Interactive Classroom



Chapter 6 Ratio, Proportion, and Percent

Click the mouse button or press the space bar to continue.

apra

Copyright © by The McGraw-Hill Companies, Inc.



Chapter Menu

- Lesson 6-1 Ratios and Rates
- Lesson 6-2 Proportional and Nonproportional Relationships
- Lesson 6-3 Using Proportions
- Lesson 6-4 Scale Drawings and Models
- **Lesson 6-5** Fractions, Decimals, and Percents
- Lesson 6-6 Using the Percent Proportion
- Lesson 6-7 Finding Percents Mentally
- Lesson 6-8 Using Percent Equations
- Lesson 6-9 Percent of Change
- Lesson 6-10 Using Sampling to Predict







Five-Minute Check (over Chapter 5)

Main Ideas and Vocabulary

Example 1: Write Ratios in Simplest Form

Example 2: Write Ratios as Fractions

Example 3: Compare Unit Rates

Example 4: Convert Rates





Main Ideas

• Write ratios as fractions in simplest form.

Chapter RESOURCES

• Determine unit rates.

New Vocabulary

- ratio
- rate
- unit rate



Express the ratio 10 roses out of 12 flowers as a fraction in simplest form.



Answer:

Ratios and Rates

Divide the numerator and denominator by the GCF, 2.

RESOURCES

The ratio of roses to flowers is 5 to 6. This means that for every 6 flowers, 5 of them are roses.











 $\frac{\$4.50}{12 \text{ ounces}} = \frac{\$0.38}{1 \text{ ounces}}$

Divide the numerator and denominator by 12 to get a denominator of 1.

RESOURCES

For the 12-oz bottle, the unit rate is \$0.38 per ounce.



For the 16-oz bottle, the unit rate is \$0.41 per ounce.

Answer: The 12-oz bottle has the lower cost per ounce.



- same per can.
- **D.** Cannot be determined from the given information.

Chapter RESOURCES



0%



Ratios and Rates

ANIMALS A snail moved 30 feet in 2 hours. How many inches per minute did the snail move?

You will need to convert $\frac{30 \text{ ft}}{2 \text{ hr}}$ to $\frac{\bullet \text{ in.}}{1 \text{ min}}$. There are 12 inches in 1 foot and 60 minutes in 1 hour. Write 30 feet in 2 hours as $\frac{30 \text{ ft}}{2 \text{ hr}}$.







Answer: 30 feet in 2 hours is equivalent to 3 inches per minute.





0%

C

0%

0

eckPoint

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Lesson Menu

5-2

Five-Minute Check (over Lesson 6-1)

Main Ideas and Vocabulary

Example 1: Identify Proportional Relationships

Example 2: Describe Proportional Relationships





Main Ideas

- Identify proportional and nonproportional relationships in tables and graphs.
- Describe a proportional relationship using an equation.

Chapter RESOURCES

New Vocabulary

- proportional
- nonproportional
- constant of proportionality



EXAMPLE Identify Proportional Relationships

Chapter RESOURCES

A. Determine whether the set of numbers in the pattern forms a proportion.

Baseballs	1	2	3	4
Cost (dollars)	2	3	4	5

$$\frac{1}{2}\neq\frac{2}{3}\neq\frac{3}{4}\neq\frac{4}{5}$$

Answer: no



EXAMPLE Identify Proportional Relationships

B. Determine whether the set of numbers in the pattern forms a proportion.

Time (seconds)	1	2	3	4
Distance (inches)	4	8	12	16

Write the rate of time to distance for each second in simplest form.

Chapter RESOURCES

$$\frac{1}{4} \qquad \frac{2}{8} = \frac{1}{4} \qquad \frac{3}{12} = \frac{1}{4} \qquad \frac{4}{16} = \frac{1}{4}$$

Answer: yes



CHECK Your Progress

Determine whether the set of numbers in the table are proportional. Explain your reasoning.

Passes Received	52	40	22	13
Number of Yards Gained	689	596	289	221

A. Yes, all the rates are equal to $\frac{1}{13.25}$.

B. Yes, all the rates are equal to $\frac{1}{14.9}$.

C. Yes, all the rates are equal to $\frac{1}{17}$.

No, the rates are not equal.







EXAMPLE Describe Proportional Relationships

WORK Nina charges \$5 for each day of pet sitting. Write an equation relating the cost of pet sitting to the number of days. What would be the cost of pet sitting for 4 days?

Find the constant of proportionality.

Words \$5 for each day of pet sitting

Variable Let d = number of days of pet sitting and c = total amount Nina charges.

Chapter RESOURCES

Equation c = 5d



Describe Proportional Relationships

- **2** c= 5d
 - = 5(4)

= 20

EXAMPLE

Write the equation.

Replace *d* with the number of days. Multiply.

Answer: *c* = 5*d*; \$20







MUSIC Lindsay paid \$10.89 to download an album with 11 songs. Write an equation relating cost to the number of songs downloaded. How much would an album of 13 songs cost?

A. The cost *c* is related to the number of songs *s* by the equation *c* = 0.99*s*. An album of 13 songs would cost \$12.87.

HECK Your Progress

- B. The cost *c* is related to the number of songs *s* by the equation *c* = 0.99*s*. An album of 13 songs would cost \$13.99.
- C. The cost c is related to the number of songs s by the equation c = 1.01 s. An album of 13 songs would cost \$13.13.
- D. The cost *c* is related to the number of songs *s* by the equation c = 1.01s. An album of 13 songs would cost \$12.12.



RESOURCES

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Five-Minute Check (over Lesson 6-2)

Main Ideas and Vocabulary

Key Concept: Proportion

Key Concept: Property of Proportions

Example 1: Solve Proportions

Example 2: Real-World Example

Example 3: Convert Measurements

Main Ideas

- Solve proportions.
- Use proportions to solve real-world problems.

Chapter RESOURCES

New Vocabulary

- proportion
- cross products

KEY CONCEPT

6-3

Proportion

Word A proportion is an equation stating that two ratios or rates are equal.

Symbols
$$\frac{a}{b} = \frac{c}{d}$$
 Example $\frac{2}{3} = \frac{6}{9}$





KEY CONCEPT

6-3

Property of Proportions

Chapter RESOURCES Words The cross products of a proportion are equal.

Symbols If
$$\frac{a}{b} = \frac{c}{d'}$$
 then $ad = bc$. If $ad = bc$, then $\frac{a}{b} = \frac{c}{d'}$.



Answer: The solution is 21.6.

EXAMPLE Solve Proportions **B.** Solve the proportion $\frac{16}{v} = \frac{4.8}{1.5}$. **16** 4.8 $\overline{v} = \frac{1.5}{1.5}$ $16 \bullet 1.5 = 4.8 \bullet V$ **Cross products** Multiply. 24 = 4.8v24 4.8v Divide. $\frac{1}{4.8} = \frac{1}{4.8}$ 5 = v**Answer:** The solution is 5.

> Chapter RESOURCES

Using Proportions







Real-World EXAMPLE

2 ARCHITECTURE An architect builds a model of a building before the actual building is built. The model is 8 inches tall and the actual building will be 22 feet tall. The model is 20 inches wide. Find the width of the actual building.

- **Explore** You know the actual height of the building and the corresponding height of the model. You need to find the actual width of the building that corresponds with a model width of 20 inches.
- Plan Write and solve a proportion using ratios that compare the actual building to the model. Let *w* represent the actual width of the building.





actual height actual width Solve 2 model height model width 22 W Write a proportion. 8 20 $22 \bullet 20 = 8 \bullet W$ **Cross products** 440 = 8wMultiply. 440 8*w* Divide. 8 8 55 = WSimplify.








Using Proportions

Real-World EXAMPLE Convert Measurements

ATTRACTIONS The Circleville Pumpkin Show in Circleville, Ohio, boasts the world's largest pumpkin pie. The pie weighs 350 pounds and is 5 feet in diameter. Find the diameter of the pie in centimeters if 1 foot = 30.48 centimeters.

Let x represent the diameter in centimeters.

customary measurement $\rightarrow 1 \text{ ft}$ metric measurement $\rightarrow 30.48 \text{ cm} = \frac{5 \text{ ft}}{x \text{ cm}} \leftarrow \text{customary measurement} \leftarrow \text{metric measurement}$

 $1 \bullet x = 30.48 \bullet 5$ Cross products

Chapter RESOURCES

x = 152.4 Simplify.

Answer: The diameter of the pie is 152.4 centimeters.



0%

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Lesson Menu

3-4

Five-Minute Check (over Lesson 6-3)

Main Ideas and Vocabulary

Example 1: Find Actual Measurements

Example 2: Determine the Scale

Example 3: Construct a Scale Drawing





Main Ideas

- Use scale drawings.
- Construct scale drawings.

Chapter RESOURCES

New Vocabulary

- scale drawing
- scale model
- scale
- scale factor



Real-World EXAMPLE Find Actual Measurements

MAP A map has a scale of 1 inch = 8 miles. Two towns are 3.25 inches apart on the map. What is the actual distance between the two towns?

Method 1 Use a proportion.

Let *x* represent the actual distance between the two towns. Write and solve a proportion.

 $\begin{array}{l} \text{map distance} \rightarrow \\ \text{actual distance} \rightarrow \\ \hline 1 \text{ inch} \\ 8 \text{ miles} \\ \hline \\ x \text{ actual distance} \\ \hline \\ x \text{ actual distance} \\ \hline \\ x = 26 \\ \hline \\ x \text{ miles} \\ \hline \\ x = 26 \\ \hline \\ x \text{ miles} \\ \hline \\ x \text{ miles} \\ \hline \\ x \text{ actual distance} \\ \hline \\ x \text{ miles} \\ \hline x \text{ miles} \\ x$











Scale Drawings and Models

CHECK Your Progress

SCALE DRAWING A scale drawing of a new house has a scale of 1 inch = 4 feet. The height of the living room ceiling is 2.75 inches on the scale drawing. What is the actual height of the ceiling?

- A. 1.45 feet
- **B.** 48 feet



D. 6.88 feet





Scale Drawings and Models

Real-World EXAMPLE Determine the Scale

MODEL CAR A model car is 4 inches long. The actual car is 12 feet long. What is the scale of the model?

Write the ratio of the length of the model to the actual length of the car. Then solve a proportion in which the length of the model is 1 inch and the actual length is x feet.

 $\begin{array}{ll} \text{model length} \rightarrow & \frac{4 \text{ inches}}{12 \text{ feet}} = \frac{1 \text{ inch}}{x \text{ feet}} \leftarrow \text{model length} \\ \leftarrow \text{actual length} \end{array}$

 $4 \bullet x = 12 \bullet 1$ Find the cross products.

Chapter RESOURCES

4x = 12 Simplify.



Answer: The scale is 1 inch = 3 feet.







Scale Drawings and Models

CHECK Your Progress

2 LOG CABIN A model log cabin is 12 inches high. The actual log cabin is 42 feet high. What is the scale of the model?

0%

🗖 A 🗆 B 🗖 C 🗖 D

- 1 inch = 3.5 feet
- **B.** 1 inch = 42 feet
- C. 2 inches = 7 feet
- **D.** 1 inch = 3.5 inches



Real-World EXAMPLE Construct a Scale Drawing

PATIO DESIGN Sheila is designing a patio that is 16 feet long and 14 feet wide. Make a scale drawing of the patio. Use a scale of 0.5 inch = 4 feet.

Step 1 Find the measure of the patio's length on the drawing. Let *x* represent the length.

 $\begin{array}{l} \text{drawing length} \rightarrow & \underline{0.5 \text{ inch}} \\ \text{actual length} \rightarrow & \overline{4 \text{ feet}} \end{array} = & \frac{x \text{ inches}}{16 \text{ feet}} & \leftarrow \text{drawing length} \\ & \leftarrow \text{actual length} \end{array}$

- $0.5 \bullet 16 = 4 \bullet x$ Find the cross products.
 - 8 = 4x Simplify.
 - 2 = x Divide each side by 4.





On the drawing, the width is 1.75 or $1\frac{3}{4}$ inches.











Enclosible Lesson Click the mouse button to return to the

Chapter Menu.





Lesson Menu

Five-Minute Check (over Lesson 6-4)

Main Ideas and Vocabulary

Example 1: Percents as Fractions

Example 2: Fractions as Percents

Key Concept: Percents and Decimals

Example 3: Percents as Decimals

Example 4: Decimals as Percents

Example 5: Fractions as Percents

Chapter RESOURCES

Example 6: Compare Numbers

Main Ideas

- Express percents as fractions and vice versa.
- Express percents as decimals and vice versa.

New Vocabulary

percent







EXAMPLE Percents as Fractions

A. Express 40% as a fraction in simplest form.

$$40\% = \frac{40}{100}$$
$$= \frac{2}{5}$$
Answer: $\frac{2}{5}$





EXAMPLE Percents as Fractions

B. Express 104% as a fraction in simplest form.

Chapter RESOURCES
$$104\% = \frac{104}{100}$$

$$=\frac{26}{25}$$
 or $1\frac{1}{25}$

Answer:
$$\frac{26}{25}$$
 or $1\frac{1}{25}$





EXAMPLE Percents as Fractions

D. Express $56\frac{1}{4}\%$ as a fraction in simplest form.

$$56\frac{1}{4}\% = \frac{56\frac{1}{4}}{100}$$

$$= 56 \frac{1}{4} \div 100$$

Answer:
$$\frac{9}{16}$$











EXAMPLE Fractions as Percents

2 A. Express $\frac{19}{20}$ as a percent.

$$\frac{19}{20} = \frac{95}{100} \text{ or } 95\%$$

Answer: 95%







Answer: 160%











KEY CONCEPT

Percents and Decimals

- To write a percent as a decimal, divide by 100 and remove the percent symbol.
- To write a decimal as a percent, multiply by 100 and add the percent symbol.







EXAMPLE Percents as Decimals

A. Express 60% as a decimal.

60% = 60% Divide by 100 and remove the %.

= 0.60

Answer: 0.60






Chapter RESOURCES (--)

7% = 07% Divide by 100 and remove the %.

= 0.07

Answer: 0.07



EXAMPLE Percents as Decimals

C. Express 658% as a decimal.

658% = 658% Divide by 100 and remove the %.

= 6.58

Answer: 6.58







EXAMPLE Percents as Decimals

D. Express 0.4% as a decimal.

0.4% = 00.4% Divide by 100 and remove the %. = 0.004

Chapter RESOURCES

Answer: 0.004











A. Express 0.4 as a percent.

0.4 = 0.40 Multiply by 100 and add the %.

Chapter RESOURCES

= 40%

Answer: 40%



B. Express 0.05 as a percent.

0.05 = 0.05 Multiply by 100 and add the %. = 5%

Chapter RESOURCES

Answer: 5%



C. Express 0.0008 as a percent.

0.0008 = 0.0008

Multiply by 100 and add the %.

Chapter RESOURCES

= 0.08%

Answer: 0.08%



EXAMPLE Decimals as Percents

D. Express 7.3 as a percent.

7.3 = 7.30 Multiply by 100 and add the %.

Chapter RESOURCES

= 730%

Answer: 730%











EXAMPLE Fractions as Percents

6 A. Express $\frac{5}{8}$ as a percent. Round to the nearest tenth percent, if necessary.

Chapter RESOURCES

$$\frac{5}{8} = 0.625$$

= 62.5%

Answer: 62.5%



B. Express $\frac{1}{3}$ as a percent. Round to the nearest tenth percent, if necessary.

Chapter RESOURCES

$$\frac{1}{3} = 0.333333...$$
≈ 33.3%

Answer: 33.3%



Chapter RESOURCES

$\frac{9}{1000} = 0.009$ = 0.9%

Answer: 0.9%



EXAMPLE Fractions as Percents

5 D. Express $\frac{23}{14}$ as a percent. Round to the nearest

Chapter RESOURCES

tenth percent, if necessary.

 $\frac{23}{14} \approx 1.6428571$

≈ 164.3%

Answer: 164.3%



HECK Your Progress

6 A. Express $\frac{3}{8}$ as a percent. Round to the nearest tenth percent, if necessary.

- A. 3.8%
- <mark>B.</mark> 37.5%
- **C.** 0.375%

D. 380%





HECK Your Progress

B. Express $\frac{5}{12}$ as a percent. Round to the nearest tenth percent, if necessary.

A. 512%
B. 0.417%
C. 41.7%
D. 5.12%





CHECK Your Progress

C. Express $\frac{13}{1000}$ as a percent. Round to the nearest tenth percent, if necessary.

- <mark>A.</mark> 1.3%
- **B.** 13%
- **C.** 13.1%
- **D.** 0.13%





CHECK Your Progress

D. Express $\frac{21}{17}$ as a percent. Round to the nearest tenth percent, if necessary.

- A. 21.17%B. 123.5%
- **C.** 2117%

D. 1.235%





Real-World EXAMPLE Compare Numbers

BAKERY A baker said that 25% of his customers buy only bread and $\frac{2}{5}$ of his customers buy only cookies. Which group is larger?

Write $\frac{2}{5}$ as a percent. Then compare.

 $\frac{2}{5} = 0.40$ or 40%

Answer: Since 40% is greater than 25%, the group that buys only cookies is larger.

Chapter RESOURCES



SCHOOL The school principal states that $\frac{3}{9}$ of the

students are involved in instrumental music while 42% are involved in vocal music. Which group is larger?



- **B.** instrumental music
- **C.** the groups are equal in size
- **D.** cannot be determined



Enclosible Lesson Click the mouse button to return to the

Chapter Menu.





Lesson Menu

6-6

Five-Minute Check (over Lesson 6-5)

Main Idea and Vocabulary

Key Concept: Percent Proportion

Example 1: Find the Percent

Example 2: Find the Part

Example 3: Find the Whole

Example 4: Apply the Percent Proportion

Concept Summary: Types of Percent Problems

Chapter RESOURCES



Main Idea

6-6

• Use the percent proportion to solve problems.

Chapter RESOURCES

New Vocabulary

percent proportion











EXAMPLE Find the Percent

A. Twenty is what percent of 25?

Twenty is being compared to 25. So, 20 is the part and 25 is the whole. Let *n* represent the percent.

$$\frac{20}{25} = \frac{n}{100}$$
 Write the percent proportion.

Chapter RESOURCES

 $20 \bullet 100 = 25 \bullet n$ Find the cross products.

2000 = 25n Simplify.



25n

25

EXAMPLE Find the Percent



6-6

Divide each side by 25.

Chapter RESOURCES $\leftarrow \rightarrow$

80 = n Simplify.

Answer: 20 is 80% of 25.



EXAMPLE Find the Percent

B. What percent of 8 is 12?

Twelve is being compared to 8. So, 12 is the part and 8 is the whole. Let *n* represent the percent.

<u>12 _ n</u>	Write the percent proportion
8 100	

Chapter RESOURCES

 $12 \bullet 100 = 8 \bullet n$ Find the cross products.

1200 = 8n Simplify.



8

EXAMPLE Find the Percent

1200 8*n*

8

6-6

Divide each side by 8.

Chapter RESOURCES

←→

150 *= n* Simplify.

Answer: 150% of 8 is 12.







EXAMPLE Find the Part

What number is 8.8% of 20?

The percent is 8.8, and the whole is 20. Let *n* represent the part.

$\frac{n}{20} = \frac{8.8}{100}$	Write the percent proportion
<i>n</i> • 100 = 20 • 8.8	Find the cross products.
100 <i>n</i> = 176	Simplify.
<i>n</i> = 1.76	Mentally divide each side by 100.

Chapter RESOURCES

Answer: 8.8% of 20 is 1.76.




EXAMPLE Find the Whole

Seventy is 28% of what number?

The percent is 28%, and the part is 70. Let *n* represent the whole.

$\frac{70}{n} = \frac{28}{100}$	Write the percent proportion.	
70 • 100 = <i>n</i> • 28	Find the cross products.	
7000 = 28n	Simplify.	





EXAMPLE Find the Whole

 $3 \quad \frac{7000}{28} = \frac{28n}{28}$

6-6

Divide each side by 28.

250 = n Simplify.

Answer: 70 is 28% of 250.









Real-World EXAMPLE Apply the Percent Proportion

TENNIS From the years 1999 through 2005, Serena Williams won the U.S. Open Tennis Championships two times and Wimbledon two times. What percent of both tournaments combined during those years was Serena Williams the women's champion? Round to the nearest tenth.

Compare the number of Serena Williams' wins, 4, to the total number of tournaments played, 14. The part is 4 and the whole is 14. Let *n* represent the percent.

6-6	Using the Percent Prop	ortion
I	Real-World EXAMPLE	Apply the Percent Proportion
4	$\frac{4}{14} = \frac{n}{100}$	
	4 • 100 = 14 • <i>n</i>	Find the cross products.
	400 = 14 <i>n</i>	Simplify.
	$\frac{400}{14} = \frac{14n}{14}$	Divide each side by 14.
	28.6 ≈ <i>n</i>	Simplify.
Answer: Serena Williams won about 28.6% of the		

tournaments.

ath Ne



HECK Your Progress

BAKE SALE At the school bake sale, 23 chocolate chip cookies, 18 oatmeal raisin cookies, and 7 peanut butter cookies were sold. If the sale started with a total of 90 cookies, what percent of the cookies were sold?

- <mark>A.</mark> 53.3%
- **B.** 7.8%
- **C.** 1.9%
- **D.** 48%



CONCEPT SUMMARY

Types of Percent Problems

		and the second
Туре	Example	Proportion
Find the Percent	3 is <u>what percent</u> of 4? or <u>What</u> <u>percent</u> of 4 is 3?	$\frac{3}{4} = \frac{n}{100}$
Find the Part	What number is 75% of 4?	$\frac{n}{4} = \frac{75}{100}$
Find the Whole	3 is 75% of <u>what number?</u>	$\frac{3}{n} = \frac{75}{100}$





Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Lesson Menu

Five-Minute Check (over Lesson 6-6)

Main Ideas

Concept Summary: Percent-Fraction Equivalents

Example 1: Find Percent of a Number Mentally

Example 2: Estimate Percents

Example 3: Real-World Example





Main Ideas

6-7

- Compute mentally with percents.
- Estimate with percents.





6-7

CONCEPT S	JMMARY	Percent-Fraction Equivalents		
$20\% = \frac{1}{5}$	$10\% = \frac{1}{10}$	$25\% = \frac{1}{4}$	$12\frac{1}{2}\% = \frac{1}{8}$	$16\frac{2}{3}\% = \frac{1}{6}$
$40\% = \frac{2}{5}$	$30\% = \frac{3}{10}$	$50\% = \frac{1}{2}$	$37\frac{1}{2}\% = \frac{3}{8}$	$33\frac{1}{3}\% = \frac{1}{3}$
$60\% = \frac{3}{5}$	$70\% = \frac{7}{10}$	$75\% = \frac{3}{4}$	$62\frac{1}{2}\% = \frac{5}{8}$	$66\frac{2}{3}\% = \frac{2}{3}$
$80\% = \frac{4}{5}$	$90\% = \frac{9}{10}$		$87\frac{1}{2}\% = \frac{7}{8}$	$83\frac{1}{3}\% = \frac{5}{6}$



Math Nine



EXAMPLE Find Percent of a Number Mentally

Chapter RESOURCES

A. Find 50% of 46 mentally.

50% of $46 = \frac{1}{2}$ of 46 Think: $50\% = \frac{1}{2}$. = 23 Think: $\frac{1}{2}$ of 46 is 23.

Answer: 50% of 46 is 23.



EXAMPLE Find Percent of a Number Mentally

Chapter RESOURCES

B. Find 25% of 88 mentally.

25% of 88 = $\frac{1}{4}$ of 88 Think: $25\% = \frac{1}{4}$. = 22 Think: $\frac{1}{4}$ of 88 is 22.

Answer: 25% of 88 is 22.



6-7

EXAMPLE Find Percent of a Number Mentally

C. Find 70% of 110 mentally.

70% of
$$110 = \frac{7}{10}$$
 of 110 Think: $70\% = \frac{7}{10}$.
= 77 Think: $\frac{1}{10}$ of 110 is 11.
So, $\frac{7}{10}$ of 110 is 77.

Chapter RESOURCES **i← ← →**

Answer: 70% of 110 is 77.









EXAMPLE Estimate Percents

2 A. Estimate 22% of 494.

22% is about 20% or $\frac{1}{5}$.

494 is about 500.

```
\frac{1}{5} of 500 is 100.
```

Answer: 22% of 494 is about 100.



6-7

EXAMPLE Estimate Percents

B. Estimate
$$\frac{1}{4}$$
% of 1219.
 $\frac{1}{4}$ % = $\frac{1}{4}$ ×1%. 1219 is about 1200.

1% of 1200 is 12.

Answer:
$$\frac{1}{4}$$
% of 1219 is about $\frac{1}{4}$ × 12 or 3.





EXAMPLE Estimate Percents

2 C. Estimate 155% of 38.

155% means about 150 for every 100 or about 15 for every 10.

Chapter RESOURCES

38 has about 4 tens.

 $15 \times 4 = 60$

Answer: 155% of 38 is about 60.









Real-World EXAMPLE

3 MONEY A restaurant bill totals \$21.35. You want to leave a 15% tip. What is a reasonable amount for the tip?

\$21.35 is about \$21.

15% = 10% + 5%

10% of \$21 is \$2.10 Move the c

Move the decimal point 1 place to the left.

Chapter RESOURCES

5% of \$21 is \$1.05 5% is one half of 10%.

So, 15% is about \$2.10 + \$1.05 or \$3.15.

Answer: A reasonable amount for the tip would be \$3.



0%

🗖 A 🗖 B 🗖 C 🗖 D



Enclosible Lesson Click the mouse button to return to the

Chapter Menu.





Lesson Menu

6-8

Five-Minute Check (over Lesson 6-7)

Main Ideas and Vocabulary

Concept Summary: The Percent Equation

Example 1: Find the Part

Example 2: Find the Percent

Example 3: Find the Whole

Example 4: Find Discount

Example 5: Apply Simple Interest Formula

Main Ideas

• Solve percent problems using percent equations.

Chapter RESOURCES

• Solve real-life problems involving discount and interest.

New Vocabulary

- percent equation
- discount
- interest

6-8

CONCEPT SUMMA	The Percent Equation	
Туре	Example	Equation
Missing Part	What number is 75% of 4?	n = 0.75(4)
Missing Percent	3 is what percent of 4?	3 = n(4)
Missing Whole	3 is 75% of what number?	3 = 0.75 <i>n</i>

Chapter RESOURCES

Math







EXAMPLE Find the Percent

2 19 is what percent of 25?

Estimate:

$$\frac{19}{25} \approx \frac{4}{5}$$
, which is 80%.

Chapter RESOURCES

You know that the whole is 25 and the part is 19. Let *n* represent the percent.

19 *= n*(25)

 $\frac{19}{25} = n$

Divide each side by 25.



Answer: 19 is 76% of 25

The answer makes sense compared to the estimate.

┝╴←╺→





You know that the part is 84 and the percent is 16%. Let *n* represent the base.

Chapter RESOURCES

84 = 0.16n Write 16% as the decimal 0.16.

 $\frac{84}{0.16} = \frac{0.16n}{0.16}$ Divide each side by 0.16.


Answer: 84 is 16% of 525. The answer is reasonable since it is close to the estimate.







Using Percent Equations

Real-World EXAMPLE Find Discount

JEWELRY The regular price of a ring is \$495. It is on sale at a 20% discount. What is the sale price of the ring?

Method 1 First, use the percent equation to find 20% of 495.

Estimate :
$$\frac{1}{5}$$
 of 500 = 100

Chapter RESOURCES

Let *d* represent the discount.

d = 0.20(495) The whole is 495 and the percent is 20. = 99 Simplify.



495 – 99 = 396 Subtract the discount from the original price.

Method 2

A discount of 20% means the ring will cost 100%–20% or 80% of the original price. Use the percent equation to find 80% of 495.

Chapter RESOURCES

Let s represent the sale price.



Answer: The sale price of the ring will be \$396.

















Answer: It will take 5.5 years to earn \$495.





B. 55 years



D. 0.4 years



Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Five-Minute Check (over Lesson 6-8)

Main Ideas and Vocabulary

Example 1: Find Percent of Change

Example 2: Find Percent of Increase

Example 3: Standardized Test Example

Example 4: Find Percent of Decrease



Main Ideas

- Find percent of increase.
- Find percent of decrease.

New Vocabulary

- percent of change
- percent of increase
- percent of decrease

EXAMPLE Find Percent of Change

Percent of Change

Find the percent of change from 325 to 390.

- **Step 1** Subtract to find the amount of change. 390 - 325 = 65 new amount – original amount
- **Step 2** Write a ratio that compares the amount of change to the original amount. Express the ratio as a percent.

 $percent of change = \frac{amount of change}{original amount}$

 $=\frac{65}{325}$

Substitution.



Answer: The percent of change from 325 to 390 is 20%.









- daughter went to the same school, the tuition was \$25,500. Find the percent of change.
 - **Step 1** Subtract to find the amount of change.
 - 25,500 7500 = 18,000 new tuition original tuition
 - **Step 2** Write a ratio that compares the amount of change to the original tuition. Express the ratio as a percent.

percent of change = $\frac{\text{amount of change}}{\text{original tuition}}$



Answer: The percent of change is 240%. In this case, the percent of change is a percent of increase.



a percent.



Percent of Change

Standardized Test EXAMPLE

3 Refer to the table shown. Which city had the least percent of increase in population from 1990 to 2000?

City	1990	2004
Anaheim	266,406	333,776
Burbank	93,643	104,114
Monterey	31,954	29,669
San Jose	782,248	904,522

Source: U.S. Census Bureau

A Anaheim C Monterey

- B Burbank
- D San Jose



Percent of Change

Standardized Test EXAMPLE

Read the Test Item

Percent of increase tells how much the population has increased in relation to 1990.

Solve the Test Item

Use a ratio to find each percent of increase. Then compare the percents.







• Burbank

 $\frac{104,114 - 93,643}{93,643} = \frac{10,471}{93,643} \approx 0.1118 \text{ or } 11.2\%$



 $\frac{522 - 782,248}{782,248} = \frac{122,274}{782,248} \approx 0.1563 \text{ or } 15.6\%$

Answer: Burbank had the least percent of increase in population from 1990 to 2004. The answer is B.



The table shows test scores on the first two math tests of the semester for four students. Which student had the greatest percent of increase from test 1 to test 2?

Student	Test 1 Score	Test 2 Score
Holly	84	91
Ben	93	89
Sally	65	79
Max	73	98

A. HollyC. Sally



🗖 A 🗖 B 🗖 C 🗖 D

Chapter RESOURCES 0%







Answer: The percent of change is –20%. In this case, the percent of change is a percent of decrease.



0%

ଡ

0%

C

0%

0

ckPoint

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Lesson Menu

Five-Minute Check (over Lesson 6-9)

Main Ideas and Vocabulary

Concept Summary: Unbiased Samples

Concept Summary: Biased Samples

Example 1: Identify and Describe Samples

Example 2: Use Sampling to Predict





Main Ideas

5-10

- Identify various sampling techniques.
- Determine the validity of a sample and predict the actions of a larger group.

New Vocabulary

- sample
- population
- unbiased sample
- simple random sample
- stratified random sample

- systematic random sample
- biased sample

- convenience sample
- voluntary response sample

CONCEPT SUMMARY Unbiased Sa		
Туре	Definition	Example
Simple Random Sample	a sample where each item or person in a population is as likely to be chosen as any other	Thirty student ID numbers are randomly selected by a computer.
Stratified Random Sample	a sample in which the population is divided into similar, nonoverlapping groups. A simple random sample is then selected from each group.	Five students are chosen with birthdays in the same month, for each of the 12 months.
Systematic Random Sample	a sample in which the items or people are selected according to a specific time or item interval	Every 20 minutes a customer is chosen. or Every 10th customer in line is chosen.

CONCEPT S	UMMARY	Biased Samples
Туре	Definition	Example
Convenience Sample	a sample which includes members of the population that are easily accessed	City council surveys residents within 1-mile of a park whether to add a recreation center to the park.
Voluntary Response Sample	a sample which involves only those who want to participate in the sampling	The school board sent an email to graduating seniors asking them where to hold commencement. Seniors are asked to vote through an online poll.







EXAMPLE Identify and Describe Samples

A. Mr. Ackerman needs several volunteers to collect homework before each class. He randomly calls out a color and whoever is wearing that color is chosen. Identify this sample as biased or unbiased and describe its type.

Answer: unbiased, stratified random sample.





EXAMPLE Identify and Describe Samples

B. A hardware store wants feedback on their products and service. They include a telephone number on each receipt so customers can voluntarily call and participate.

Answer: biased, both voluntary and convenience





Using Sampling to Predict



- To determine the leading candidate for governor, all of the registered voters in one district are called and asked who they favor. Is the sample biased or unbiased? Describe its type.
 - A. unbiased; simple random sample
 - B. unbiased; systematic random sample
 - C. biased; convenience sample
 - D. biased; voluntary response sample





Using Sampling to Predict

Real-World EXAMPLE Using Sampling to Predict

A. SPORTS Miss Newman surveyed every tenth student in the hallway to see which sports they preferred watching. 44% preferred football, 28% basketball, 20% soccer, and 8% tennis. Is this sampling method valid? If so, out of 560 students in the entire school, how many would you expect to say they preferred watching basketball?

This is an unbiased, systematic random sample since Miss Newman selected students according to a specific interval. So, this sampling method is valid. Since 28% of those surveyed preferred watching basketball, to find how many would say they preferred watching basketball in the entire school, find 28% of 560.




Using Sampling to Predict

Real-World EXAMPLE Using Sampling to Predict

B. MUSIC A middle school planned to play music during lunch. Fifty students were randomly surveyed and asked what type of music they preferred. Sixteen said they wanted country music. Is this sampling method valid? If there were 535 students, how many would you expect to prefer country music?

Answer: yes; 171 students







Using Sampling to Predict

CHECK Your Progress

- A. COLORS To determine favorite colors, students wearing either blue or red were surveyed. 32% preferred blue, 29% preferred red, 23% preferred yellow, and 16% preferred green. Is this sampling method valid? If so, out of 450 students in the entire school, how many would you expect to say they prefer red?
 - A. yes; 144 students
 - **B.** yes; 29 students
 - C. yes; 131 students
 - D no; invalid sample





Using Sampling to Predict

CHECK Your Progress

B. EDUCATION The board of a school system consisting of 22 elementary schools, 6 middle schools and 4 high schools is considering three possible weeks for spring break for the upcoming school year. The board surveyed three randomly-chosen teachers from each school. Of the teachers surveyed, 84 chose the first week of April. Is this sampling method valid? If so, about how many of the 848 teachers in the school district would choose the first week of April?

- A. The survey is invalid because this is a convenience sample.
- B. The survey is invalid because this is a voluntary response sample.
- C. The survey is valid because this is a simple random sample. Of all the teachers, 106 would choose the first week of April.
- D. The survey is valid because this is a stratified random sample. Of all the teachers, 742 would choose the first week of April.



RESOURCES

Enclosible Lesson Click the mouse button to return to the

Chapter Menu.







Ratio, Proportion, and Percent

Chapter Resources Menu



CheckPoint Five-Minute Checks



Image Bank





C^Oncepts in MOtion

Animation Using a Percent Model

Interactive + Probability





Ratio, Proportion, and Percent

Lesson 6-1 (over Chapter 5)

Five-Minute CHECK

Lesson 6-2 (over Lesson 6-1)

Lesson 6-3 (over Lesson 6-2)

Lesson 6-4 (over Lesson 6-3)

Lesson 6-5 (over Lesson 6-4)

Lesson 6-6 (over Lesson 6-5)

Lesson 6-7 (over Lesson 6-6)

Lesson 6-8 (over Lesson 6-7)

Lesson 6-9 (over Lesson 6-8)

Lesson 6-10 (over Lesson 6-9)



Image Bank

To use the images that are on the following three slides in your own presentation:

- **1.** Exit this presentation.
- 2. Open a chapter presentation using a full installation of Microsoft[®] PowerPoint[®] in editing mode and scroll to the Image Bank slides.
- **3.** Select an image, copy it, and paste it into your presentation.













Ratio, Proportion, and Percent

Concepts in Motion Animation













greater fraction of boys has a pet.







6 Which statement is true about {6, 2, 7, 3, 4, 6, 2, 4, 2}?

- A. The mean and the mode are the same number.
- **B.** The median and the mode are the name number.
- C. The mean and the median are the same number.
- D. The median, the mean, and the mode are different numbers.



0%

🗖 A 🗖 B 🗖 C 🗖 D









Express the ratio as a unit rate. Round to the nearest tenth, if necessary. 230 miles in 4.5 hours

- A. 0.5 mi/h
- B. 5.1 mi/h
- **C.** 50 mi/h



🗖 A 🗖 B 🗖 C 🗖 D







Express the ratio as a unit rate. Round to the nearest tenth, if necessary. 54 pages in 30 minutes



- **B.** 1.5 pages/min
- C. 0.8 pages/min
- D. 0.5 pages/min







6 What is the cost per pound for a 20-ounce box of cereal that sells for \$4.50?







D. \$5.63

🗖 A 🗆 B 🗖 C 🗖 D







Determine whether the sets of numbers in the table are proportional.











Determine whether the sets of numbers in the table are proportional.





B. no







A deli sells 3 pounds of sliced meat for \$20.85. Write an equation relating cost *c* to the number of pounds *p* of meat.

$$(A) \quad c = 6.95p$$

B.
$$p = 6.95c$$

- **C.** c = 0.695p
- **D.** p = 0.695c









A deli sells 3 pounds of sliced meat for \$20.85. How much is 5 pounds of meat?

- A. \$30.00
- **B.** \$32.50



D. \$35.00





- **B.** 30 revolutions in 45 minutes
- **C.** 35 revolutions in 50 minutes
- **D.** 40 revolutions in 55 minutes











Write a proportion that could be used to solve for the variable and then solve. 18 donuts in 3 boxes, 30 donuts in *b* boxes

(A)
$$\frac{18}{3} = \frac{30}{b}; 5$$

B. $\frac{18}{3} = \frac{b}{30}; 6$
C. $\frac{3}{18} = \frac{30}{b}; 6$
D. $\frac{18}{3} = \frac{b}{30}; 5$

0%







Write a proportion that could be used to solve for the variable and then solve. 5 pounds of meat for \$17.45, p pounds of meat for \$10.47

A.
$$\frac{5}{17.5} = \frac{10.47}{p}$$
; 5
B. $\frac{5}{p} = \frac{17.45}{10.47}$; 5
C. $\frac{5}{p} = \frac{10.47}{17.45}$; 3
D. $\frac{5}{17.45} = \frac{p}{10.47}$; 3

0%	0%	0%	0%
	\bigcirc	\bigcirc	
P	\$	C	\diamond
CheckPoint			





There are approximately 2.54 centimeters in 1 inch. Write a proportion that could be used to find the length, in inches, of a meter stick (100 centimeters). What is the length, in inches, of a meter stick?

(A)
$$\frac{2.54}{1} = \frac{100}{x}$$
; 39.37 in.
B. $\frac{1}{2.54} = \frac{100}{x}$; 254 in.
C. $\frac{2.54}{100} = \frac{1}{x}$; 39.37 in.
D. $\frac{2.54}{1} = \frac{x}{100}$; 254 in.



Standardized Test Practice

6 There are 35 red and blue marbles in a bag. The ratio of blue marbles to red marbles is 2 to 5. Which proportion could be used to find the number of red marbles in the bag?

A.
$$\frac{2}{5} = \frac{r}{35}$$

B. $\frac{2}{7} = \frac{r}{35}$
C. $\frac{5}{7} = \frac{r}{35}$
D. $\frac{5}{35} = \frac{7}{r}$

🗖 A 🗖 B 🗖 C 🗖 D










On a map the distance between two cities is 4.5 inches. The actual distance is 270 miles. What is the scale of the map?

- **A.** 1 mile = 121.5 inches
- **B.** 1 mile = 60 inches
- **C.** 1 inch = 121.5 miles







- **6** A flower garden is 3 feet wide by 8 feet long. What
 - will be the width and length of the garden on a scale drawing if the scale is $\frac{1}{4}$ inch = 1 foot?
 - A. 12 inches wide; 32 inches long
 - **B.** $\frac{3}{4}$ inch wide; 32 inches long
 - **C**, $\frac{3}{1}$ inch wide; 2 inches long
 - D. 2 inches wide; 12 inches long









- **B.** 4.4%
- **C.** 2.8%

D. 22.0%

0% 0% 0% ► ★ C ↓ **CheckPoint**



Express the decimal 0.007 as a percent. Round to the nearest tenth percent, if necessary.

- A. 70 percent
- **B.** 7 percent



D. 0.07 percent

🗖 A 🗖 B 🗖 C 🗖 D







Express 32% as a decimal and as a fraction in simplest form.



0%

🗖 A 🗆 B 🗖 C 🗖 D





Express 6% as a decimal and as a fraction in simplest form.











18 is what percent of 75? Use the percent proportion to solve the problem.

- **A. 0.04%**
- **B.** 0.24%



D. 41%







What is 56% of 125? Use the percent proportion to solve the problem.

A. 45

B. 60



D. 81

■ A □ B ■ C ■ D







4.5 is what percent of 98? Use the percent proportion to solve the problem.



B. 4%

C. 0.25%

D. 0.04%





At a bake sale, 63 cookies were sold. This was 75% of the number of cookies baked. How many cookies were baked?

A. 19 cookies

- **B.** 21 cookies
- C. 47 cookies



🗖 A 🗖 B 🗖 C 🗖 D







Twenty-four of 30 students in a class met their goal in the pizza sale. What percent of the students did not meet their goal in the sale?

0%

A. 80%

B. 76%

C.) 20%

D. 6%







Which of the following state a correct estimate for 79% of 40, along with the method used for estimation?

$$\frac{4}{5} \bullet 40 = 32$$
; fraction method

- B. 0.8 80 = 64; 1 percent method
- **C.** $4 \bullet 4 = 16$; meaning of percent method
- **D.** $1 \bullet 40 = 40$; 1 percent method

0%

 $\leftarrow \rightarrow$



Which of the following states a correct estimate for 67% of 120, along with the method used for estimation?

A. 0.7 ● 70 = 49; 1 percent method

B.
$$\frac{1}{3} \bullet 120 = 40$$
; fraction method

C.
$$(60 \bullet 1) + (6 \bullet 2) = 72;$$

meaning of percent method

$$\frac{2}{3} \bullet 120 = 80$$
; fraction method





In 1990, the population of a town was about 65,000. By 2000, the population increased to about 180% of the 1990 figure. About how many people live in the town in 2000.



117,000

B. 65,180

C. 52,000

D. 11,700

🗖 A 🗆 B 🗖 C 🗖 D







6 A store is having a 25%-off sale on all televisions. About how much will a television that regularly sells for \$359 cost?





Solve the problem using the percent equation. 24 is what percent of 80?





C. 25%

D. 20%





Solve the problem using the percent equation. 39 is 52% of what number?

- **A.** 65
- **B.** 68



D. 78

■ A ■ B ■ C ■ D









What is the annual interest rate if \$2500 is invested for 2 years and \$225 in interest is earned?





C. 4.2%

D. 3.5%





One season the Miami Dolphins had 10 wins. This was 62.5% of the games the team played. How many did they play?





B. \$45

C. \$244

D. \$245.65

0%

🗖 A 🗖 B 🗖 C 🗖 D





State whether the change from \$15 to \$18 is a percent of increase or a percent of decrease and find the percent of change. Round to the nearest tenth, if necessary.

- A. percent of decrease; -20%
- B. percent of decrease; -16.7%
- C. percent of increase; 16.7%
 - percent of increase;
 20%





State whether the change from 80 lb to 72 lb is a percent of increase or a percent of decrease and find the percent of change. Round to the nearest tenth, if necessary.

- **A**,
- percent of decrease; -10%
- B. percent of decrease; -11.1%
- C. percent of increase; 10%
- D. percent of increase; 11.1%

🗖 A 🗆 B 🗖 C 🗖 D







State whether the change from 325 ft to 280 ft is a percent of increase or a percent of decrease and find the percent of change. Round to the nearest tenth, if necessary.

- A. percent of decrease; -16.1%
 - percent of decrease; –13.8%
- C. percent of increase; 13.8%
- D. percent of increase; 16.1%







Myra bought a new car. Her monthly car payment went from \$294 to \$324. Find the percent of change.

- A. percent of decrease of 10.2%
- B. percent of decrease of 9.25%



D. percent of increase of 9.25%





Ratio, Proportion, and Percent

ve-Minute CHECK

Standardized Test Practice

B Refer to the table. Which represents the percent of change in the total number of students between the two school years?

A .	4%
------------	----

- **B.** 4.5%
- **C.** 5%
- **D.** 10%

Number of Students	2001–2002	2002–2003
6th Grade	420	462
7th Grade	432	422
8th Grade	398	416

(over Lesson 6-9)

