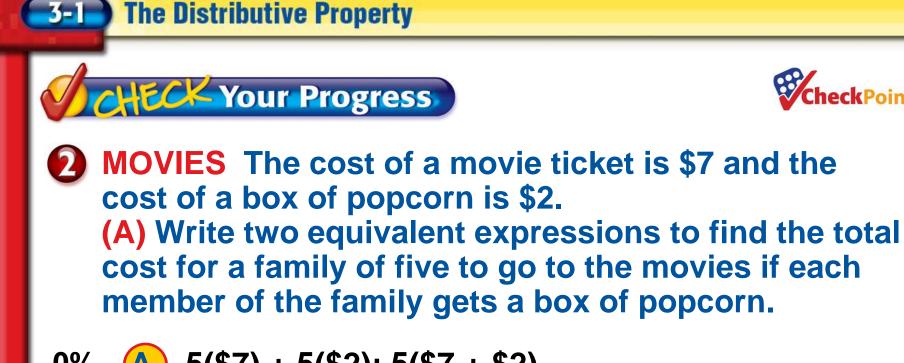
4(\$80 + \$39) = 4(\$80) + 4(\$39) Distributive Property

= \$320 + \$156 Multiply.

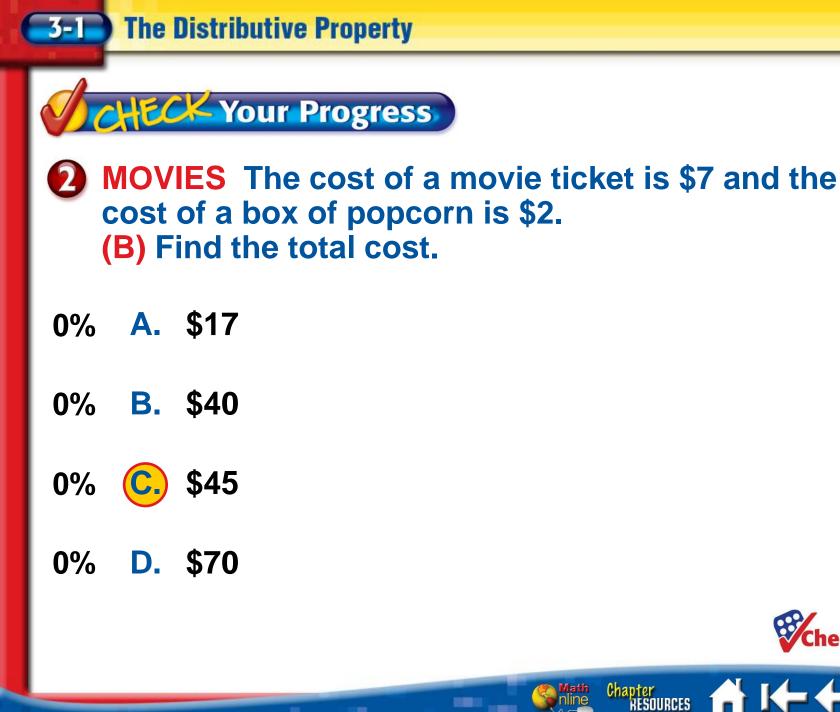
Chapter RESOURCES

= \$476 Add.

Answer: The total cost is \$476. You can check your results by evaluating 4(\$119).



- 0% A. 5(\$7) + 5(\$2); 5(\$7 + \$2)
- 0% **B.** 5(\$7) + 5(\$2); 5(\$7 \$2)
- 0% **C.** \$7 + 5(\$2); \$7 + \$10
- 0% D. \$7 + 5(\$2); 5(\$7 + \$2)







A. Use the Distributive Property to write 2(x + 4) as an equivalent algebraic expression.

$$2(x+4) = 2x+2 \bullet 4$$

$$= 2x + 8$$
 Simplify.

Chapter RESOURCES

Answer: 2x + 8



B. Use the Distributive Property to write (*y* + 3)6 as an equivalent algebraic expression.

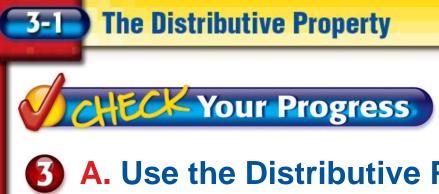
$$(y+3)6 = y \bullet 6 + 3 \bullet 6$$

= 6y + 18 Simplify.

Answer: 6*y* + 18





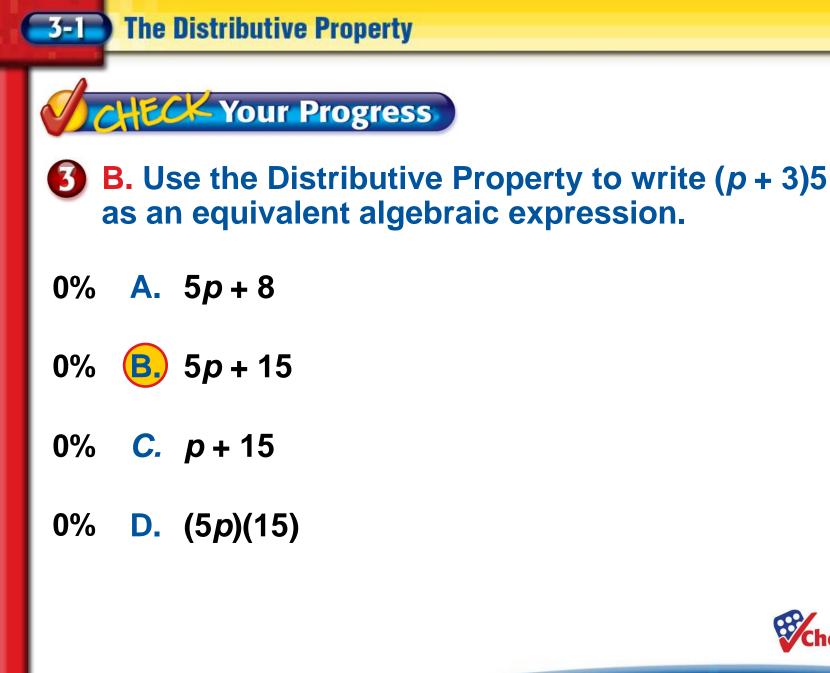


A. Use the Distributive Property to write 4(m + 7) as an equivalent algebraic expression.

0% **A**. *m* + 28

- 0% **B.** 4*m* + 11
- 0% C. (4*m*)(28)
- 0% **D**, 4*m* + 28









EXAMPLE Simplify Expressions with Subtraction

A. Use the Distributive Property to write 4(x - 2) as an equivalent algebraic expression.

$$4(x-2) = 4[x + (-2)]$$

$$=$$
 4*x* + **4**(-2)

= 4x + (-8)

Rewrite x - 2 as x + (-2).

Distributive Property

Simplify.

=4x - 8

Definition of subtraction

Chapter RESOURCES

Answer: 4x - 8



EXAMPLE Simplify Expressions with Subtraction

B. Use the Distributive Property to write –2(n – 3) as an equivalent algebraic expression.

-2(n-3) = -2[n + (-3)]

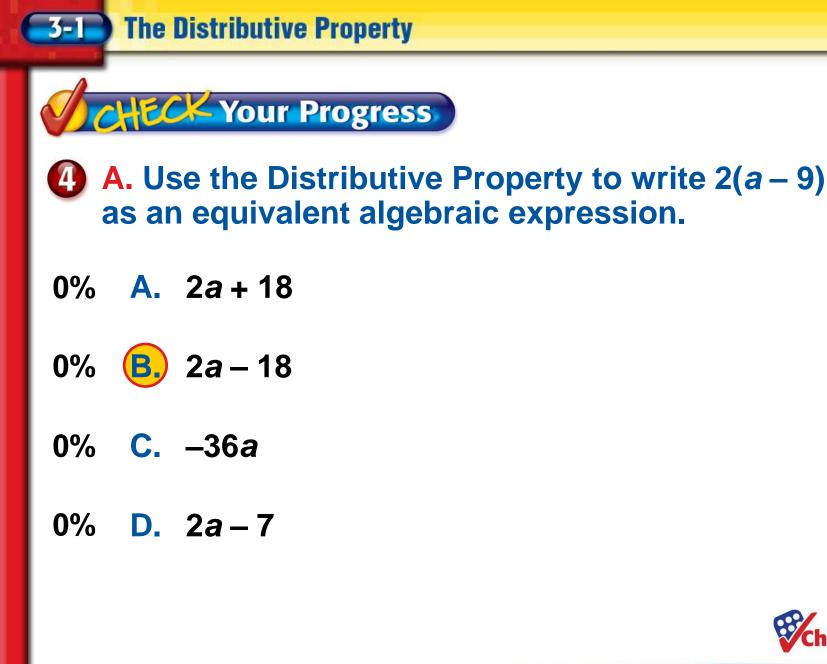
Rewrite n - 3 as n + (-3).

Distributive Property

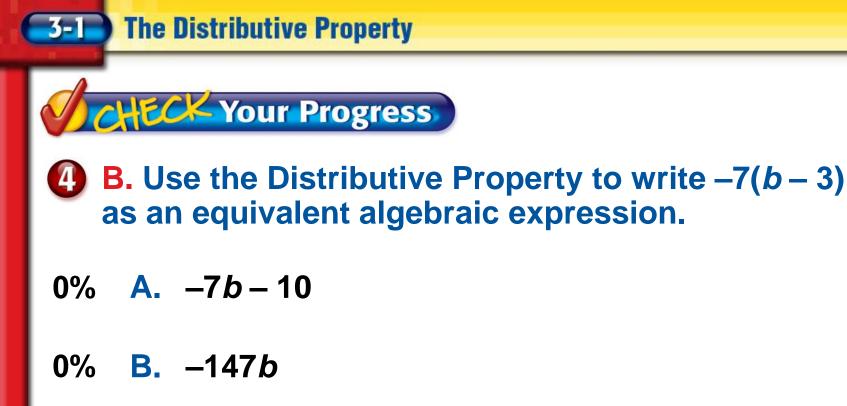
Chapter RESOURCES

= -2n + 6 Simplify.

Answer: -2n + 6









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Lesson Menu

Five-Minute Check (over Lesson 3-1)

Main Idea and Vocabulary

Example 1: Identify Parts of Expressions

Example 2: Simplify Algebraic Expressions

Example 3: Real-World Example



Main Idea

Use the Distributive Property to simplify algebraic expressions.

Chapter RESOURCES

New Vocabulary

- term
- coefficient
- like terms
- constant
- simplest form
- simplifying an expression

EXAMPLE Identify Parts of Expressions

Identify the terms, like terms, coefficients, and constants in the expression 4x - x + 2y - 3.

$$4x - x + 2y - 3 = 4x + (-x) + 2y + (-3)$$
 Definition of
subtraction

$$= 4x + (-1x) + 2y + (-3)$$
 Identity
Property

Chapter RESOURCES

Answer: The terms are 4x, -x, 2y, and -3. The like terms are 4x and -x. The coefficients are 4, -1, and 2. The constant is -3.

CHECK Your Progress

- Identify the terms, like terms, coefficients, and constants in the expression 5x + 3y 2y + 6.
- 0% A. terms: 5*x*, 3*y*, –2*y*; like terms: 3*y*, –2*y*; coefficients: 5, 3, –2; constant: 6
 - B. terms: 5x, 3y, -2y, 6; like terms: none; coefficients: 5,3,-2; constant: 6

0%

0%

- terms: 5x, 3y, -2y, 6; like terms: 3y, -2y; coefficients: 5, 3, -2; constant: 6
- 0%
- D. terms: 5x, 3y, -2y; like terms: 5x, 3y, -2y; coefficients: 5, 3, -2, 6; constant: none



2 A. Simplify 8*n* + 4 + 4*n*.

8*n* and 4*n* are like terms.

8n + 4 + 4n = 8n + 4n + 4

$$= (8 + 4)n + 4$$

= 12*n* + 4

- **Commutative Property**
- **Distributive Property**

Chapter RESOURCES

Simplify.

Answer: 12*n* + 4

B. Simplify 6x + 4 - 5x - 7.

6x and -5x are like terms. 4 and -7 are also like terms. 6x + 4 - 5x - 7 = 6x + 4 + (-5x) + (-7) Definition of subtraction

$$= 6x + (-5x) + 4 + (-7)$$

= [6 + (-5)]x + 4 + (-7)

= x - 3

- Commutative Property
- Distributive Property

Simplify.

Chapter RESOURCES

Answer: x - 3

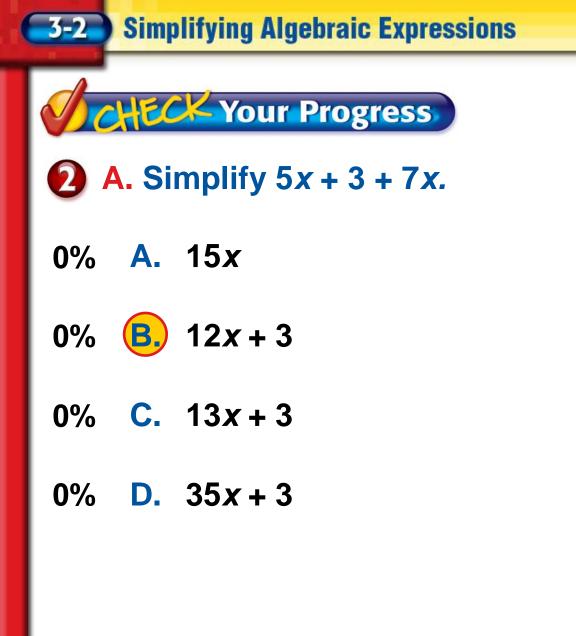
2 C. Simplify -y + 2(x + 3y).

- -y + 2(x + 3y) = -y + 2x + 2(3y) Distributive Property
 - = -y + 2x + 6y Associative Property
 - = -1y + 6y + 2x Commutative Property
 - = (-1 + 6)y + 2x Distributive Property

Chapter RESOURCES

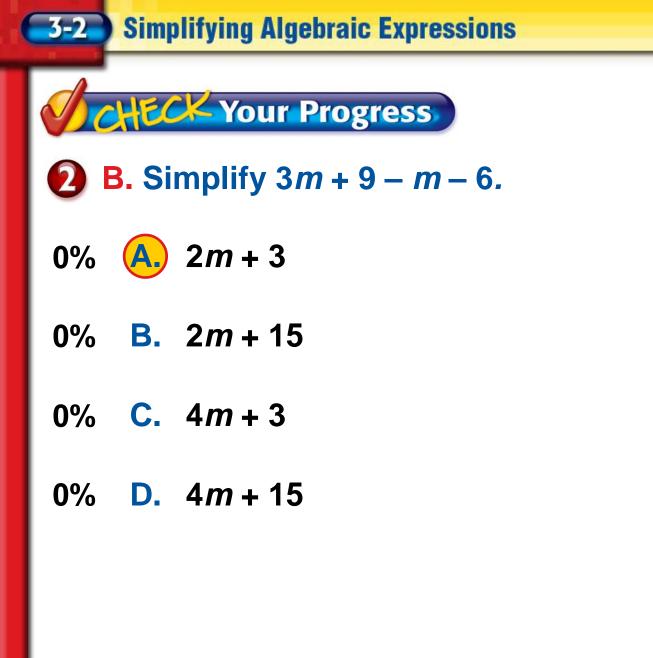
= 5y + 2x Simplify.

Answer: 5y + 2x



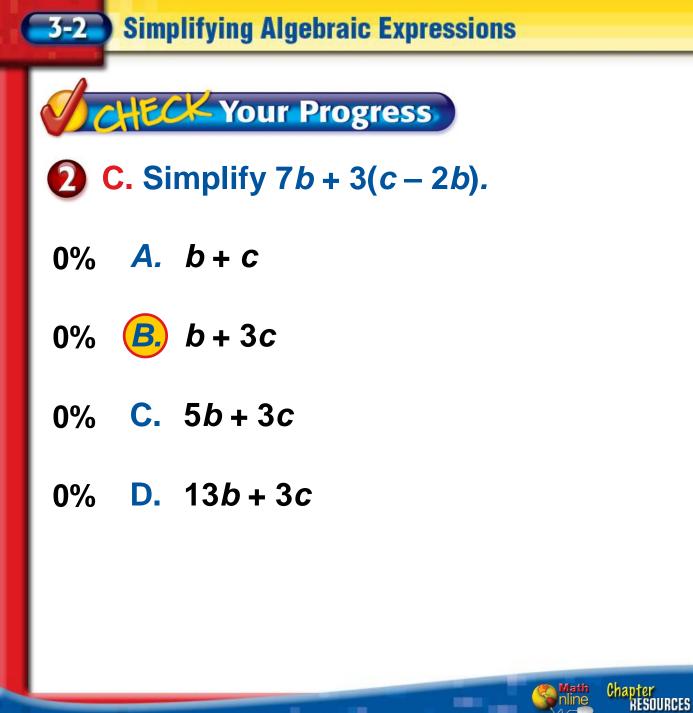


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Real-World EXAMPLE

3 WORK You and a friend worked in the school store last week. You worked 4 hours more than your friend. Write an expression in simplest form that represents the total number of hours you both worked.

- Words number of hours your friend worked + number of hours you worked
- Variables Let h = number of hours your friend worked. Let h + 4 = number of hours you worked.

Chapter RESOURCES

Expression h + h + 4



Real-World EXAMPLE

$$\mathbf{3} \quad h + (h + 4) = (h + h) + 4$$

- = (1h + 1h) + 4
- = (1 + 1)h + 4

- Associative Property
- Identity Property
- Distributive Property

Chapter RESOURCES

= 2h + 4 Simplify.

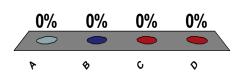
Answer: The expression 2h + 4 represents the total number of hours worked, where *h* is the number of hours your friend worked.



- Your friend borrowed three more books than you did. Write an expression in simplest form that represents the total number of books you both borrowed.
 - A. 4b
 B. b+3



D. 2b + 3b





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Lesson Menu

Five-Minute Check (over Lesson 3-2)

Main Ideas and Vocabulary

Key Concept: Subtraction Property of Equality

Example 1: Solve Equations by Subtracting

Key Concept: Addition Property of Equality

Example 2: Solve Equations by Adding

Example 3: Standardized Test Example: Solve Equations by Adding

> Chapter RESOURCES

Example 4: Real-World Example

Main Ideas

- Solve equations by using the Subtraction Property of Equality.
- Solve equations by using the Addition Property of Equality.

Chapter RESOURCES

New Vocabulary

- inverse operation
- equivalent equations



KEY CO	NCEPT	Subtraction Property of Equality	
Words	If you subtract the same number from each side of an equation, the two sides remain equal.		
Symbols	For any numbers a, b, and c, if $a = b$, then $a - c = b - c$.		
Examples	5 = 5 5 - 3 = 5 - 3 2 = 2	x + 2 = 3 x + 2 - 2 = 3 - 2 x = 1	

Math Chapter RESOURCES

EXAMPLE Solve Equations by Subtracting

Solve x + 4 = -3. Check your solution and graph it on a number line.

$$x + 4 = -3$$
 Write the equa

$$x + 0 = -7$$

$$x = -7$$

ation.

x + 4 - 4 = -3 - 4 Subtract 4 from each side.

$$4 - 4 = 0, -3 - 4 = -7$$

Identity Property; x + 0 = x



EXAMPLE Solve Equations by Subtracting

To check your solution, replace x with –7 in the original equation.

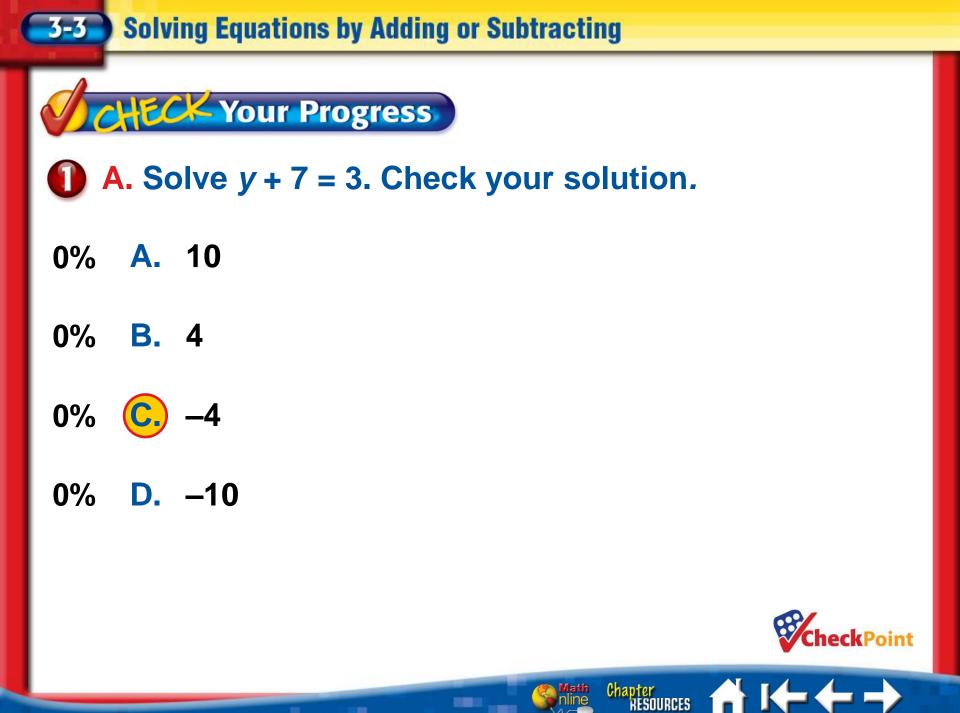
Check x + 4 = -3 Write the equation.

$$-7 + 4 \stackrel{?}{=} -3$$
 Check to see whether this sentence is true.

-3 = -3 The sentence is true.

Chapter RESOURCES

Answer: The solution is –7. To graph, draw a dot at –7 on a number line.



KEY CC	NCEPT	Addition Property of Equality	
Word	If you add the same number to each side of an equation, the two sides remain equal.		
Symbols	For any numbers a, b, and c, if $a = b$, then $a + c = b + c$.		
Examples	6 = 6 6 + 3 = 6 + 3 9 = 9	$ \begin{array}{l} x - 2 = 5 \\ x - 2 + 2 = 5 + 2 \\ x = 7 \end{array} $	

hine chapter RESOURCES

EXAMPLE Solve Equations by Adding

2 Solve y - 3 = -14.

$$y-3 = -14$$

 $y + (-3) = -14$
 $y + (-3) + 3 = 14 + 3$
 $y + 0 = -14 + 3$

Write the equation.

Rewrite y - 3 as y + (-3).

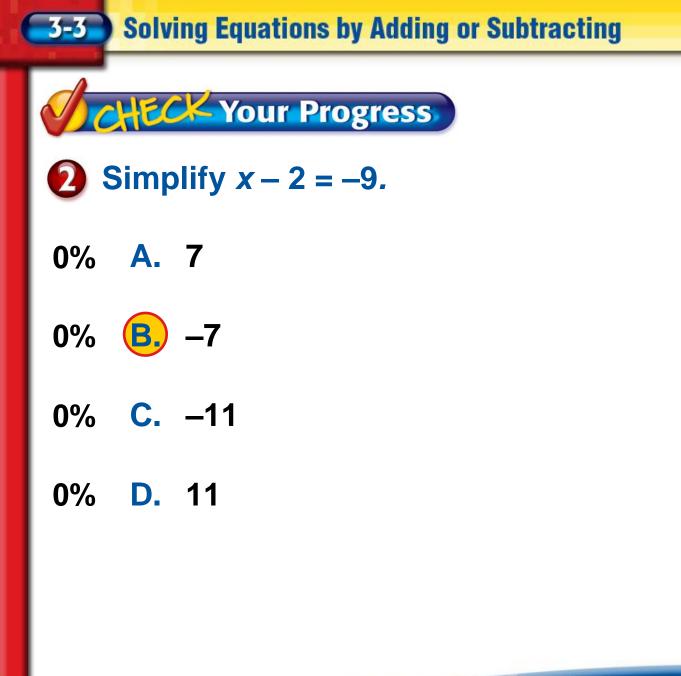
Add 3 to each side.

Additive Inverse Property; (-3) + 3 = 0

> Chapter RESOURCES

y = -11 Identity Property; y + 0 = y

Answer: The solution is –11. Check your solution.





←→



ENTERTAINMENT Movie A earned \$225 million at the box office. That is \$38 million less than Movie B earned. Which equation can be used to find the amount of money Movie B earned?

- **B.** 38 *B* = 225
- **C.** B = 225 38

D. B - 38 = 225

Read the test item.

Translate the verbal sentence into an equation.

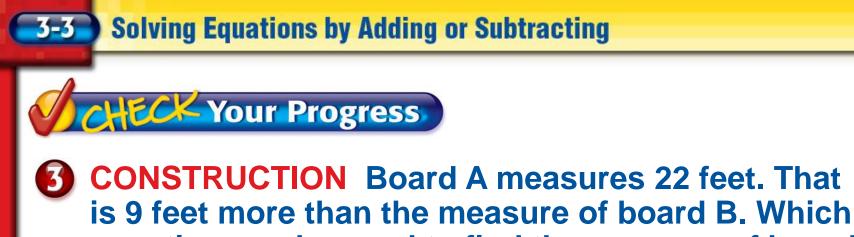
Solve the test item.



Standardized Test EXAMPLE

Multiple-Choice Test Item

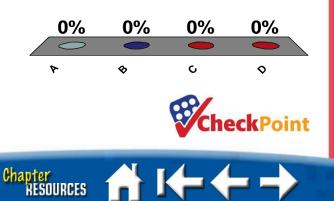
- Words Movie A earned \$38 million less than Movie B earned.
 - **Variables** Let *B* = amount Movie B earned.
 - **Equation** 225 = B 38
 - Answer: So the equation 225 = B 38 or B 38 = 225can be used to find the amount Movie B earned. This is choice D.



equation can be used to find the measure of board B?

A.
$$B + 9 = 22$$

- **B.** B 9 = 22
- **C.** 9 B = 22
- **D**. *B* = 22 + 9





Real-World EXAMPLE

MOUNTAINS Write and solve an equation to find the height of Guadalupe Peak, the highest point in Texas. Driskill Mountain, with a height of 535 feet, is the highest point in the neighboring state of Louisiana. It is 8214 feet lower than Guadalupe Peak.

Let h = the height of Guadalupe Peak.

535 = h - 8214 Write the equation.

Chapter RESOURCES

535 + 8214 = h - 8214 + 8214 Add 8214 to each side.

8749 = h Simplify.

Answer: Guadalupe Peak is 8749 feet high.



CHECK Your Progress

- BUILDINGS Write and solve an equation to find the expected height of the Freedom Tower, which is being built at the World Trade Center site in New York City. The Sears Tower in Chicago, 1450 feet tall, is 326 feet lower than the expected height of the Freedom Tower.
- 0% A. 1450 = h + 326; 1124 feet
- **0% B.** *h* = 1450 326; 1124 feet
- 0% (C) 1450 = h 326; 1776 feet
- 0% **D**. 1450 h = 326; 1776 feet



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Lesson Menu

Five-Minute Check (over Lesson 3-3)

Main Ideas

Key Concepts: Division Property of Equality

Example 1: Solve Equations by Dividing

Example 2: Real-World Example

Key Concepts: Multiplication Property of Equality

Example 3: Solve Equations by Multiplying



Main Ideas

- Solve equations by using the Division Property of Equality.
- Solve equations by using the Multiplication Property of Equality.

3-4

KEY CO	NCEPT	Division Property of Equality	
Words	When you divide each side of an equation by the same nonzero number, the two sides remain equal.		
Symbols	For any numbers a, b, and c, where $c \neq 0$, then $\frac{a}{c} = \frac{b}{c}$.		
Examples	$14 = 14$ $\frac{14}{7} = \frac{14}{7}$ $2 = 2$	3x = -12 $\frac{3x}{3} = \frac{-12}{3}$ x = -4	



Solving Equations by Multiplying or Dividing

EXAMPLE Solve Equations by Dividing

Solve 7x = -56. Check your solution and graph it on a number line.

$$7x = -56$$

$$\frac{7(x)}{7} = \frac{-56}{7}$$

$$1x = -8$$

$$x = -8$$

Write the equation.

Divide each side by 7 to undo the multiplication in $7 \bullet x$.

$$\frac{7}{7} = 1, \ \frac{-56}{7} = -8$$

Identity Property; 1x = x

Chapter

RESOURCES

Solving Equations by Multiplying or Dividing

EXAMPLE Solve Equations by Dividing

To check your solution, replace x with –8 in the original equation.

Check 7x = -56

Write the equation.

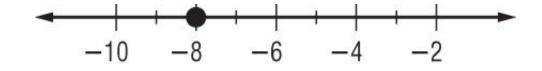
Check to see whether this statement is true.

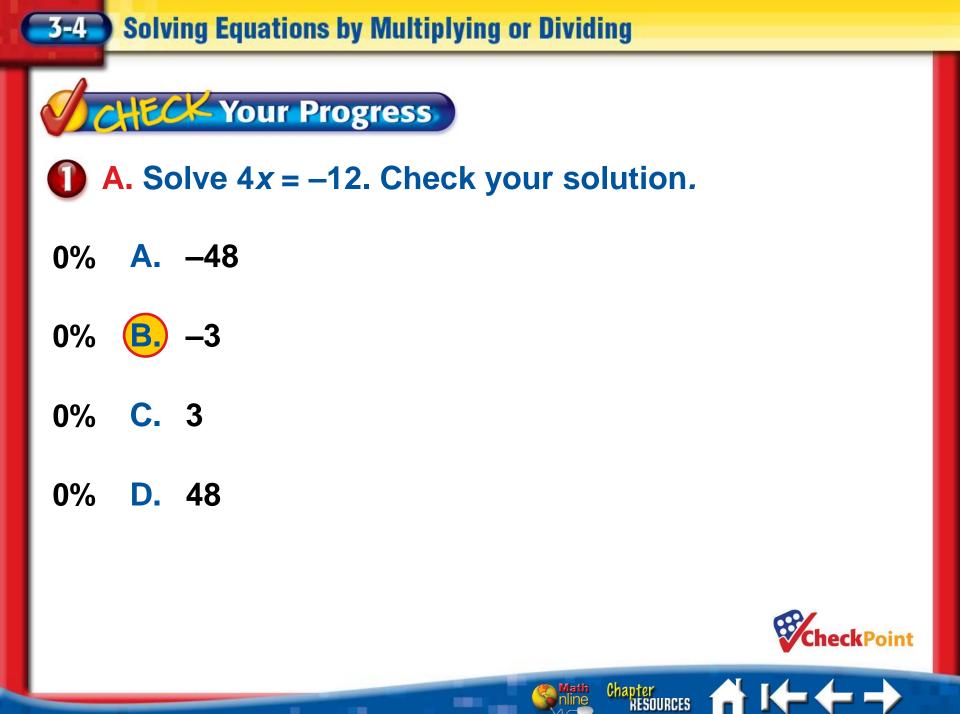
$$-56 = -56$$

The statement is true.

Chapter RESOURCES

Answer: The solution is –8.





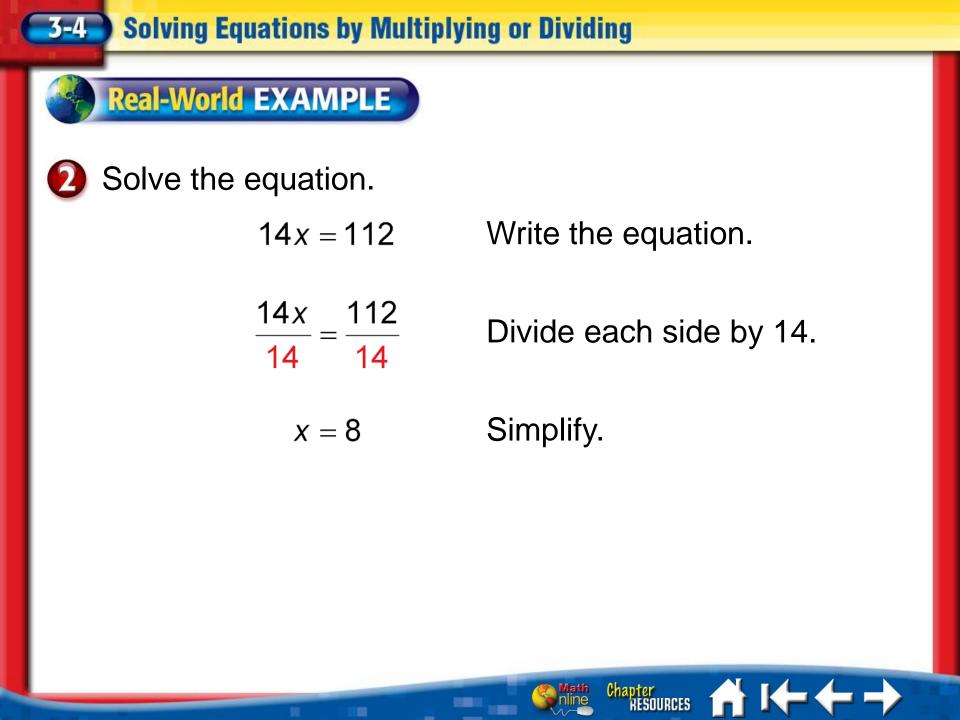


Real-World EXAMPLE

- HOBBIES Esteban spent \$112 on boxes of baseball cards. If he paid \$14 per box, how many boxes of cards did Esteban buy?
 - Words \$14 times the total number of boxes equals the total.
 - Variables Let *x* represent the number of boxes.

Chapter RESOURCES

Equation $$14 \cdot x = 112





Real-World EXAMPLE

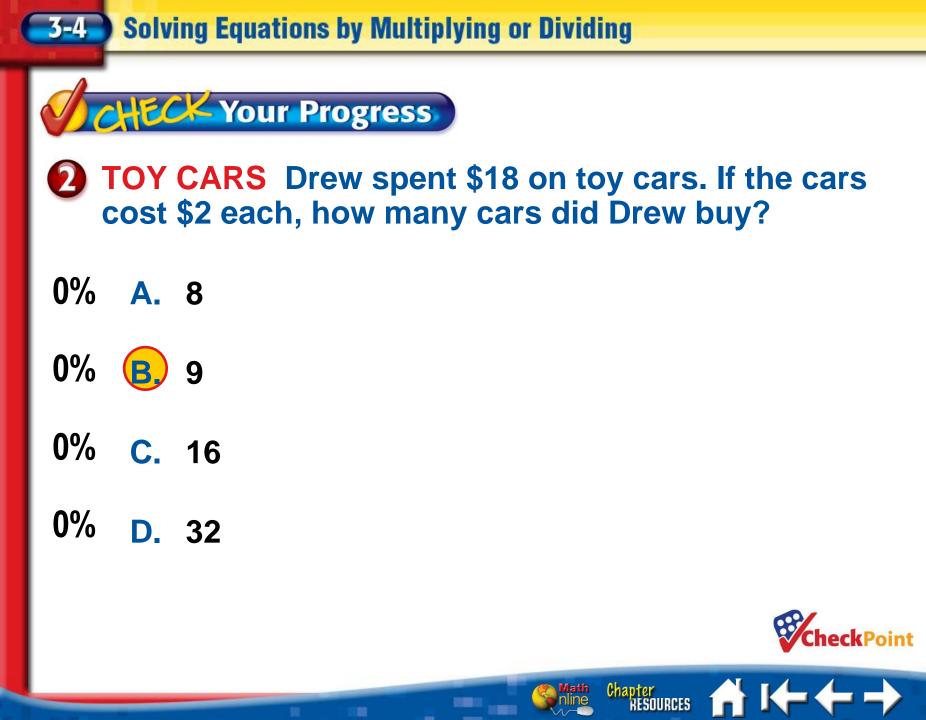
2 To check your solution, replace x with 8 in the original equation.

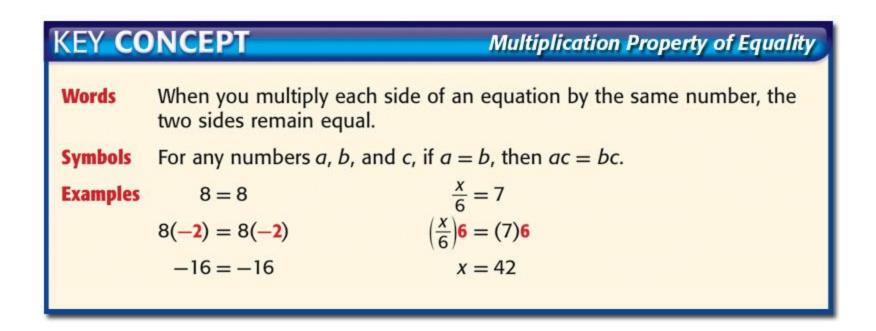
- Check14x = 112Write the equation. $14(8) \stackrel{?}{=} 112$ Check to see whether this
 - 112 = 112 The statement is true.

statement is true.

Answer: Therefore, Esteban bought 8 boxes of cards.









Multiplication and Division

Click here to view!



Solving Equations by Multiplying or Dividing

EXAMPLE Solve Equations by Multiplying

Solve $\frac{y}{-5} = -12$. Check your solution and graph it on a number line.

$$\frac{y}{-5} = -12$$

Write the equation.

$$\frac{y}{-5}(-5) = -12(-5)$$

Multiply each side by -5 to undo the division in $\frac{y}{-5}$.

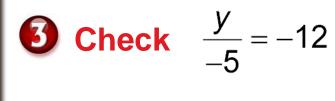
> Chapter RESOURCES

y = 60

Simplify.

Solving Equations by Multiplying or Dividing

EXAMPLE Solve Equations by Multiplying



Write the equation.

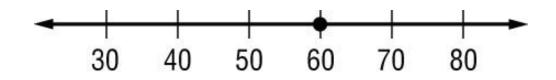
Chapter RESOURCES

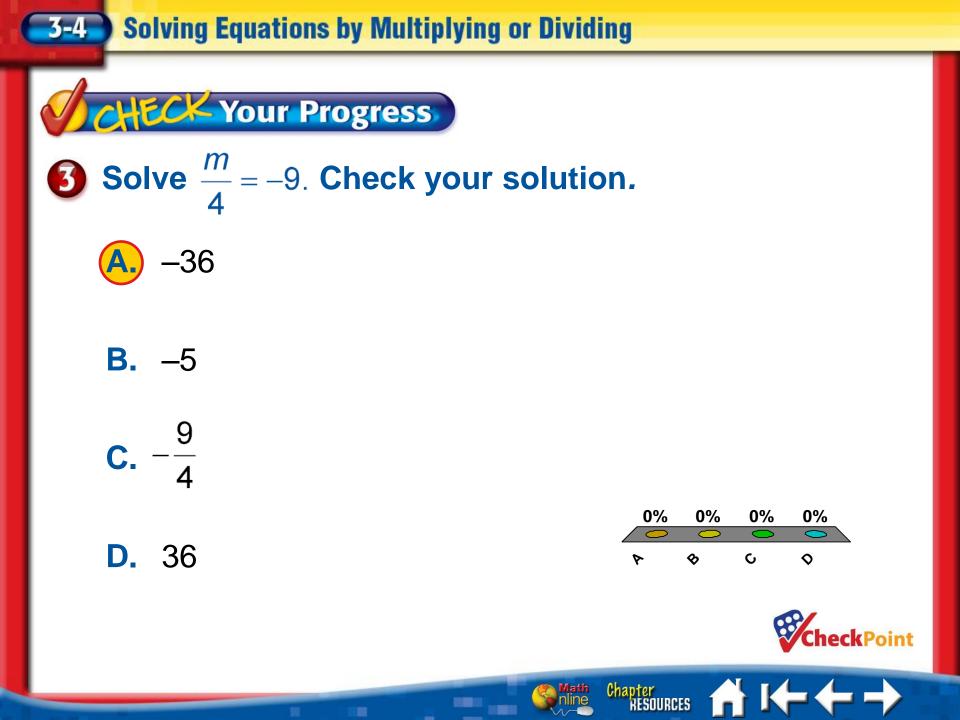
 $\frac{60}{-5} \stackrel{?}{=} -12$

Check to see whether this statement is true.

-12 = -12 The statement is true.

Answer: The solution is 60. To graph it, draw a dot at 60 on a number line.





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Lesson Menu

Five-Minute Check (over Lesson 3-4)

Main Idea and Vocabulary

Example 1: Solve Two-Step Equations

Example 2: Real-World Example

Example 3: Equations with Negative Coefficients

Example 4: Combine Like Terms Before Solving



Main Idea

• Solve two-step equations.

Chapter RESOURCES

New Vocabulary

two-step equation



EXAMPLE Solve Two-Step Equations

() A. Solve 3x - 4 = 17. Check your solution.

- 3x 4 = 17 Write the equation.
- 3x 4 + 4 = 17 + 4
- Undo subtraction. Add 4 to each side.

3*x* = 21

 $\frac{3x}{3} = \frac{21x}{3}$

x = 7

Simplify.

Undo multiplication. Divide each side by 3.

Simplify.



Solving Two-Step Equations

EXAMPLE Solve Two-Step Equations

Check 3x - 4 = 17 Write the equation.

Check to see whether this sentence is true.

Chapter RESOURCES

17 = 17 The sentence is true.

Answer: The solution is 7.

Solving Two-Step Equations

EXAMPLE Solve Two-Step Equations

B. Solve $3 = \frac{n}{3} + 8$. Check your solution.

 $3 = \frac{n}{3} + 8$ Write the equation.

$$3-8=\frac{n}{3}+8-8$$

Undo addition. Subtract 8 from each side.

Chapter RESOURCES

$$-5 = \frac{n}{3}$$

Simplify.



Solving Two-Step Equations

EXAMPLE Solve Two-Step Equations

$$\bigcirc 3(-5) = 3\left(\frac{n}{3}\right)$$

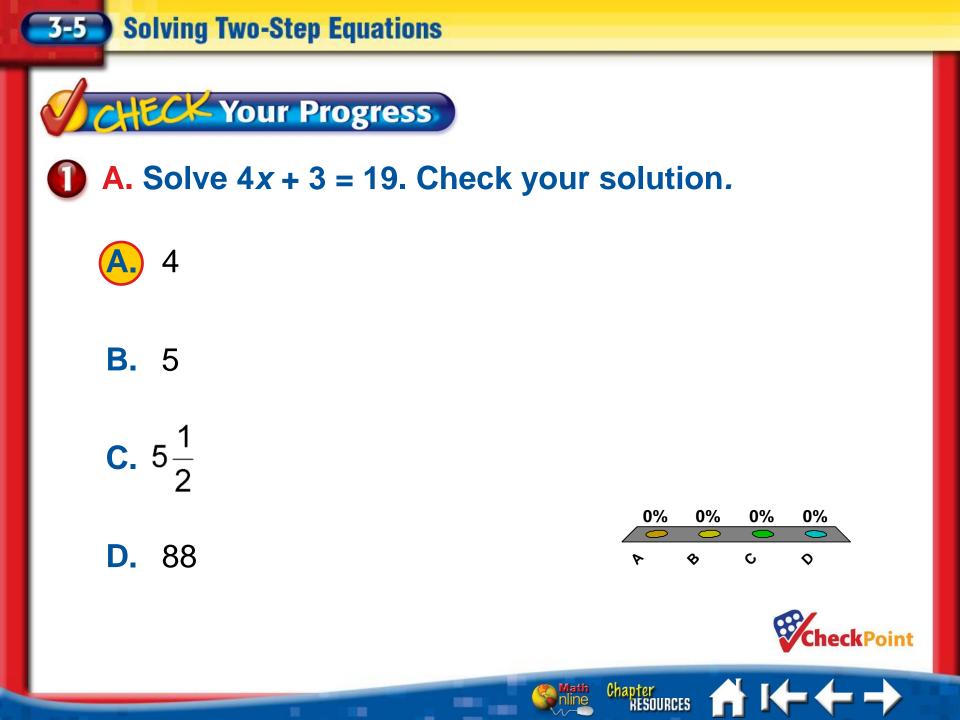
Undo division. Multiply each side by 3.

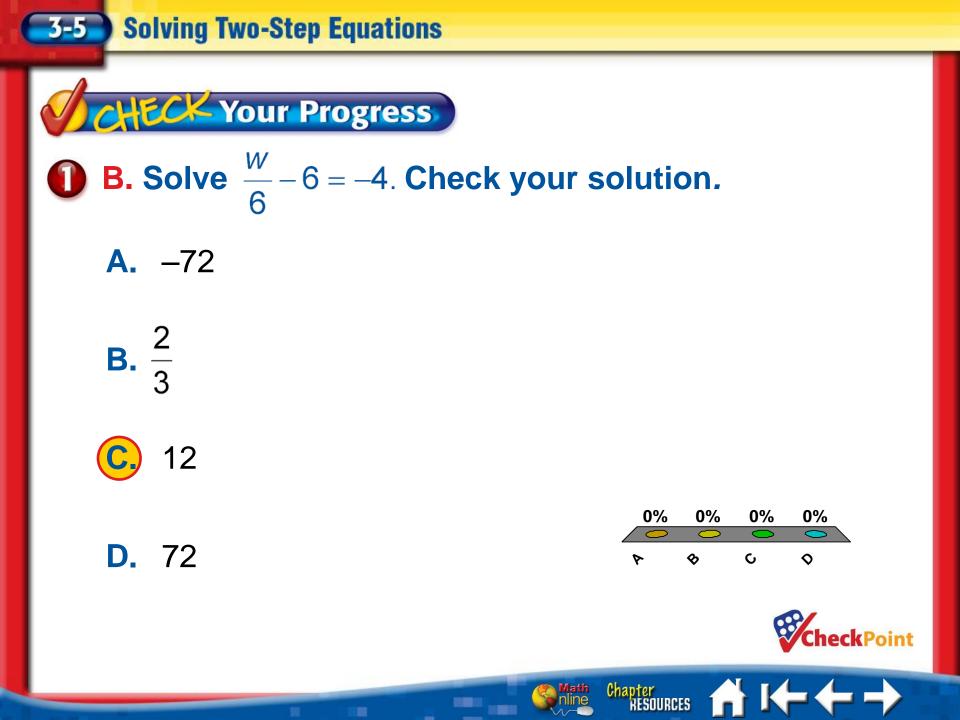
-15 = n Simplify.

Answer: The solution is –15. Check your solution.











Solving Two-Step Equations

Real-World EXAMPLE

MEASUREMENT The formula F = 1.8C + 32 can be used to convert Fahrenheit degrees to Celsius degrees. Solve the equation to find the equivalent Celsius temperature for 59°F.

59 = 1.8C + 32 Write the equation.

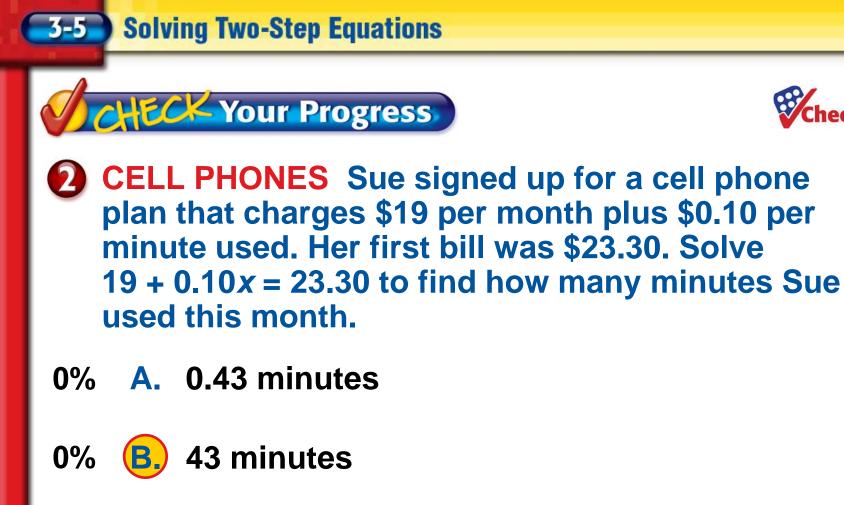
59 - 32 = 1.8C + 32 - 32 Subtract 32 from each side.

- 27 = 1.8C Simplify.
- $\frac{27}{1.8} = \frac{1.8C}{1.8}$ Divide each side by 1.8.

Chapter RESOURCES

15 = C Simplify.

Answer: The solution is 15. Therefore, 15° Celsius is equivalent to 59° Fahrenheit.



- 0% **C.** 53 minutes
- 0% **D.** 423 minutes

Equations with Negative Coefficients

3 Solve 5 - x = 7.

EXAMPLE

5 – <i>x</i> = 7
5 - 1x = 7
5 + (-1x) = 7
-5 + 5 + (-1x) = -5 + 7
-1x = 2
$-1x _2$
_1 _1

Write the equation. Identity Property; x = 1xDefinition of subtraction Add -5 to each side. Simplify.

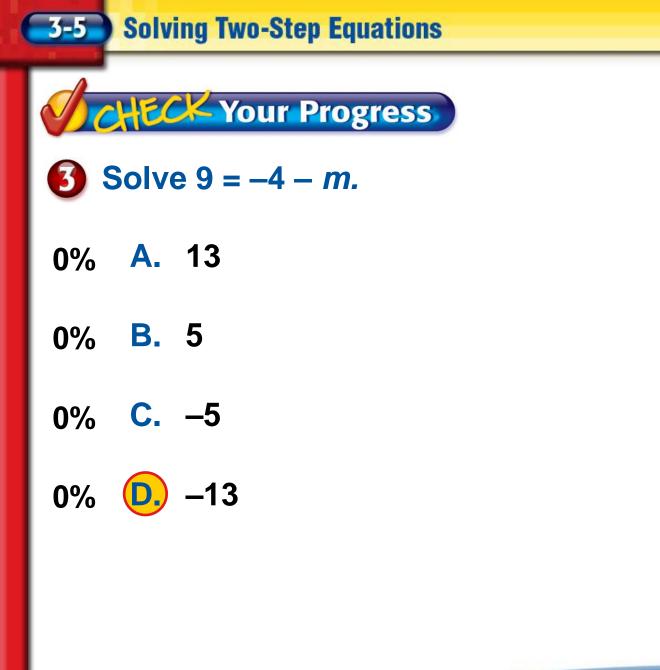
Divide each side by -1.

Chapter RESOURCES

Check your solution.

Answer: The solution is –2.

x = -2





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EXAMPLE Combine Like Terms Before Solving

4 Solve b - 3b + 8 = 18.

- b 3b + 8 = 18
- 1b 3b + 8 = 18

−2*b* + 8 = 18

- Write the equation.
 - Identity Property; b = 1b
- Combine like terms, 1*b* and –3*b*.
- -2b + 8 8 = 18 82b = 10 $\frac{-2b}{-2} = \frac{10}{-2}$ b = -5

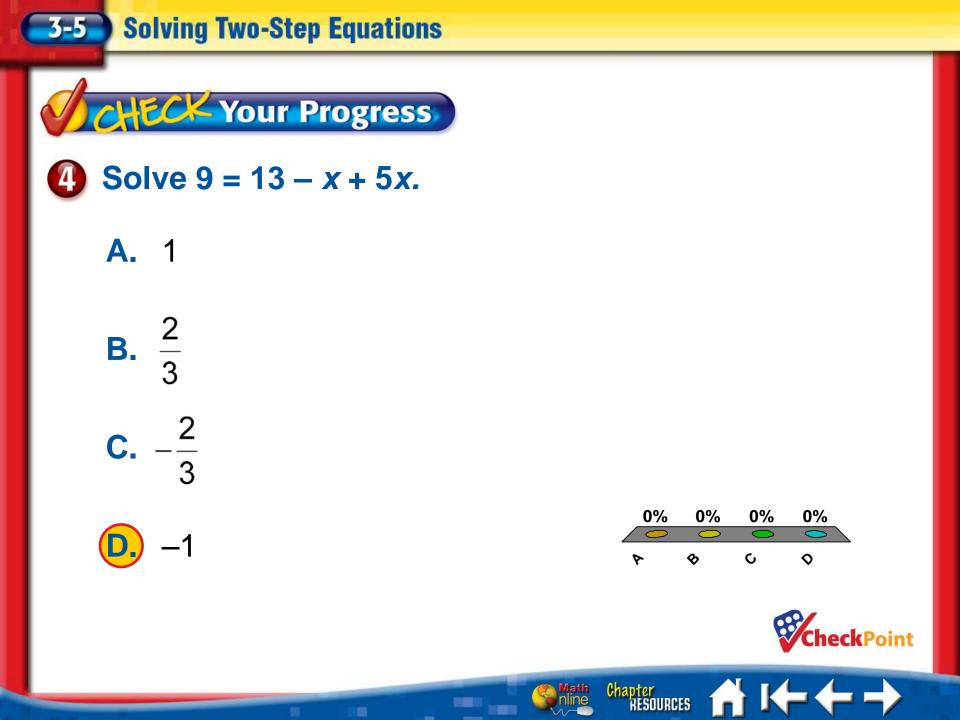
Subtract 8 from each side. Simplify.

Divide each side by -2.

Chapter RESOURCES

Simplify.

Answer: The solution is –5.



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Lesson Menu

5-6

Five-Minute Check (over Lesson 3-5)

Main Ideas

Example 1: Translate Sentences into Equations

Example 2: Translate and Solve an Equation

Example 3: Real-World Example

Example 4: Real-World Example



Main Ideas

5-6

- Write verbal sentences as two-step equations.
- Solve verbal problems by writing and solving two-step equations.



EXAMPLE Translate Sentences into Equations

A. Translate this sentence into an equation.

Twice a number, increased by 5, equals –25.

Answer: The equation is 2n + 5 = -25.







EXAMPLE Translate Sentences into Equations

B. Translate this sentence into an equation.

Four times a number, minus 8, equals 28.

Answer: The equation is 4n - 8 = 28.







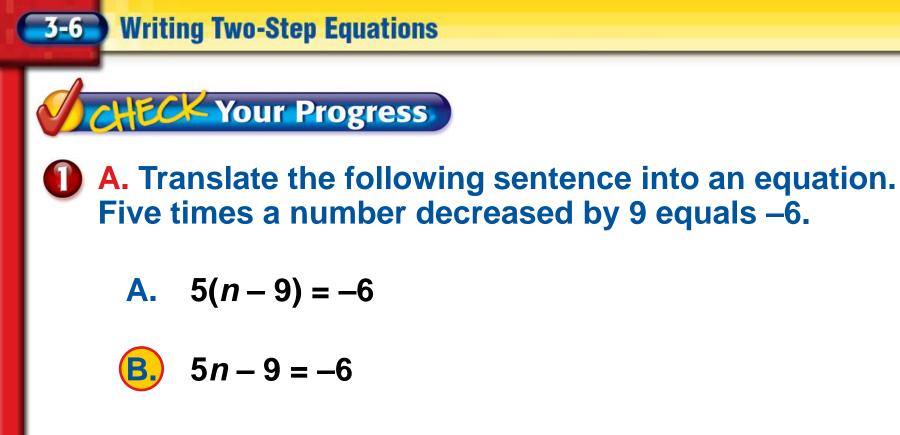
EXAMPLE Translate Sentences into Equations

C. Translate this sentence into an equation.

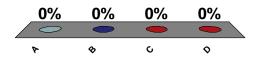
When five is added to the product of a number and 8, the result is 12.

Chapter RESOURCES

Answer: The equation is 5 + 8n = 12.



- **C.** 5n + 9 = -6
- **D.** n(5-9) = -6





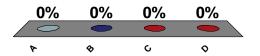


B. Translate the following sentence into an equation. Three times a number increased by 7 equals 18.

A.
$$3n - 7 = 18$$

B.
$$n(3+7) = 18$$

D.
$$3(n+7) = 18$$



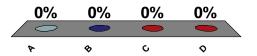




C. Translate the following sentence into an equation. When seven is subtracted from the product of 2 and a number, the result is 10.

$$2n - 7 = 10$$

- **B.** 7 2n = 10
- **C.** 2(n-7) = 10
- **D.** n(2-7) = 10







1-0

EXAMPLE Translate and Solve an Equation

Nine more than four times a number is 41. Find the number.

9 + 4n = 41 Write the equation.

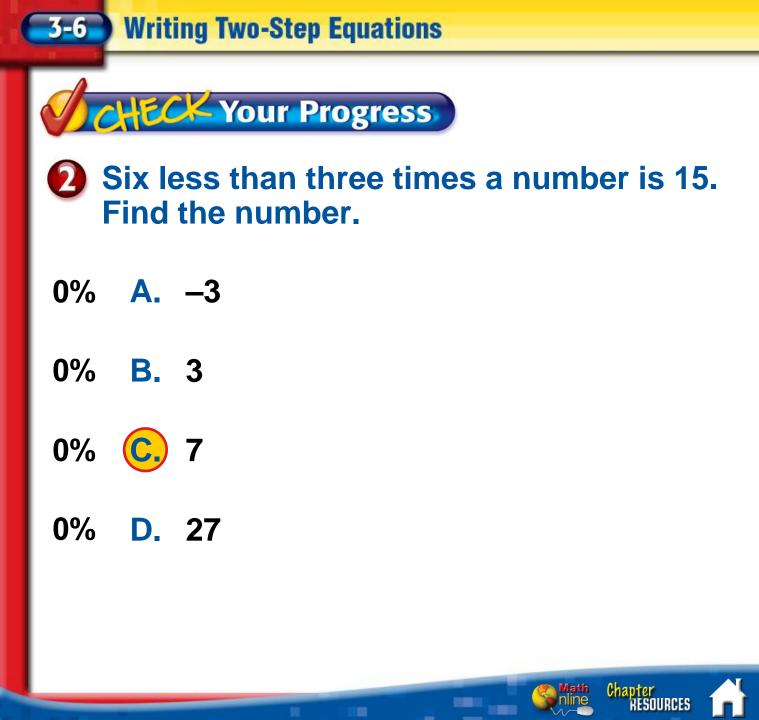
9 - 9 + 4n = 41 - 9 Subtract 9 from each side.

4n = 32 Simplify.

n = 8 Mentally divide each side by 4.

Chapter RESOURCES

Answer: Therefore, the number is 8.





←→



Real-World EXAMPLE

- **EARNINGS** Ms. Parsons earns \$48,400 per year. This is \$4150 more than three times as much as her daughter earns. How much does her daughter earn?
 - **Explore** Ms. Parsons earns \$4150 more than three times as much as her daughter.
 - Plan Write an equation to represent the situation.
 - Let d = her daughter's earnings.

Chapter RESOURCES

48,400 = 4150 + 3d



Real-World EXAMPLE

 3 Solve
 48,400 = 4150 + 3d Write the equation.

 48,400 - 4150 = 4150 - 4150 + 3d Subtract 4150 from each side.

 44,250 = 3d Simplify.

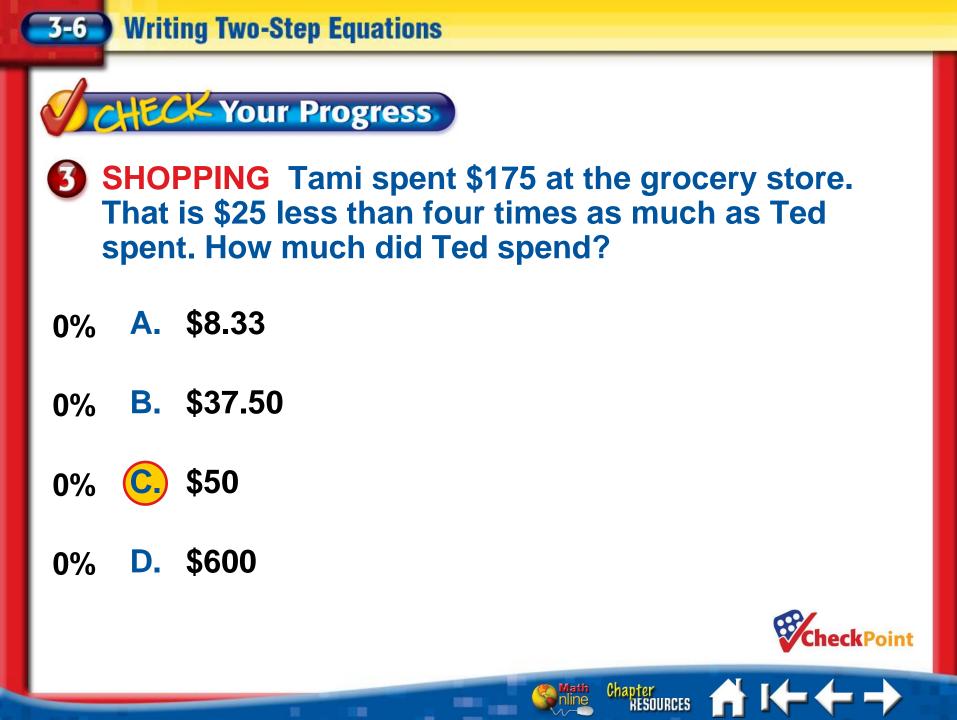
 $\frac{44,250}{3} = \frac{3d}{3}$ Divide each side by 3.

 14,750 = d Simplify.

Check Multiply 3 times 14,750 and add 4150. The result is 48,400, which is Ms. Parson's salary. The answer is correct.

Chapter RESOURCES

Answer: Ms. Parson's daughter earns \$14,750.





Real-World EXAMPLE

COMMUNITY SERVICE In a canned food drive, Sam collected 12 more cans than Louise. Together, they collected 128 cans. How many cans did Sam collect?

Let x = number of cans collected by Louise. Then x + 12 = number of cans collected by Sam.







Writing Two-Step Equations

Real-World EXAMPLE

4

$$x + (x + 12) = 128$$

(x + x) + 12 = 128

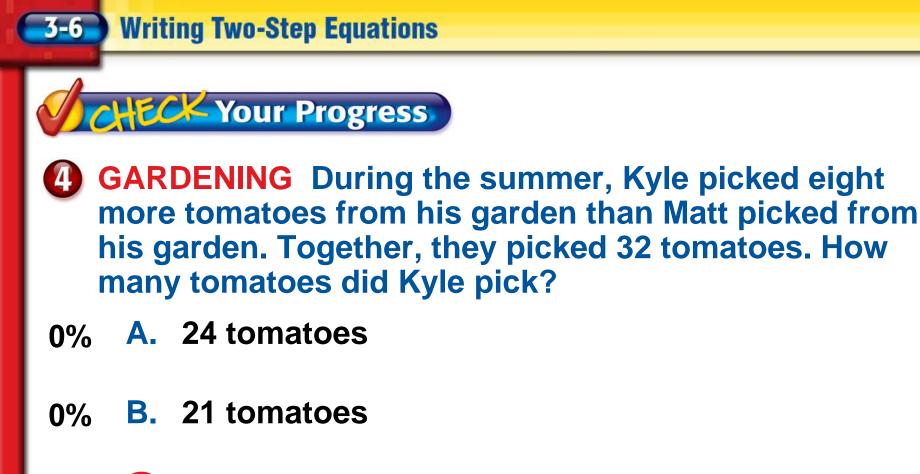
2x + 12 = 128

- Write the equation.
- Associative Property
- Combine like terms.
- 2x + 12 12 = 128 12 Subtract 12 from each side.

Chapter RESOURCES

- 2x = 116Simplify.
 - Mentally divide each side x = 58by 2.

Answer: So, Louise collected 58 cans and Sam collected 58 + 12 or 70 cans.



- 0% C. 20 tomatoes
- 0% D. 12 tomatoes



Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Lesson Menu

Five-Minute Check (over Lesson 3-6)

Main Ideas and Vocabulary

Example 1: Describe an Arithmetic Sequence

Example 2: Find a Term in an Arithmetic Sequence

Example 3: Real-World Example





Main Ideas

• Describe sequences using words and symbols.

Chapter RESOURCES

• Find terms of arithmetic sequences.

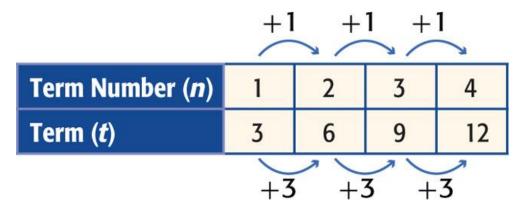
New Vocabulary

- sequence
- arithmetic sequence
- term
- common difference



EXAMPLE Describe an Arithmetic Sequence

Describe the sequence 3, 6, 9, 12, ... using words and symbols.



Answer: The difference of the term numbers is 1. The terms have a common difference of 3. Also, a term is 3 times the term number. The equation t = 3n describes the sequence.



HECK Your Progress

Describe the sequence 7, 14, 21, 28, ... using words and symbols.

- ^{0%} A. difference of term numbers: 7; common difference: 1; equation: t = n + 3
- 0% B. difference of term numbers: 7; common difference: 1; equation: t = 7n
- ^{0%} C. difference of term numbers: 1; common difference: 7; equation: t = n + 3

0%

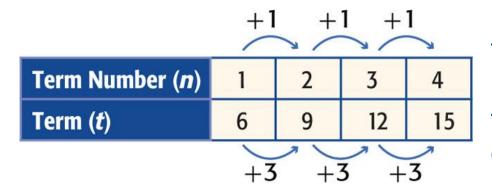
difference of term numbers: 1; common difference: 7; equation: *t* = 7*n*





EXAMPLE Find a Term in an Arithmetic Sequence

Pind the 11th term of 6, 9, 12, 15,



The difference of the term numbers is 1.

The terms have a common difference of 3.

Chapter RESOURCES

The common difference is 3 times the difference of the term numbers.

This suggests that t + 3n. However, you need to add 3 to get the exact value of t. Thus, t = 3n + 3.



EXAMPLE Find a Term in an Arithmetic Sequence

2 Check If n = 2, then t = 3(2) + 3 or 9.

If
$$n = 4$$
, then $t = 3(4) + 3$ or 15.

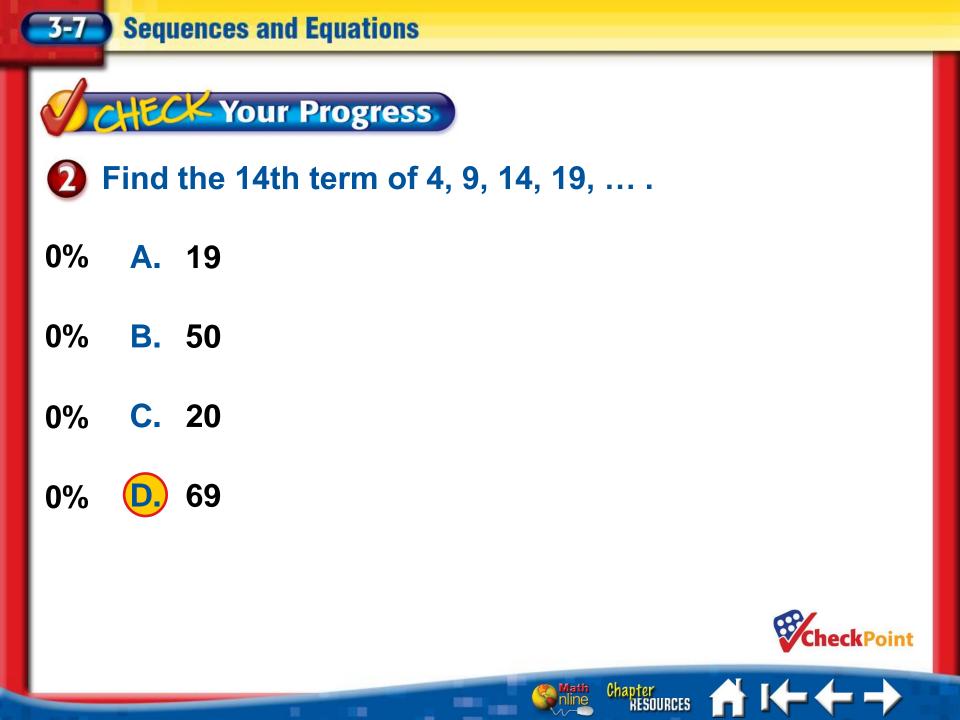
To find the 11th term in the sequence, let n = 11 and solve for *t*.

t = 3n + 3 Write the equation.

Chapter RESOURCES

= 3(11) + 3 or 36

Answer: The 11th term is 36.





Sequences and Equations

Real-World EXAMPLE

3 TELEPHONE CHARGES For a telephone call to India, a telephone company charges \$8 for the first minute and \$4 for each additional minute. How much does it cost for a 10-minute call?









Make a table to organize the sequence and find a rule.

Number of Minutes (<i>m</i>)	1	2	3	
Cost (c)	8	12	16	•
				•

The difference of the term numbers is 1.

The terms have a common difference of 4.

Chapter RESOURCES

The pattern in the table shows the equation c = 4m + 4.

If c = 4m + 4 or c = 4(10) + 4, then c = 44.

Answer: A 10-minute call would cost \$44.



3 READING During one month Mitch read 3 books. Each month after, he read only 2 books. After 12 months, how many books did Mitch read?

- 0% A. 22 books
- 0% B. 24 books
- 0% **C.** 25 books
- 0% D. 27 books



Chapter RESOURCES

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.





Lesson Menu

Five-Minute Check (over Lesson 3-7)

Main Ideas and Vocabulary

Example 1: Real-World Example

Key Concept: Perimeter of a Rectangle

Example 2: Find Perimeters and Lengths of Rectangles

Key Concept: Area of a Rectangle

Example 3: Find Areas and Lengths of Rectangles

Chapter RESOURCES

Main Ideas

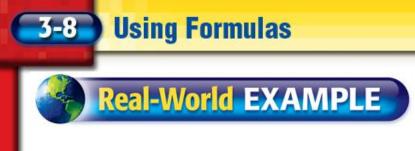
Using Formulas

- Solve problems by using formulas.
- Solve problems involving the perimeters and areas of rectangles.

Chapter RESOURCES

New Vocabulary

- formula
- perimeter
- area



3

45 = r

TRAVEL If you travel 135 miles in 3 hours, what is your average speed in miles per hour?

Method 1 Substitute first.

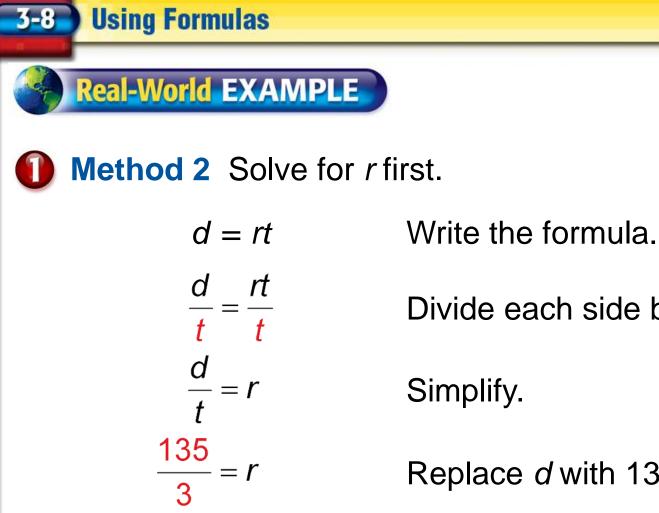
d = rt Write the formula.

135 = $r \cdot 3$ Replace d with 135 and t with 3.135 $r \cdot 3$ Divide cook cide by 2

Divide each side by 3.

Chapter RESOURCES

Simplify.

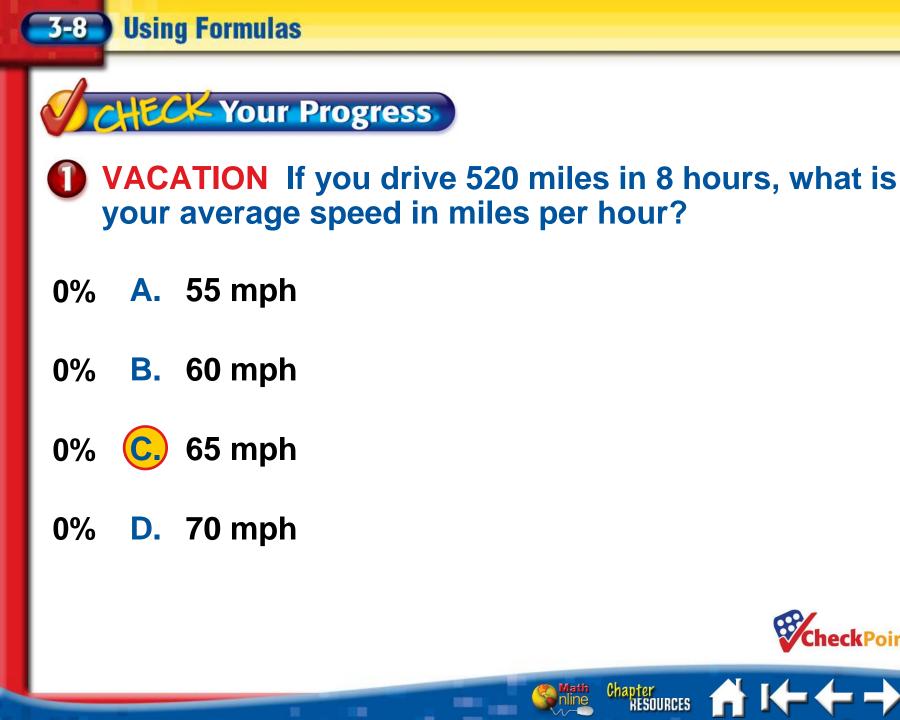


Divide each side by t. Simplify. Replace *d* with 135 and *t* with 3.

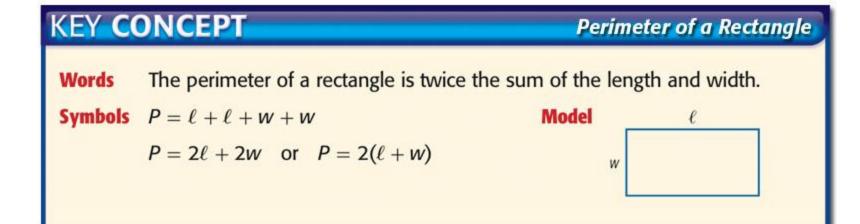
Chapter RESOURCES

45 = rSimplify.

Answer: The average speed is 45 miles per hour.



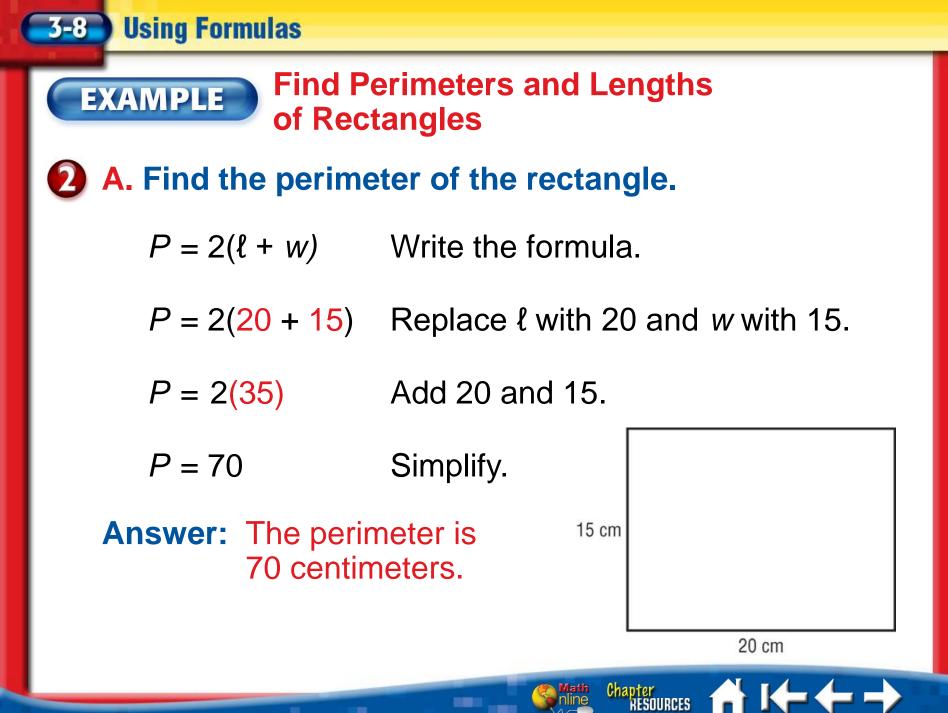




Using Formulas

3-8





Using Formulas

EXAMPLE

Find Perimeters and Lengths of Rectangles

B. The perimeter of a rectangle is 60 feet. Its width is 9 feet. Find its length.

$P=2\ell+2w$	Write the formula.

 $60 = 2\ell + 2(9)$ Replace *P* with 60 and *w* with 9.

 $60 = 2\ell + 18 \qquad \text{Simplify.}$

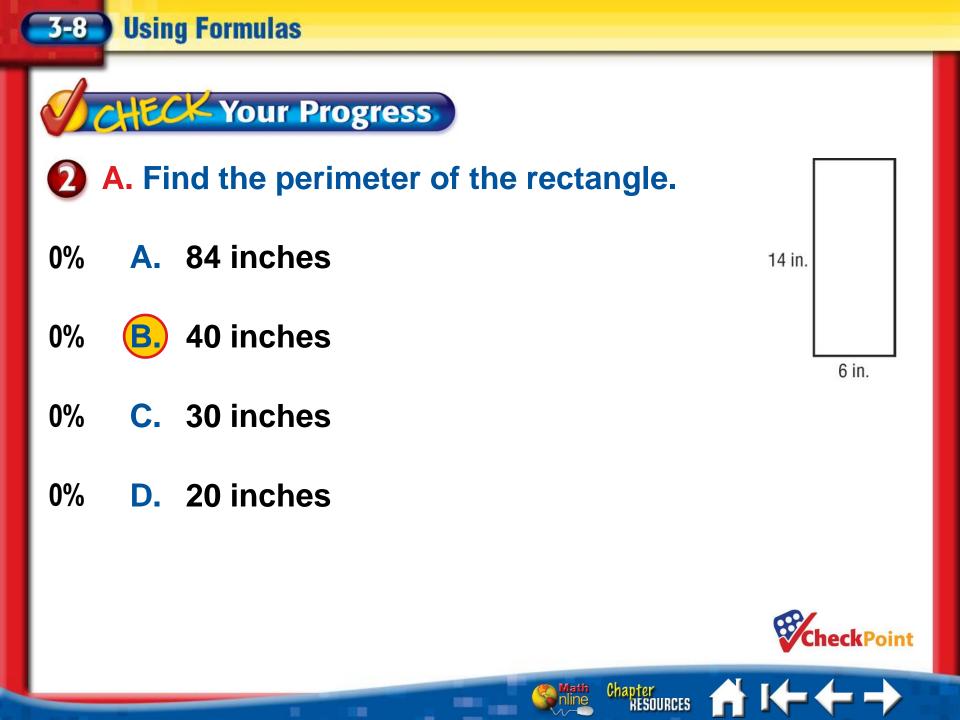
 $60 - 18 = 2\ell + 18 - 18$ Subtract 18 from each side.

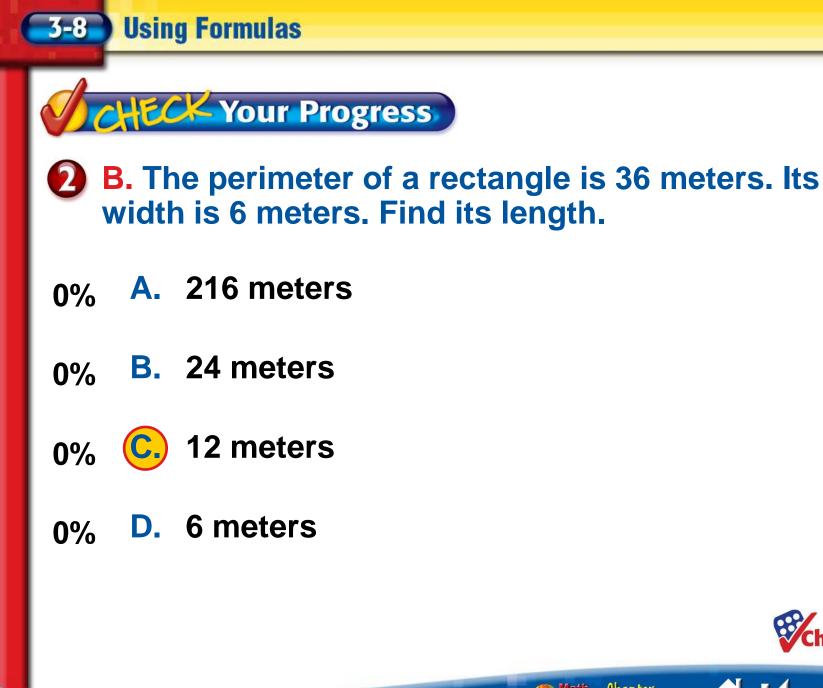
 $42 = 2\ell$ Simplify.

 $21 = \ell$ Mentally divide each side by 2.

Chapter RESOURCES

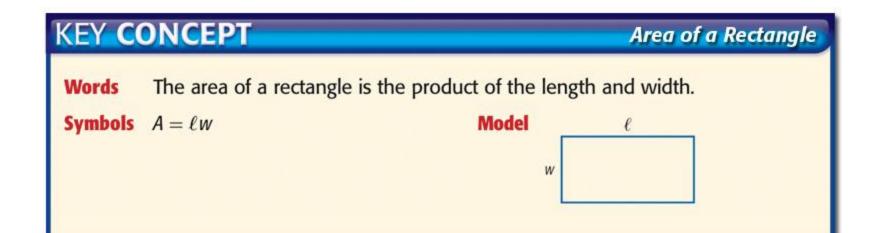
Answer: The length is 21 feet.







Chapter RESOURCES



3-8

Using Formulas



EXAMPLE Find Areas and Lengths of Rectangles

Chapter RESOURCES

A. Find the area of a rectangle with length 14 feet and width 6 feet.

 $A = \ell w$ Write the formula.

- $A = 14 \bullet 6$ Replace ℓ with 14 and w with 6.
- A = 84 Simplify.

Using Formulas

Answer: The area is 84 square feet.

EXAMPLE Find Areas and Lengths of Rectangles

B. The area of a rectangle is 40 square meters. Its length is 8 meters. Find its width.

Using Formulas

Method 1 Substitute, then solve for the variables.

- $A = \ell w$ Write the formula.
- 40 = 8w Replace A with 40 and ℓ with 8.
 - 5 = w Mentally divide each side by 8.



EXAMPLE Find Areas and Lengths of Rectangles

Method 2 Solve, then substitute.

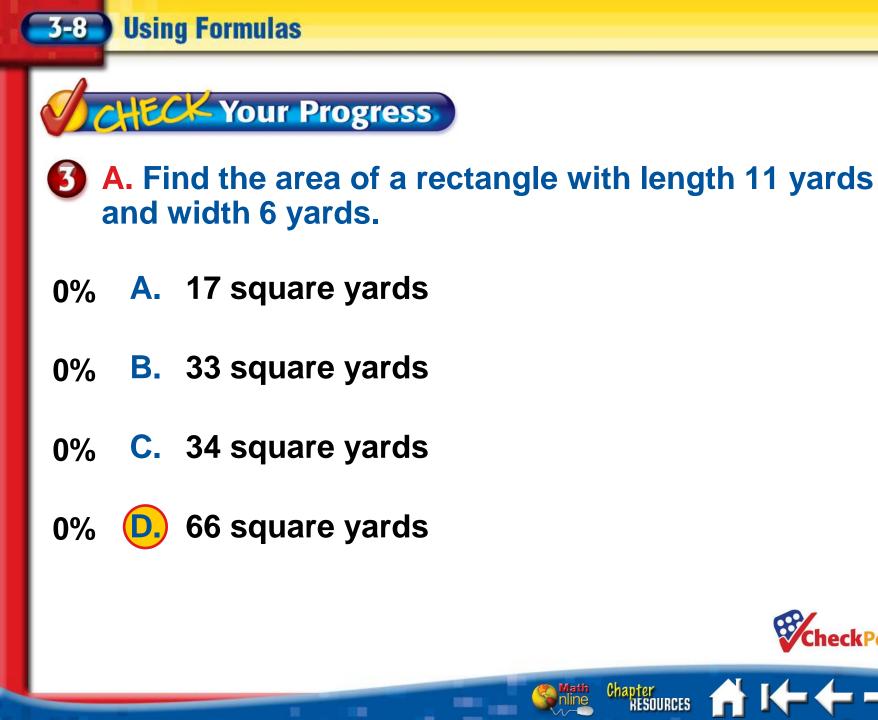
Using Formulas

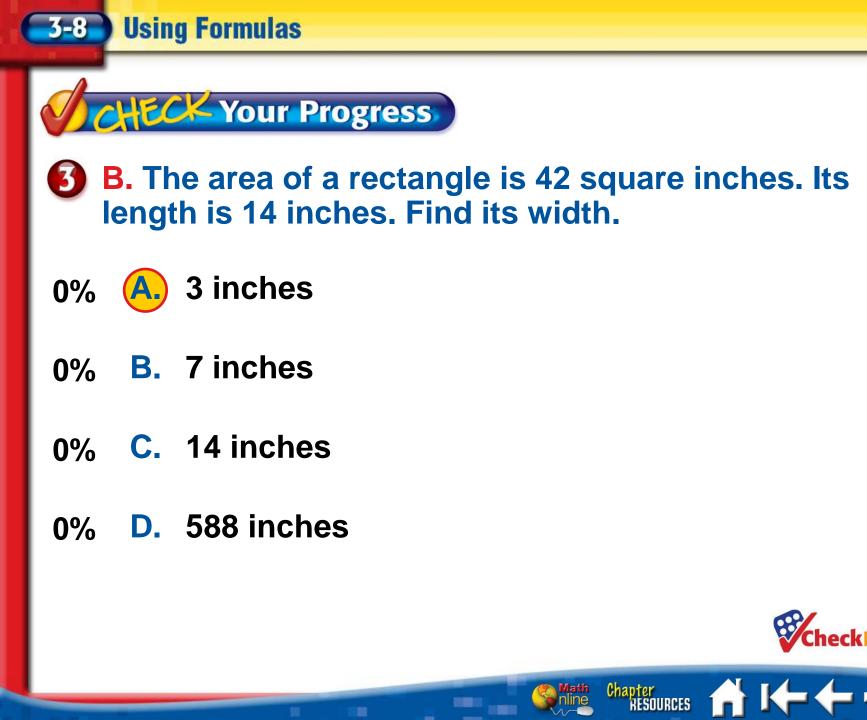
-8

$A = \ell w$	Write the formula.
$\frac{A}{\ell} = \frac{\ell w}{\ell}$	Divide each side by <i>l</i> .
$\frac{A}{\ell} = W$	Simplify.
$\frac{40}{8} = W$	Replace A with 40 and ℓ with 8.
5 = <i>w</i>	Simplify.

Chapter RESOURCES

Answer: The width is 5 meters.





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Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







CHAPTER

3

Chapter Resources Menu



CheckPoint Five-Minute Checks



Image Bank



Math Tools

C^Oncepts in **MOtion**

An Imation Solving Equations Using Algebra Tiles

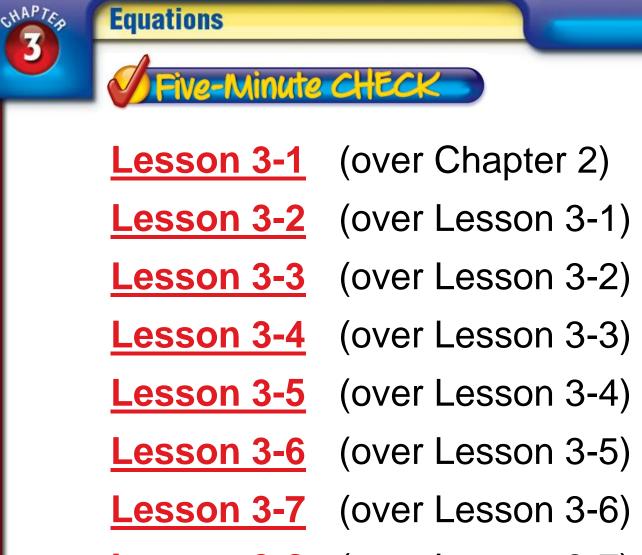


Interactive Solving Equations Using Multiplication and Division

Brain

Distributive Property





Lesson 3-8 (over Lesson 3-7)



HAPTE



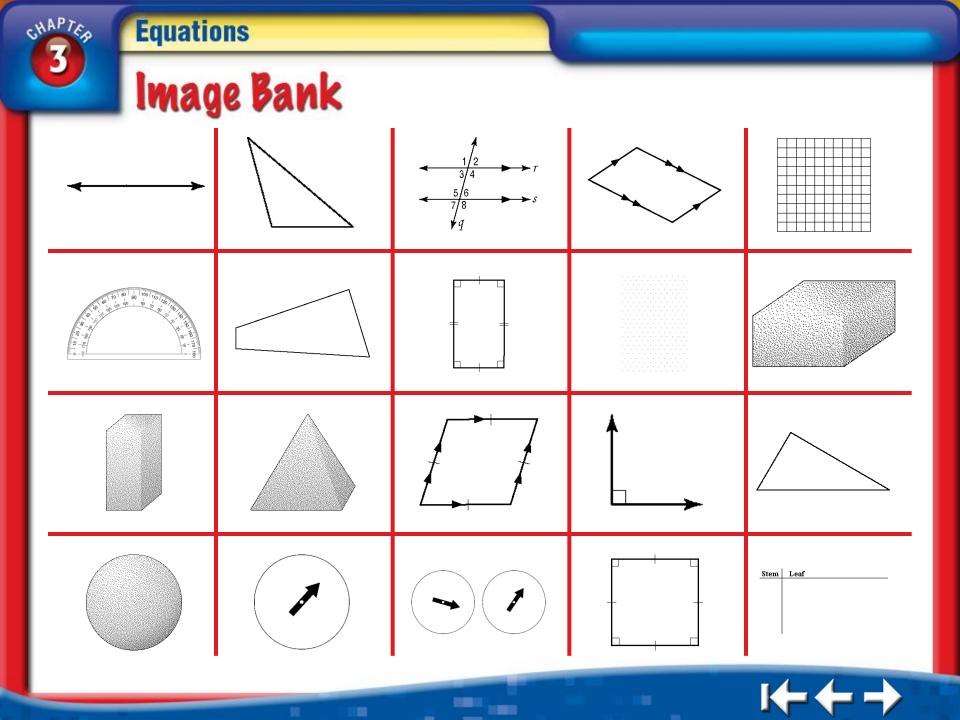
To use the images that are on the following three slides in your own presentation:

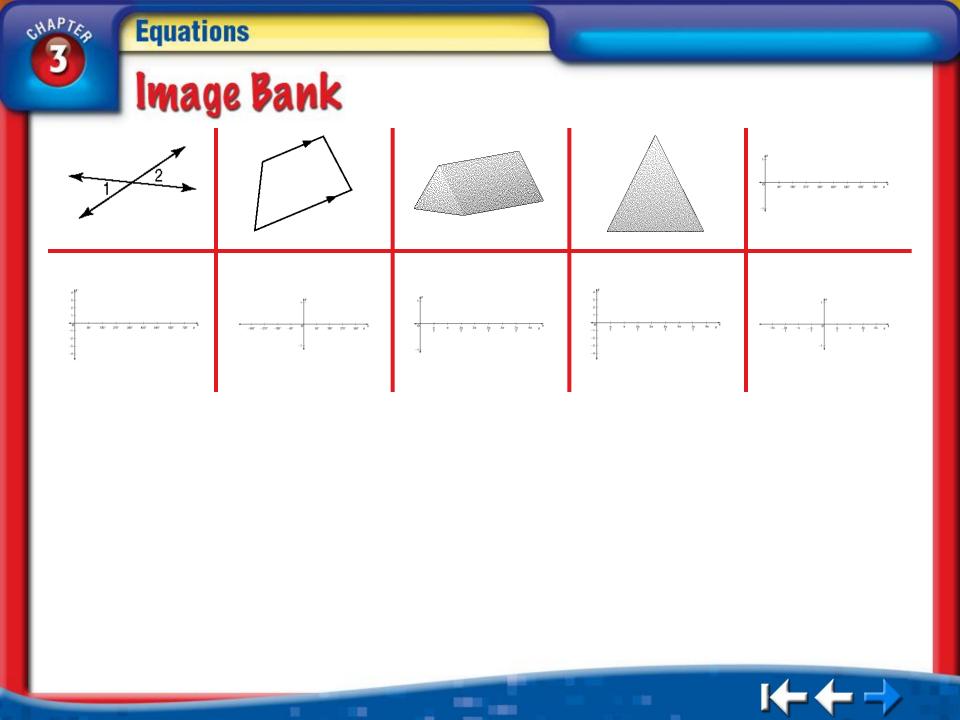
- **1.** Exit this presentation.
- 2. Open a chapter presentation using a full installation of Microsoft[®] PowerPoint[®] in editing mode and scroll to the Image Bank slides.
- **3.** Select an image, copy it, and paste it into your presentation.



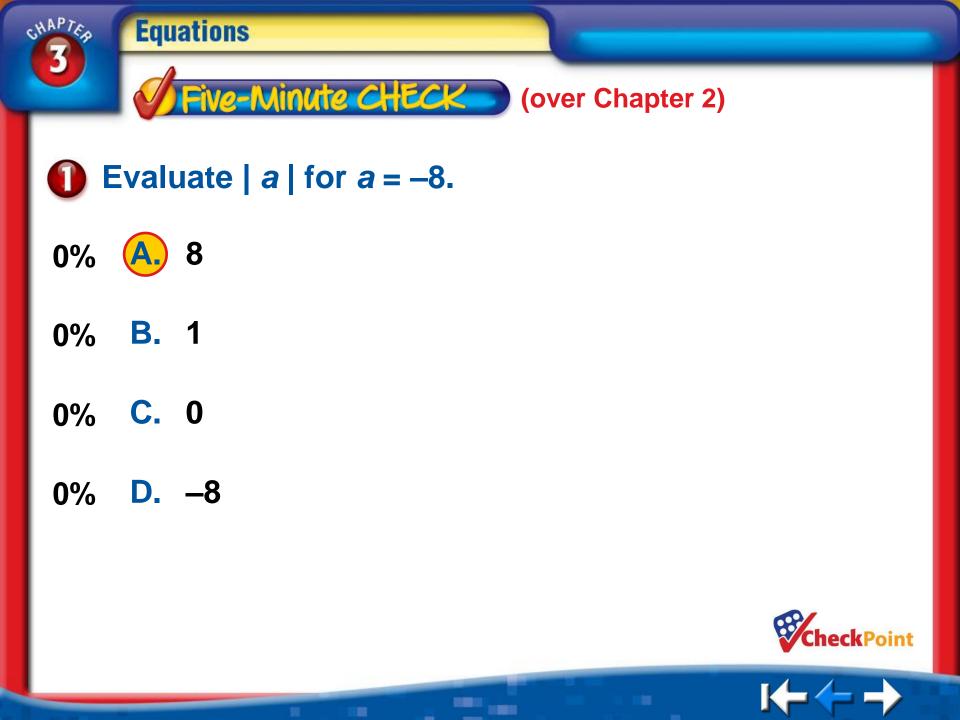
CHAPTER Equation	ons					
Image Bank						
$\begin{array}{c} \bullet + \bullet + \bullet + \bullet + \bullet + \bullet + \bullet \bullet \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \bullet \bullet + \bullet \\ \bullet \bullet - 5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 \end{array}$			5 6	$\xrightarrow{1/2}$		
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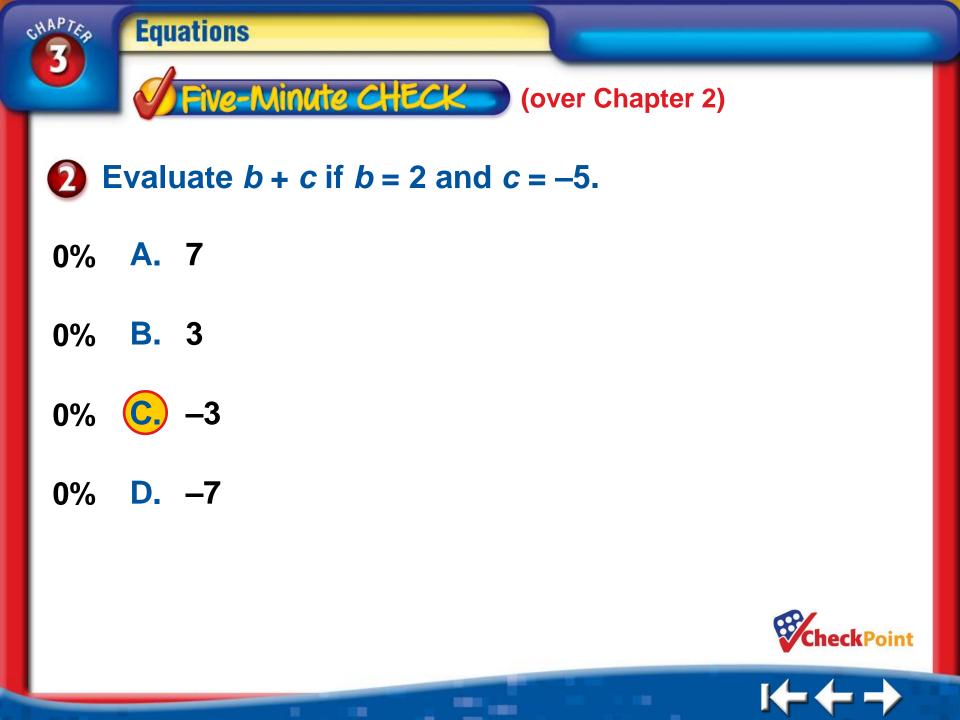


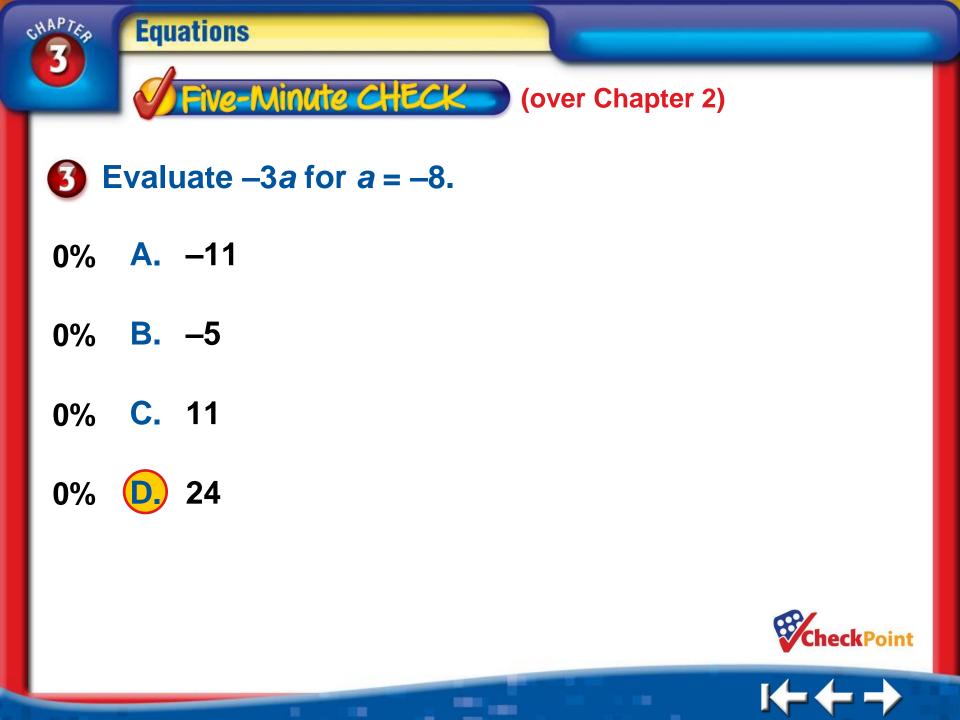


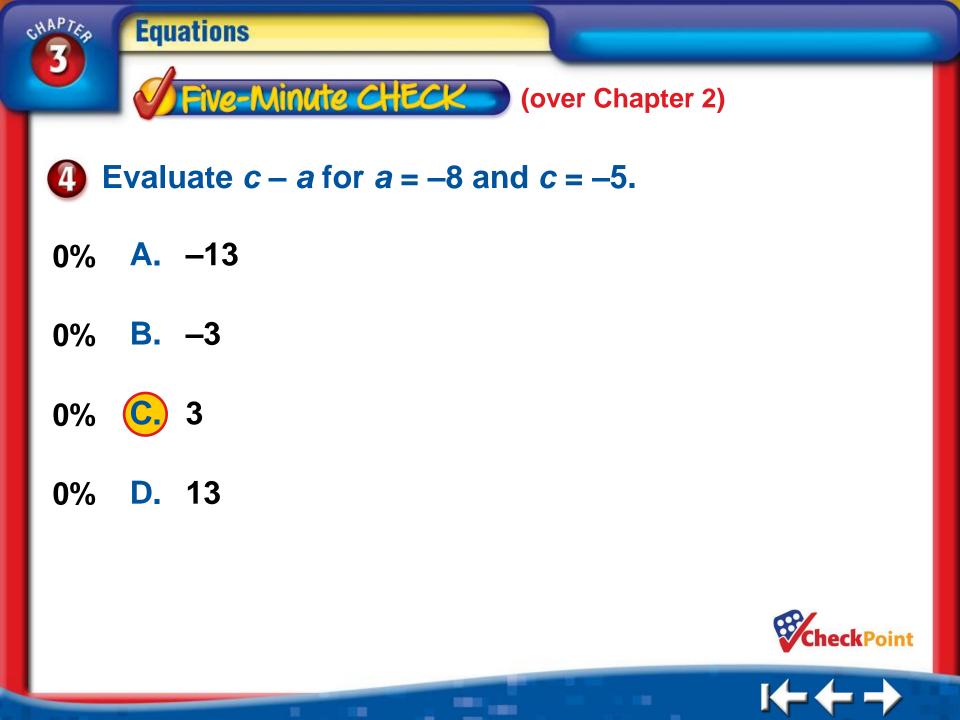


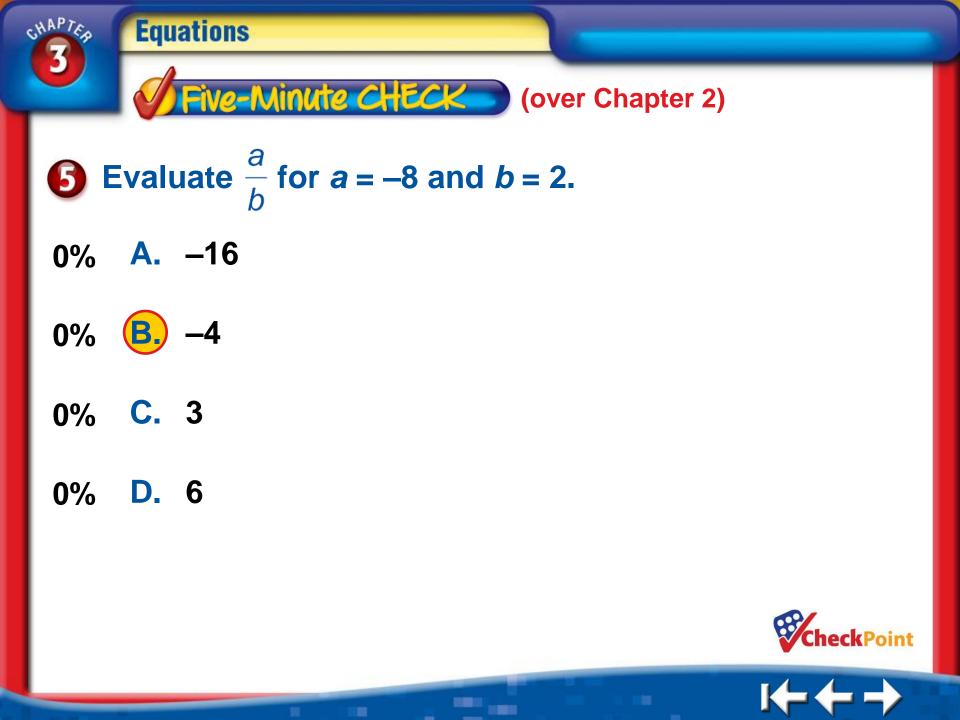








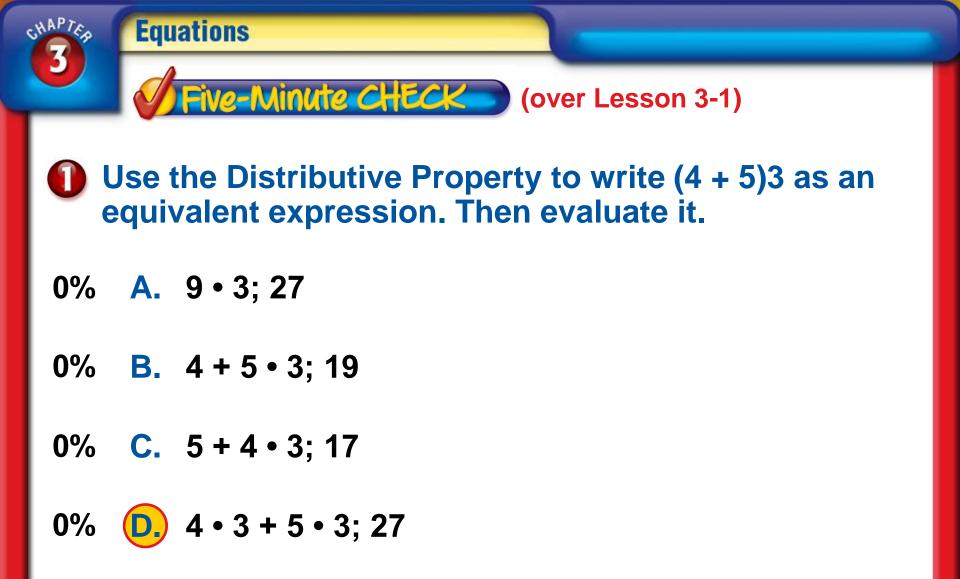




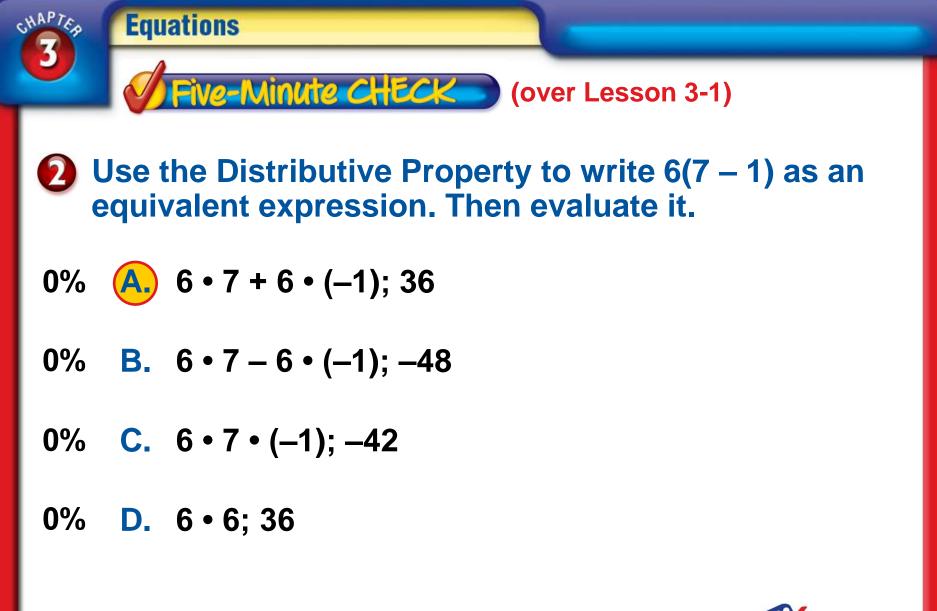


- **6** The daily low temperatures over the past 5 days were 0° F, –5°F, –7°F, –1°F, and 3°F. What was the average low temperature over the 5-day period?
- 0% A. 0°F
- 0% **B.** –1°F
- 0% **C**. –2°F
- 0% **D.** –5°F



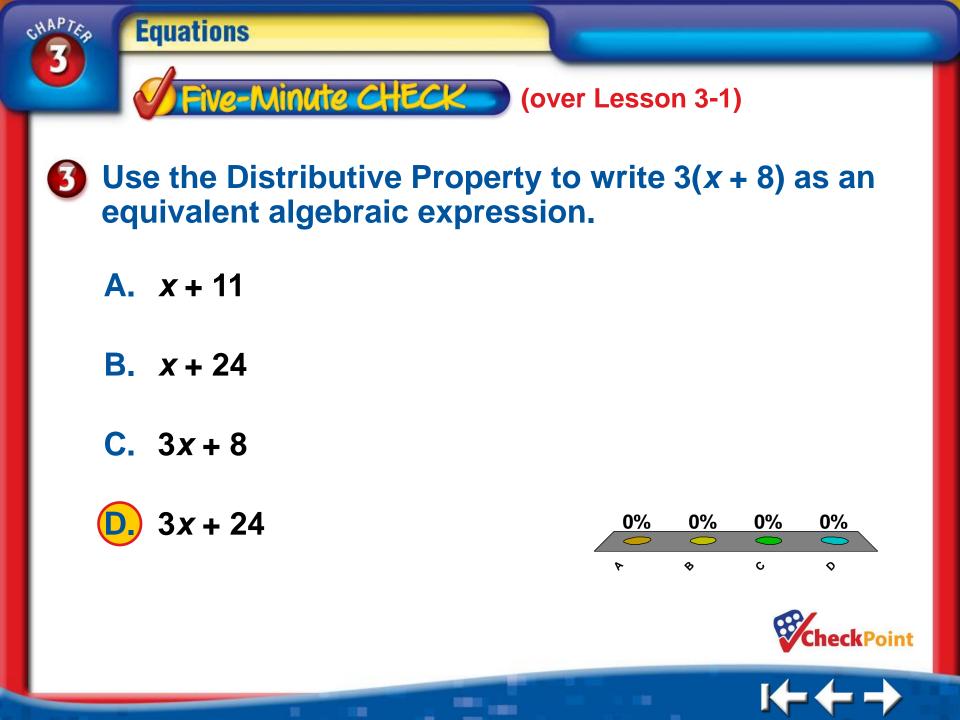


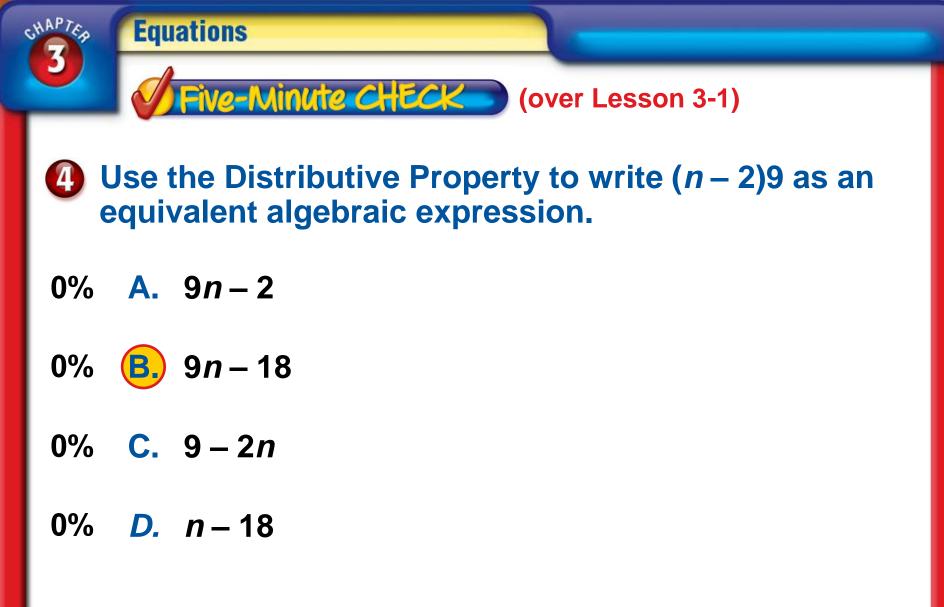
















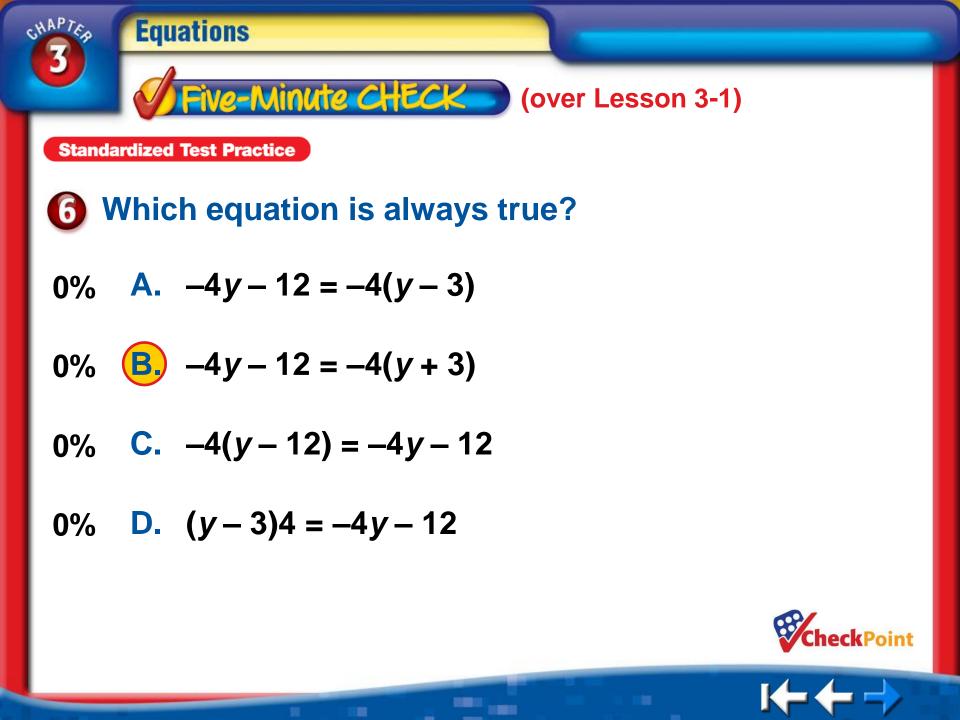
Use the Distributive Property to write –2(a + 5) as an equivalent algebraic expression.

0% A. −*a* − 5

- 0% **B**. −*a* − 10
- 0% **C**. –2*a* 10
- 0% **D**. −2*a*−5









Identify the terms, like terms, coefficients, and constants in the expression 4q + 5p - 9 - p + 8q.

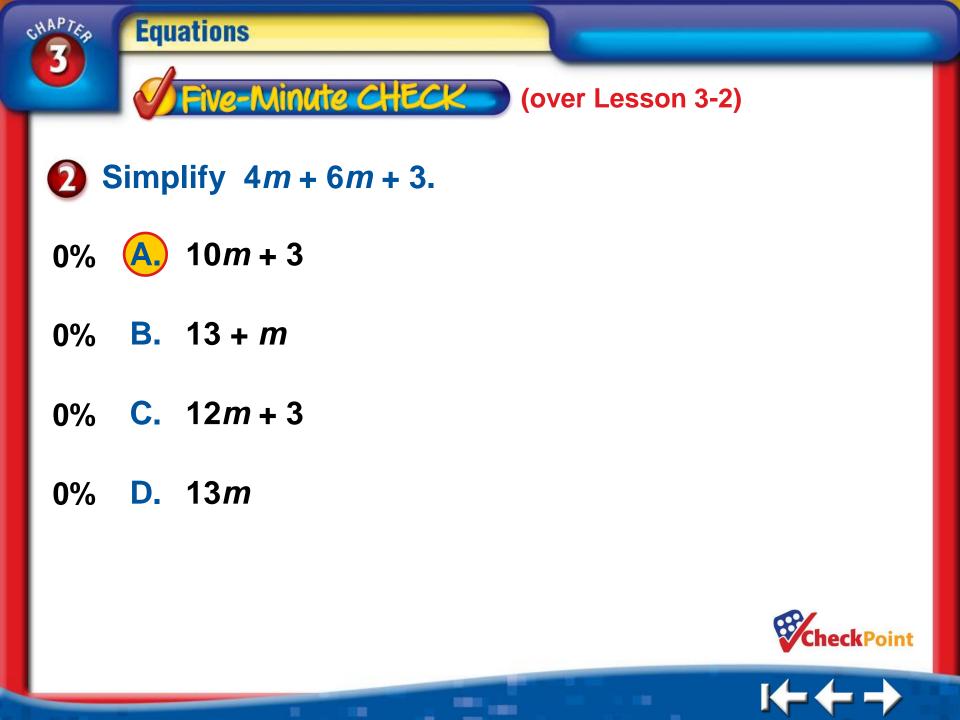
- 0% A. terms: 4q, 5p, -9, -p, 8q; like terms: 4q, 8q, 5p, -p; coefficients: 4, 5, -1, 8, -9; constants: 4, 5, -9, -1, 8
 - B. terms: 4q, 5p, -p, 8q; like terms: 4q, 8q; coefficients: 4, 5, -1, 8; constants: 4, 5, -9, -1, 8

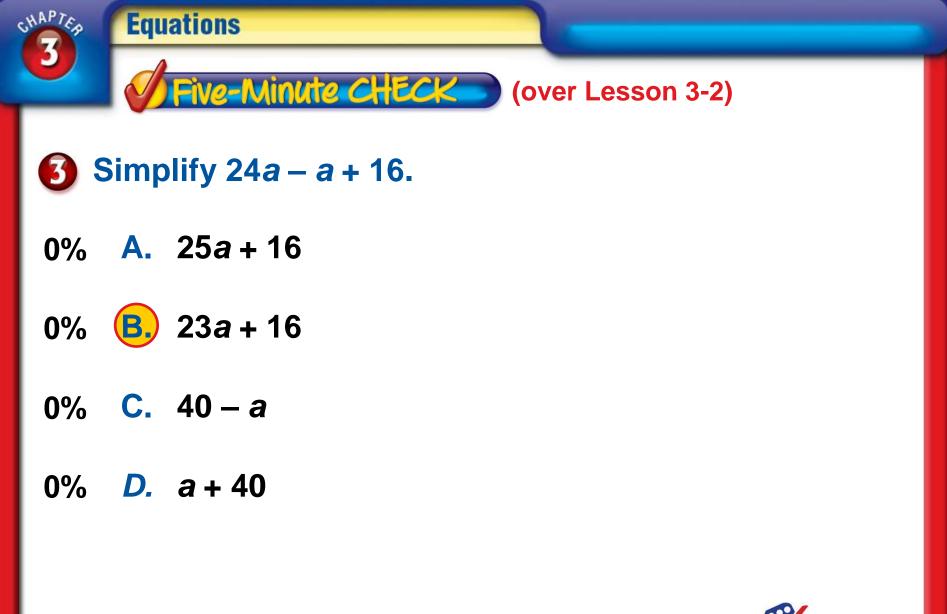
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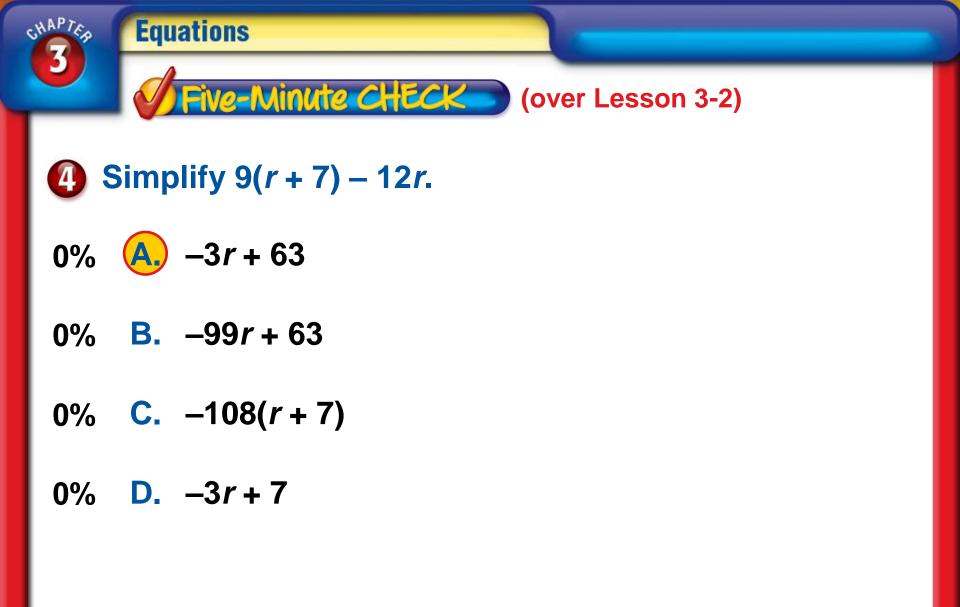
- terms: 4*q*, 5*p*, –9, –*p*, 8*q*; like terms: 4*q*, 8*q*; 5*p*, –*p;* coefficients: 4, 5, –1, 8; constants: –9
- **0% D.** terms: 4q, 5p, -9, -p, 8q; like terms: 4q, 8q: 5p, -p; coefficients: 4, 5, -1, 8, -9; constants: -9











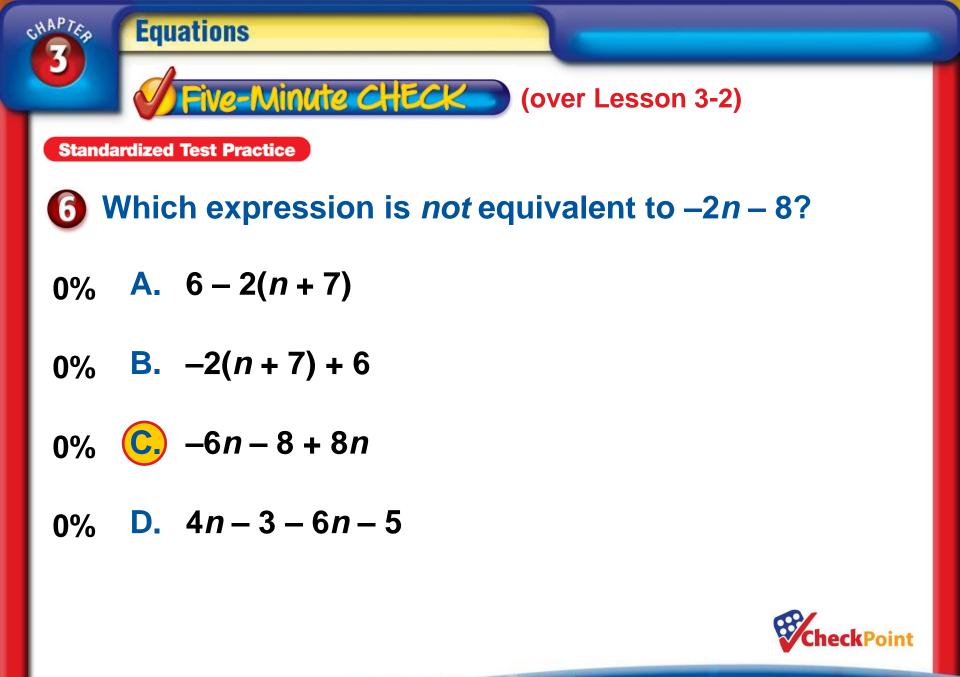


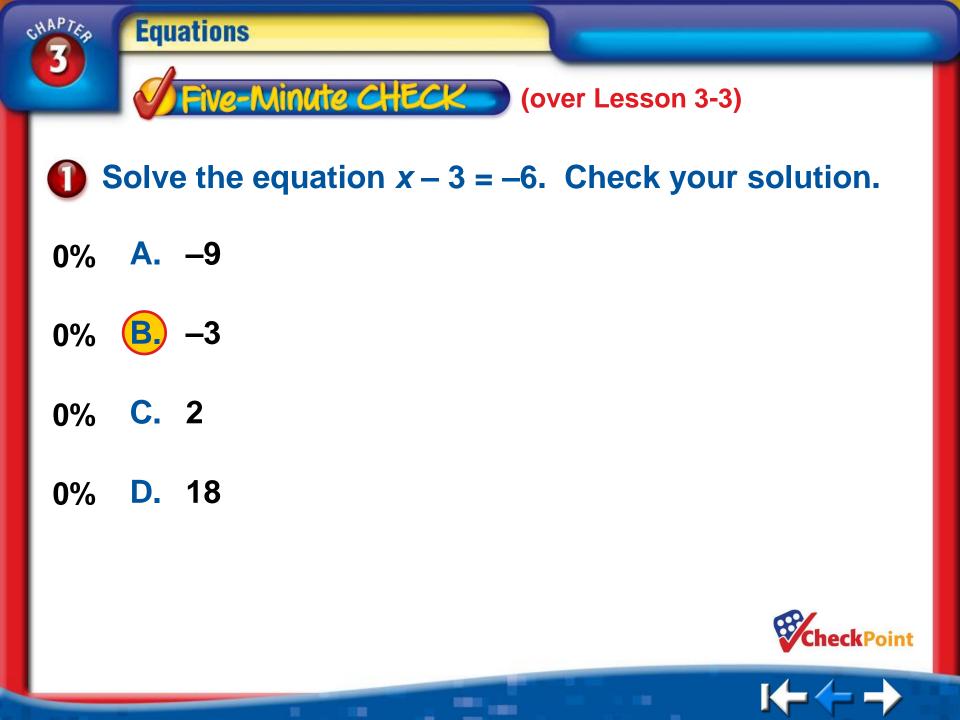


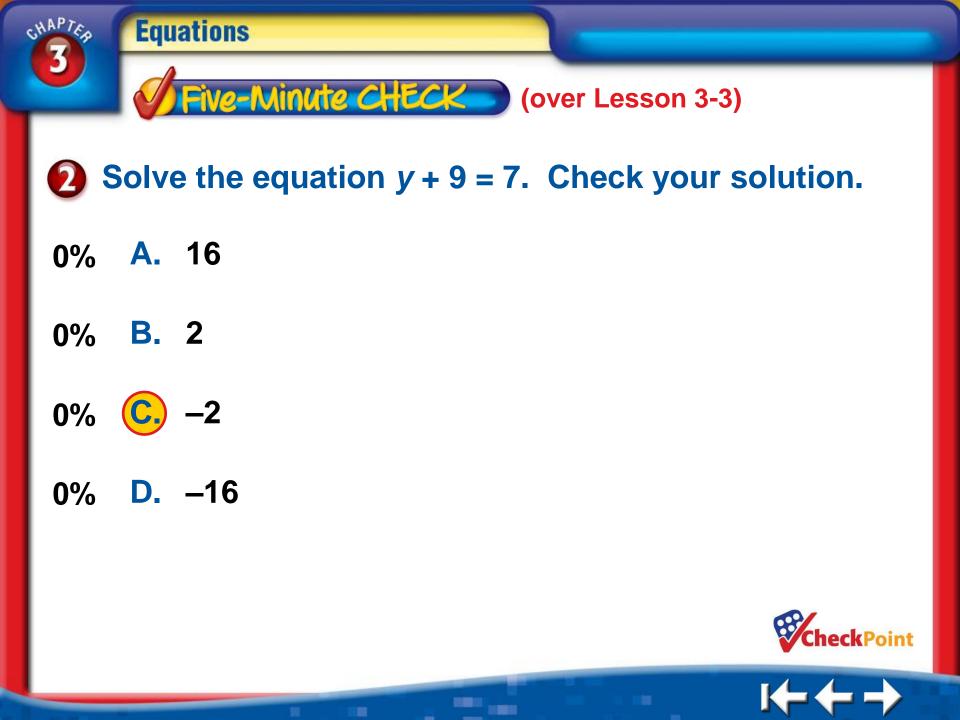
- 0% A. 9*x* 12
- 0% **B**. 14*x* 2
- **0% C.** 54*x*−12
- 0% **D**, 14*x* 12

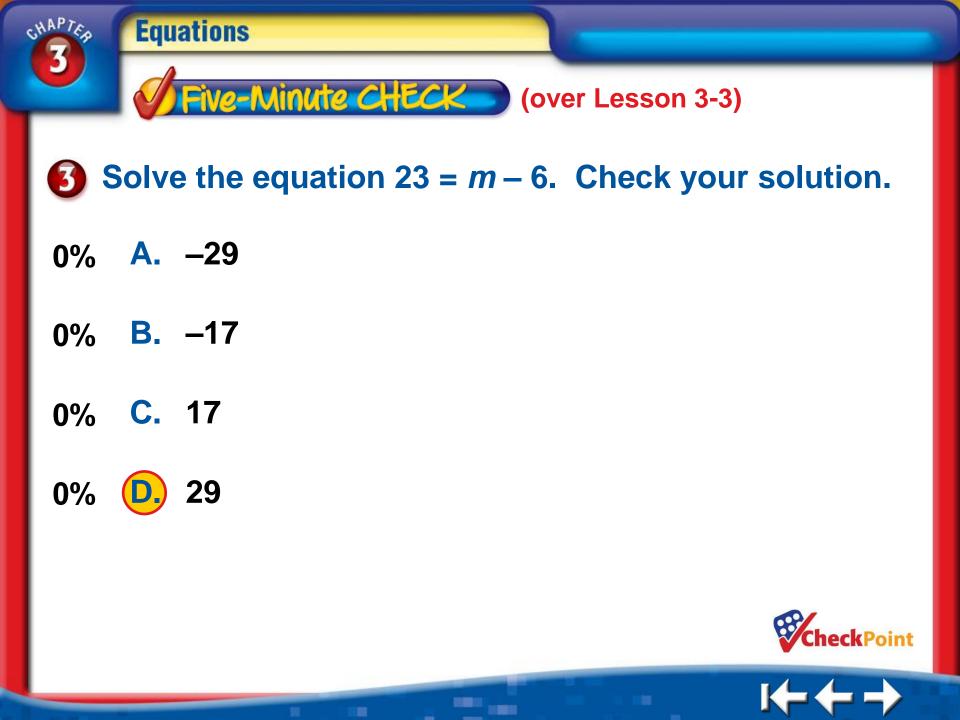


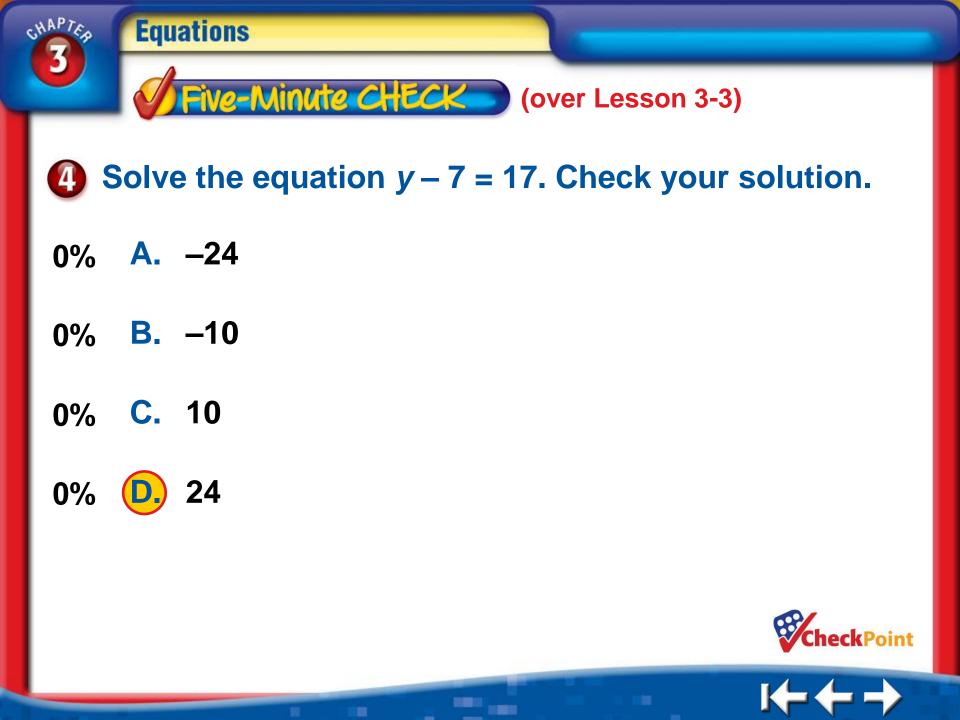


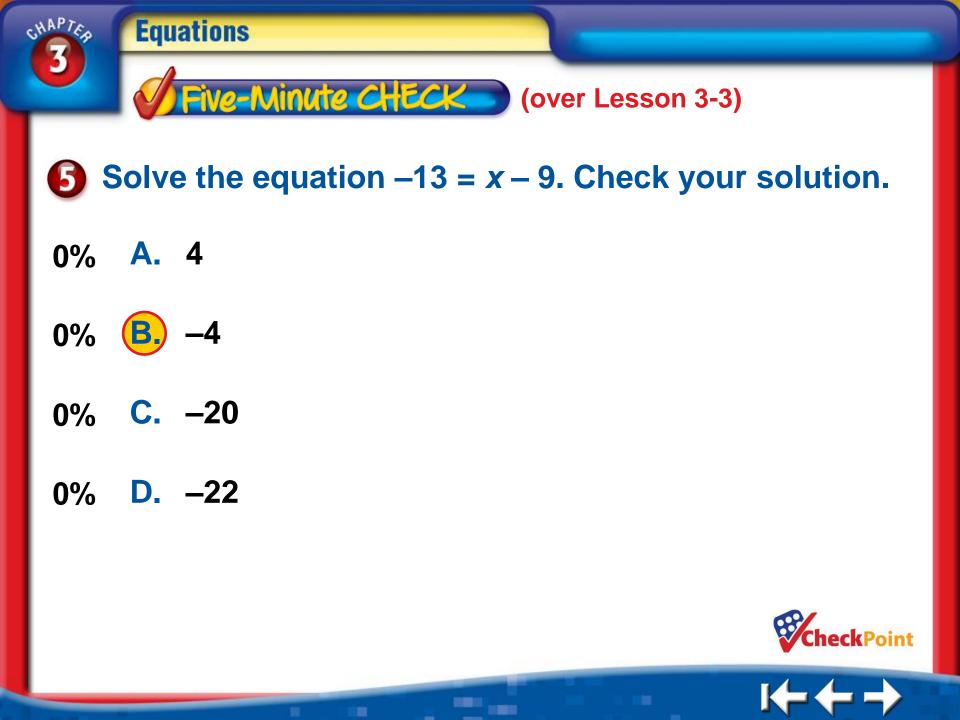














6 Kendal scored 63 points during the basketball season. This is 11 less than the number of points that Santiago scored. Which equation can be used to find the number of points Santiago scored during the season?

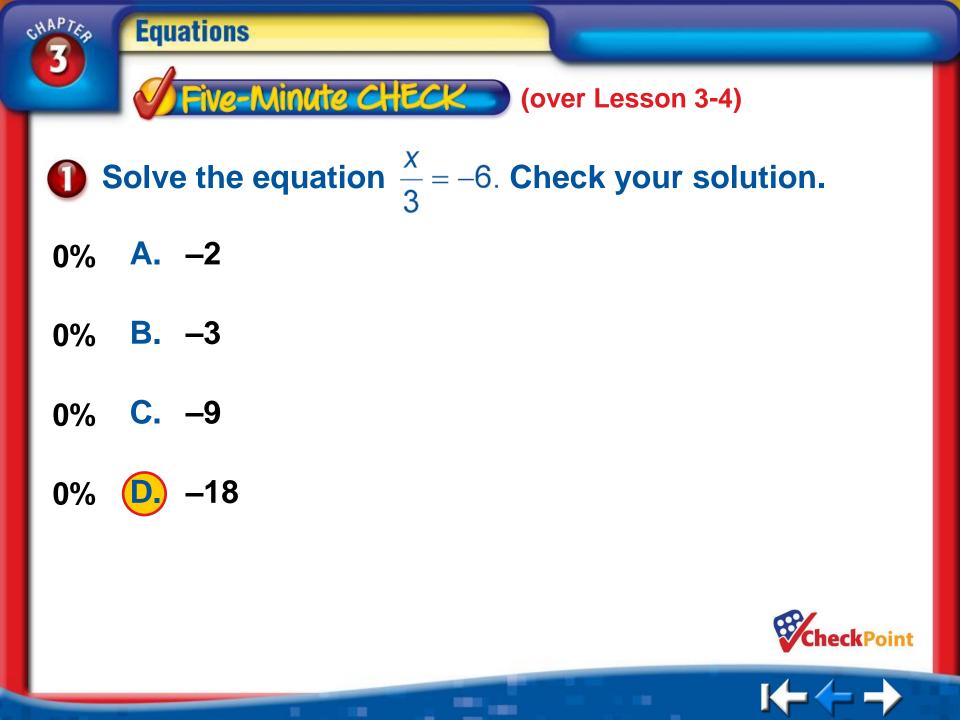
0% A.
$$11 - x = 63$$

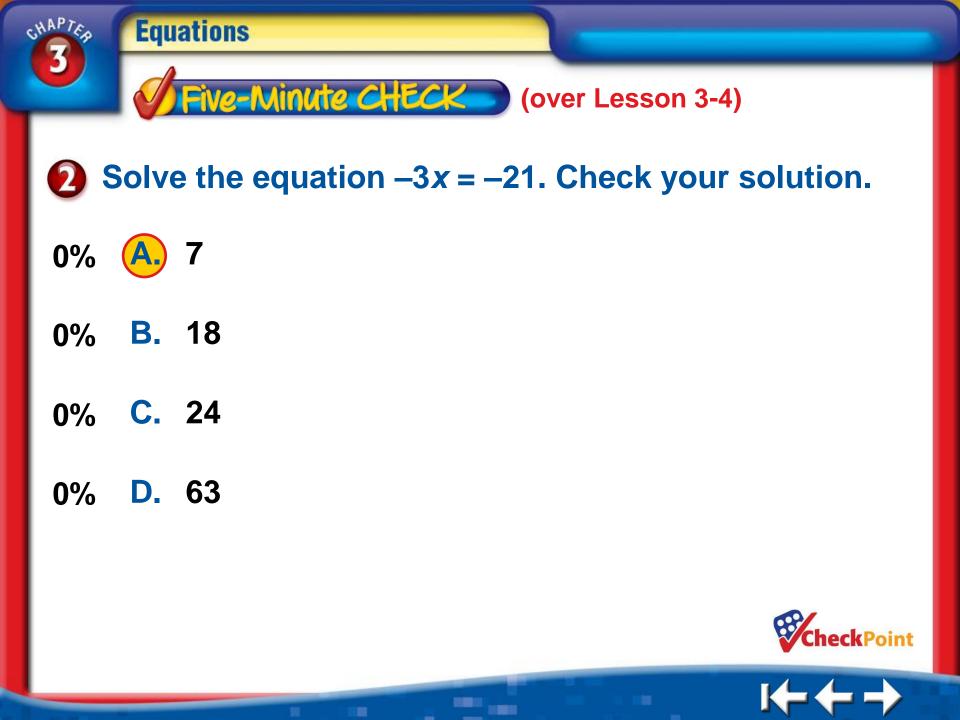
0% **B**.
$$x - 11 = 63$$

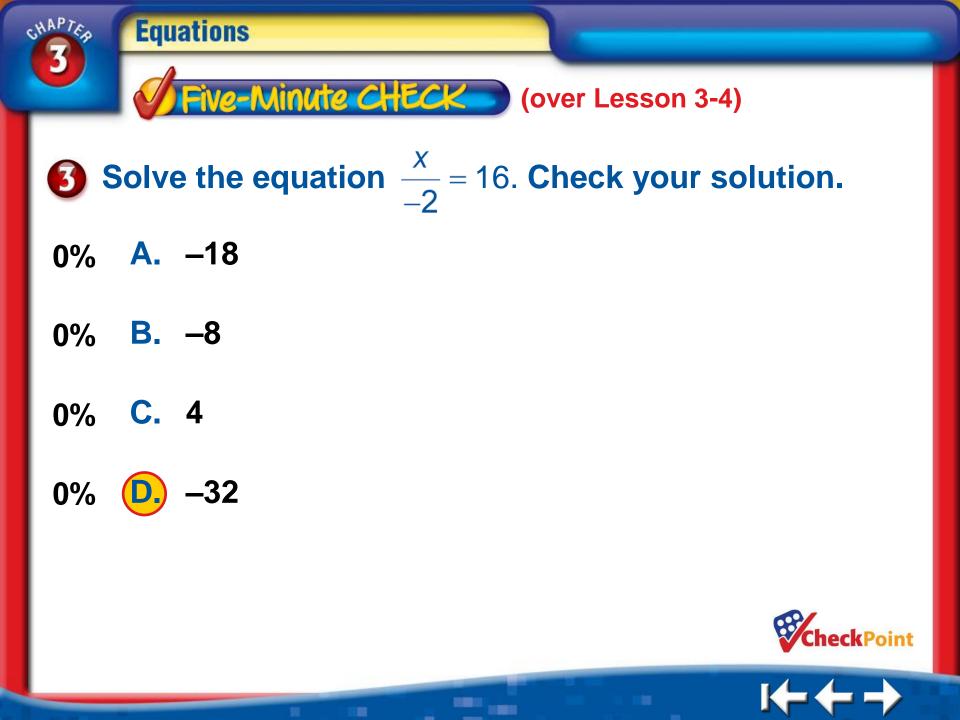
0% C.
$$x + 11 = 63$$

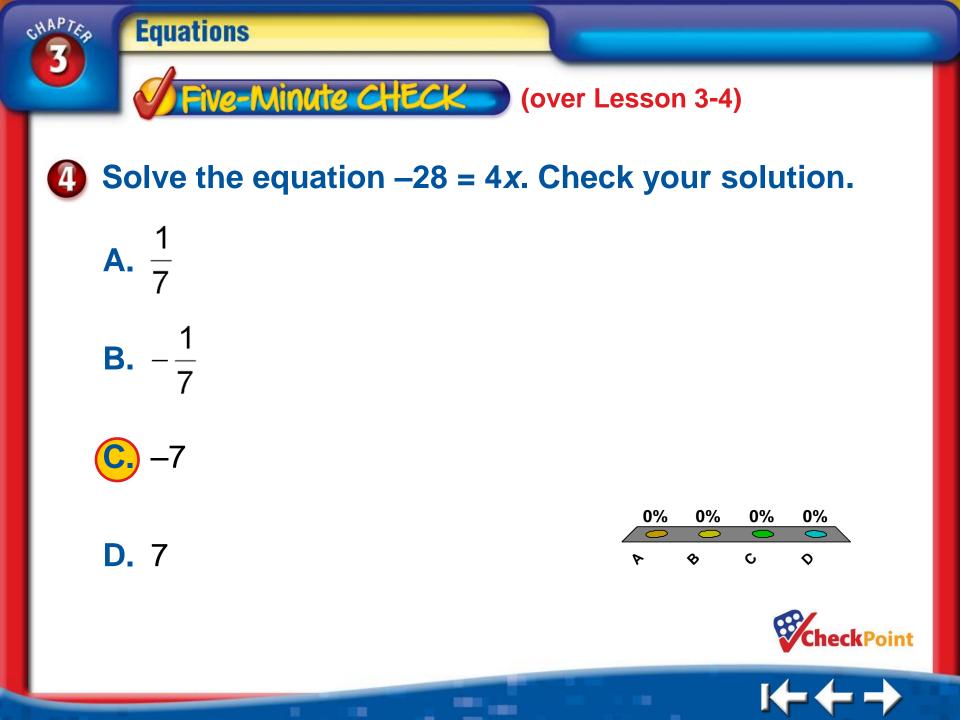
0% **D**. -63 = 11 + x

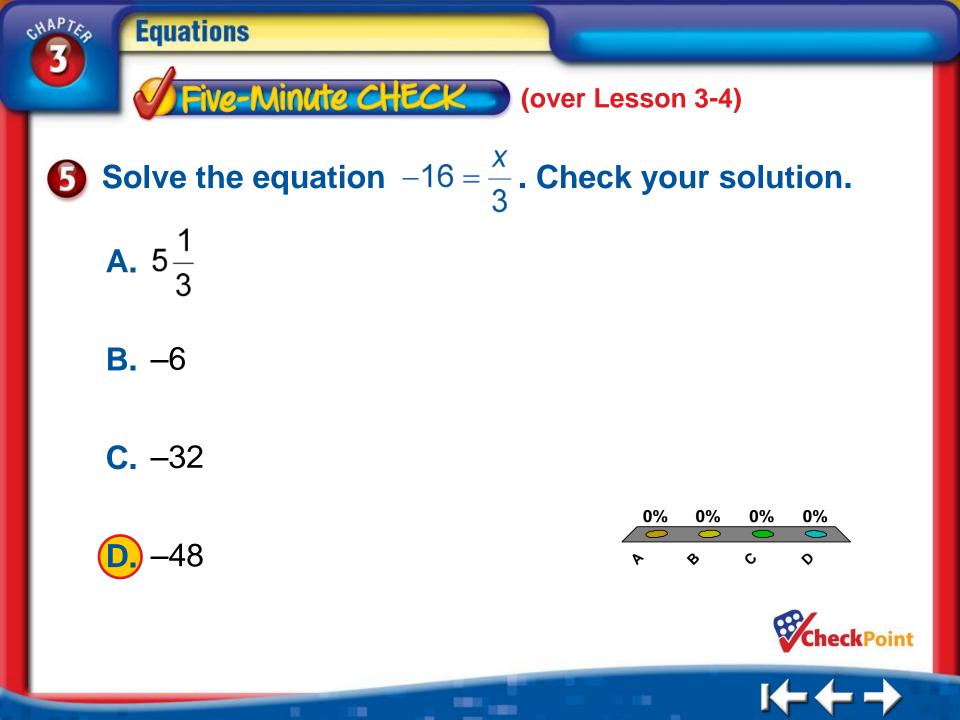


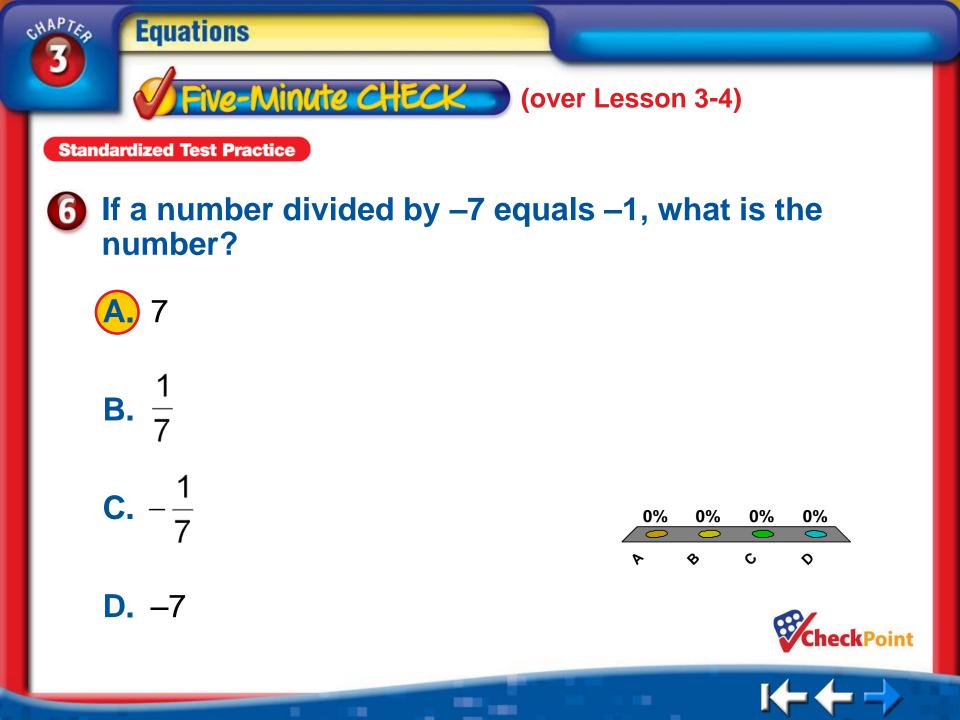


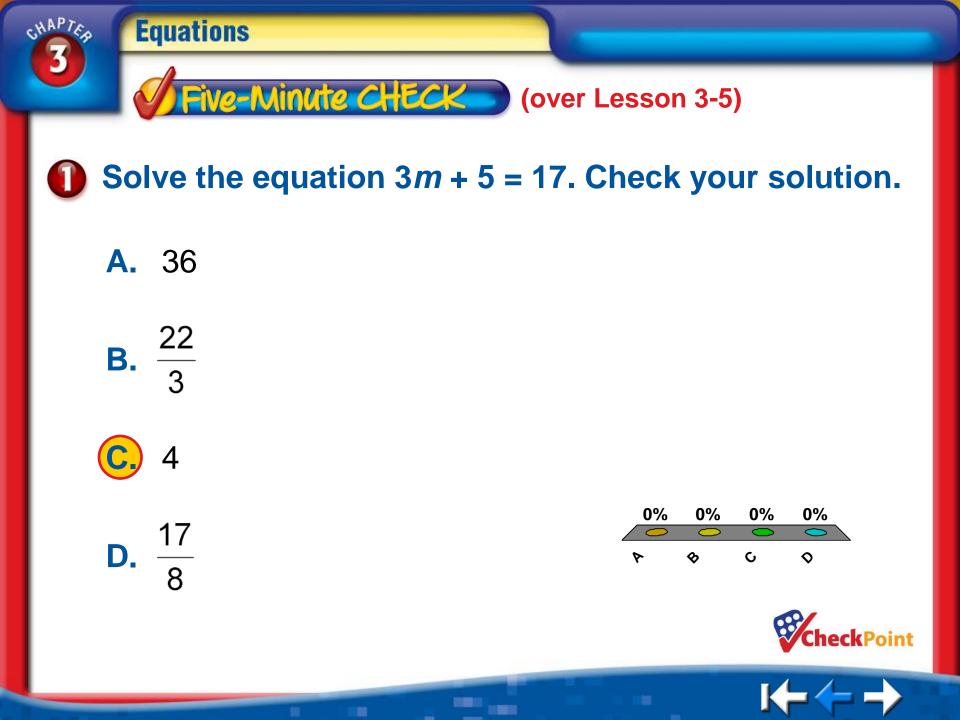


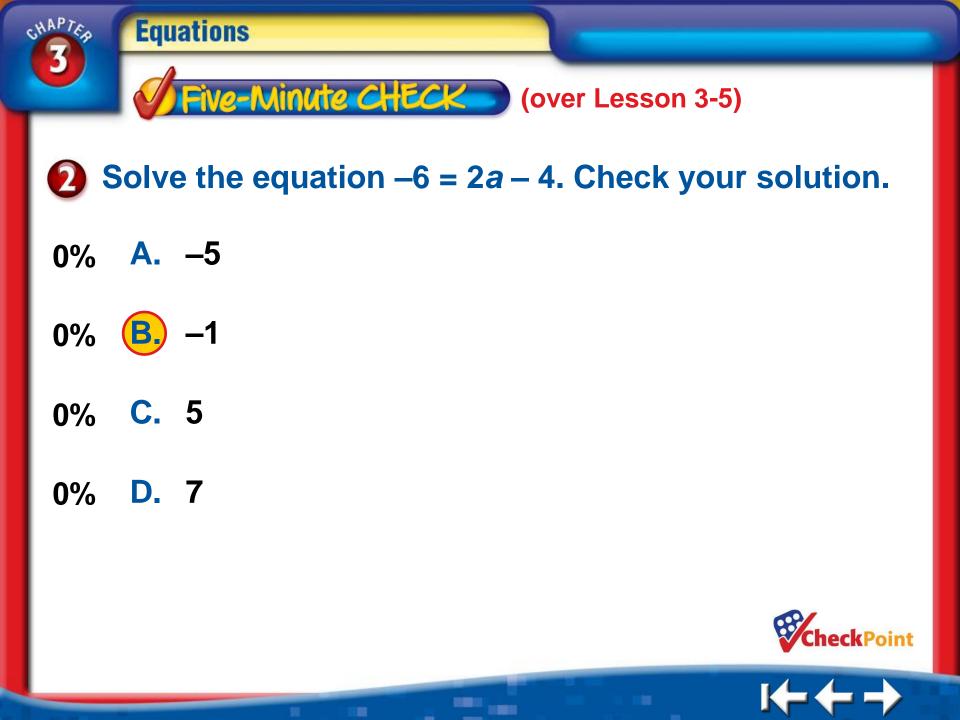


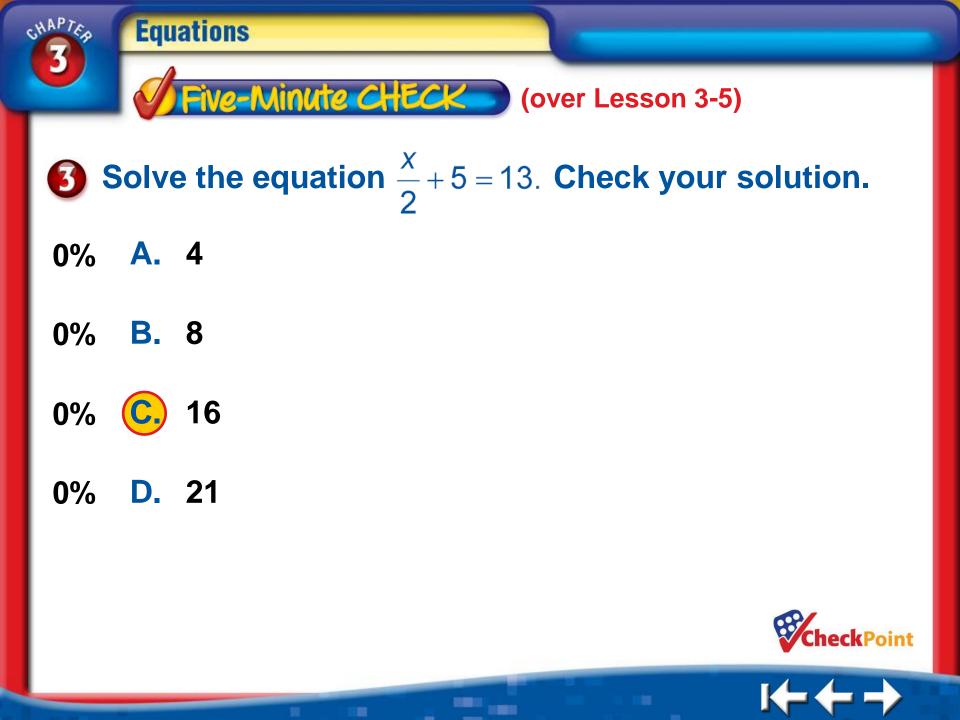


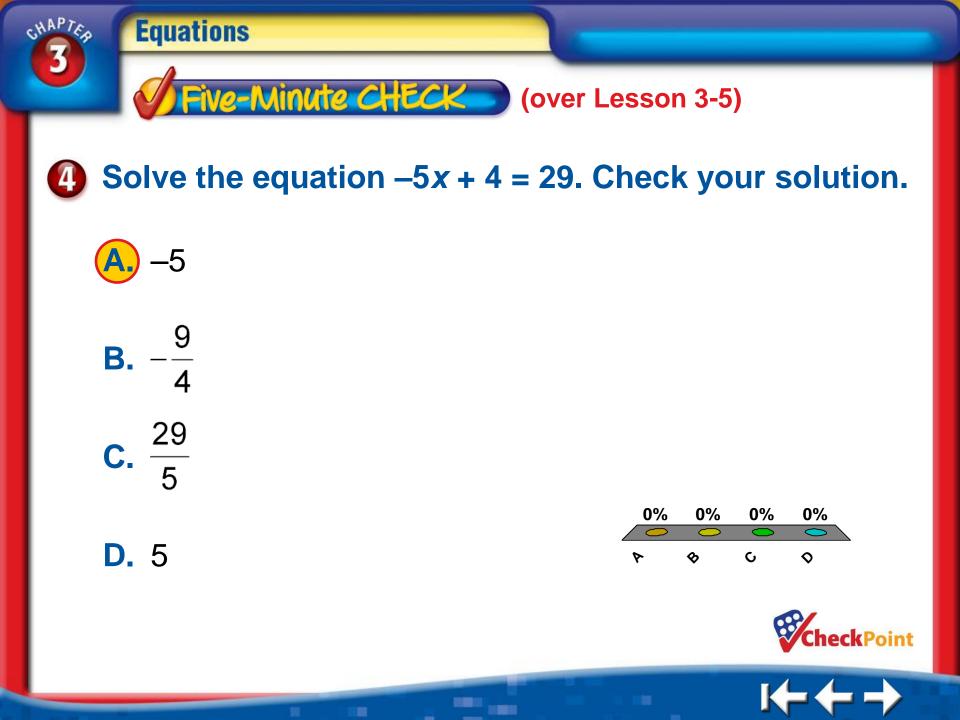


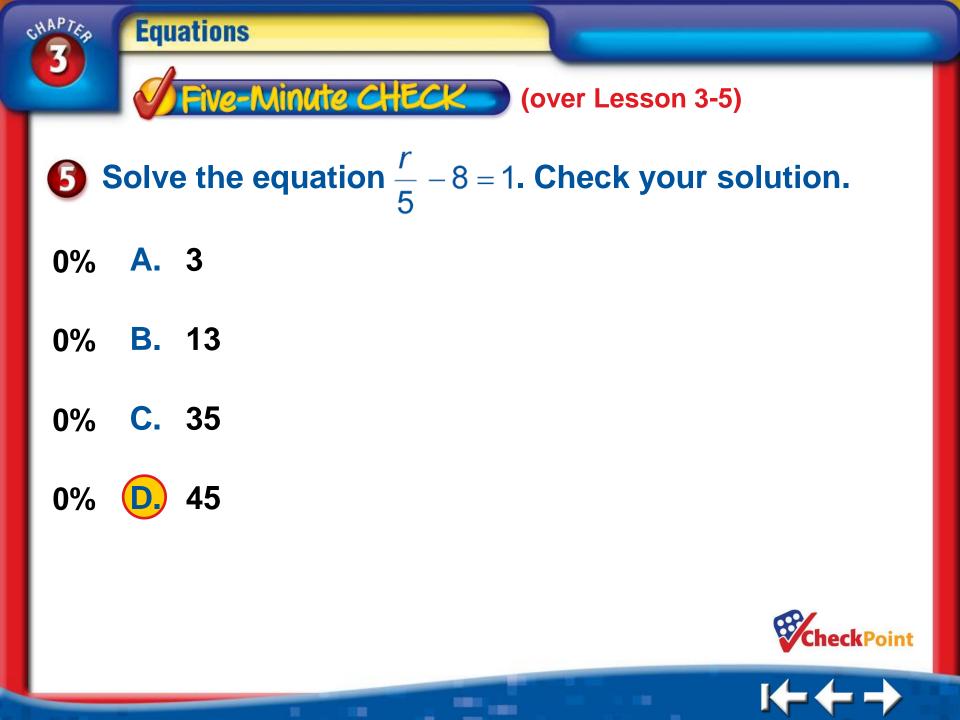














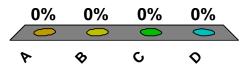
6 Which equation does *not* have a solution of –9?

A.
$$6x + 29 = -25$$

B.
$$\frac{x}{3} + 12 = 9$$

C.
$$-1 = 2x + 17$$

D.
$$5 + \frac{x}{-3} = 2$$







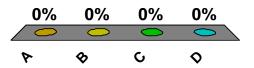


Seven more than three times a number is 34. Translate the sentence into an equation and then find the number.

B.
$$7n - 3 = 34; \frac{37}{7}$$

C.
$$7n + 3 = 34; \frac{31}{7}$$

D.
$$3(n+7) = 34; 13$$







Nine less than six times a number is 57. Translate the sentence into an equation and then find the number.

0% **B.**
$$9 - 6n = 57; -8$$

- 0% C. 9n 6 = 57; 7
- 0% **D**. 6n 9 = 57; 11







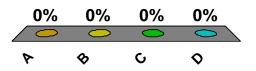
The quotient of a number and –3, less 5, is –7. Translate the sentence into an equation and then find the number.

$$(A) \frac{n}{-3} - 5 = -7; 6$$

B.
$$\frac{n-5}{-3} = -7; 36$$

C.
$$\frac{n}{-3} = -5 - 7; 6$$

D.
$$\frac{n}{-3} = -5 - 7; 36$$





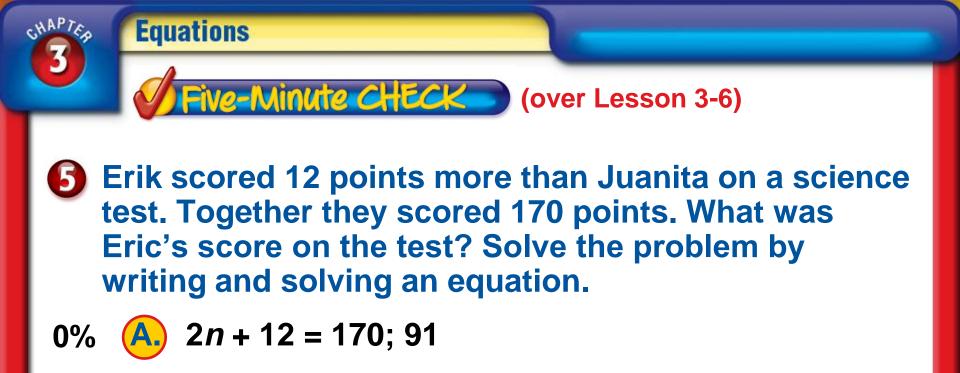




Sam sold a car for \$200 more than half the original price. If he sold the car for \$6540, what was the original price? Solve the problem by writing and solving an equation.

A.
$$6540 + 200 = \frac{n}{2}$$
; \$13,480
B. $6540 = 200 + \frac{n}{2}$; \$12,680
C. $\frac{1}{2}(n - 6540) = 200$; \$16,940
D. $n + \frac{200}{2} = 6540$; \$16,940

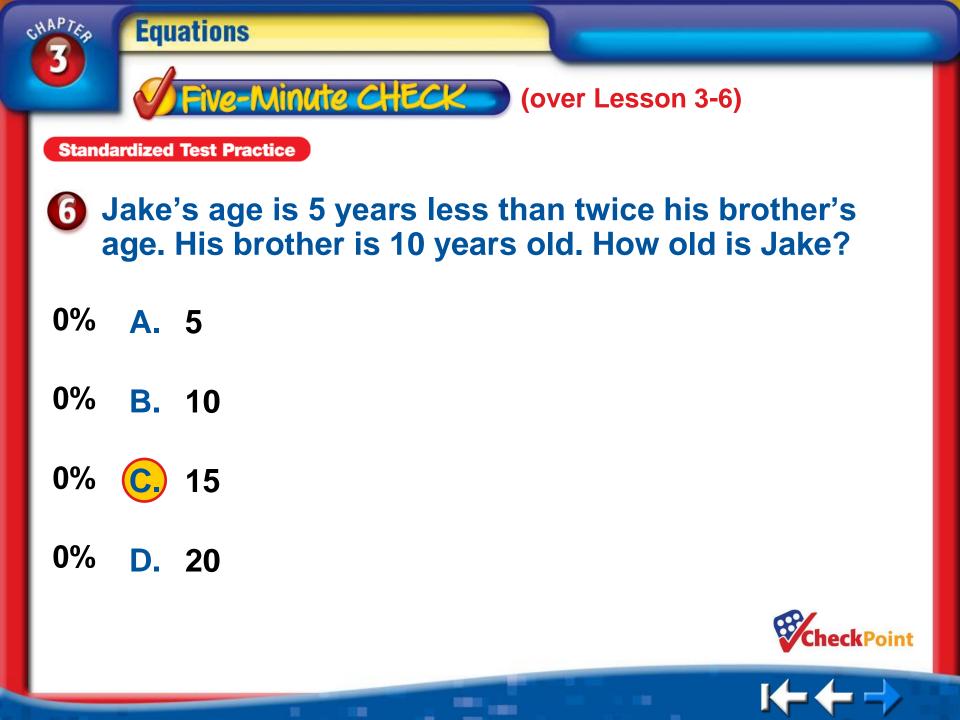




- 0% **B**. 12 + 2*n* = 170; 79
- 0% **C**. 12*n* + 2 = 170; 14

0% **D**. 12*n* + 2 = 170; 15







Describe the sequence 2, 4, 6, 8, 10, ... using words and symbols.

- 0% A The terms have a common difference of 2; t = 2n.
- **B.** The terms have a common difference of 1; t = n.
- 0% C. The terms have a common difference of 2; t=2+n.
- 0% D. The terms have a common difference of 4; t = 4n.





Describe the sequence 10, 20, 30, 40, ... using words and symbols.

- 0% A. The terms have a common difference of 10; t = 10 + n.
- 0% B. The terms have a common difference of 5; t = 5n.
- 0% C. The terms have a common difference of 10; t = 10n.
- 0% D. The terms have a common difference of 20; t = 20 + n.





Obscribe the sequence 9, 10, 11, 12, ... using words and symbols.

- 0%
- 0% 😬

Α.

- The terms have a common difference of 8, and you have to add 1 to the term number to get the term; *t* = 8*n*.
- The terms have a common difference of 1, and you have to add 8 to the term number to get the term; t = n + 8.
- 0%

0%

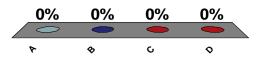
- C. The terms have a common difference of 1, and you have to add 8 to the term number to get the term; t = 8n.
- **D.** The terms have a common difference of 1; t = n.





Write the equation that describes the sequence 7, 8, 9, 10, ... Then find the 14th term of the sequence.

A.
$$t = n + 7; 21$$









Write the equation that describes the sequence 7, 10, 13, 16, ... Then find the 22nd term of the sequence.

A.
$$t = 3n + 4;70$$

C. *t* = 3*n*; 66

D. *t* = 2*n* + 4; 48

